

Interpolating Refinable Functions and Wavelets for General Scaling Matrices

Stephan Dahlke ^{*}
Institut für Geometrie
und Praktische Mathematik
RWTH Aachen
Templergraben 55
52056 Aachen
Germany

Peter Maass [†]
Fachbereich Mathematik
Universität Potsdam
Postfach 601553
14415 Potsdam
Germany

Abstract

This paper introduces a general procedure for constructing interpolating refinable functions for arbitrary dilation matrices. The key ideas are based on the construction presented in [24]. Several families of interpolating refinable functions are computed explicitly. They originate from a convolution product of some simple function, either generalized B-splines or the Laplace scheme. A suitable correction is added to obtain interpolating solutions.

Key Words: Interpolating scaling functions, spline functions, wavelets, expanding scaling matrices.

AMS Subject classification: Primary 26B05, 41A05, 41A15, secondary 41A30, 41A63.

^{*}This work has been supported by the Volkswagen-Stiftung (RiP-Programm Oberwolfach)

[†]This work has been supported by the Volkswagen-Stiftung (RiP-Programm Oberwolfach) and BMBF under grant 03-MA7POT-6