

$$\mathbb{L}^* = Q_e \mathbb{L}^t Q_e$$

$$\overset{t}{\mathbb{L}}=P_{e\mathbb{L}}\mathbb{L}^{-1}\text{ trans }\mathsf{C}(\mathbb{L};e)$$

$$\mathbb{L}\in\mathsf{C}|\overset{\perp}{\mathbb{L}}\Rightarrow P(\mathsf{L}\mathbb{L})=Q_eQ_{\mathsf{L}\mathbb{L}}=Q_e\overset{*}{\mathbb{L}}Q_{\mathsf{L}}\mathbb{L}=Q_e\overset{*}{\mathbb{L}}Q_eP_{\mathsf{L}}\mathbb{L}\underset{\mathsf{L}=e}{\Rightarrow}e\mathbb{L}\in\mathsf{C}^\perp$$

$$\overset{t}{\mathbb{L}}=P_{e\mathbb{L}}\mathbb{L}^{-1}\Rightarrow Q_{\mathsf{L}\mathbb{L}}=Q_e\overset{t}{\mathbb{L}}Q_eQ_{\mathsf{L}}\mathbb{L}=\overset{*}{\mathbb{L}}Q_{\mathsf{L}}\mathbb{L}$$

$$\mathsf{L}\in\mathsf{C}^\perp$$

$$\mathbb{L}\in\mathsf{C}|\overset{\perp}{\mathbb{L}}\Rightarrow\mathsf{L}\mathbb{L}\in\mathsf{C}^\perp$$

$$(\mathsf{L}\mathbb{L})^{-1}=\mathsf{L}^{-1}\overset{t-1}{\mathbb{L}}$$

$$P_{\mathsf{L}\mathbb{L}}=\overset{t}{\mathbb{L}}P_{\mathsf{L}}\mathbb{L}\text{ inv}\Rightarrow\mathsf{L}\mathbb{L}\in\mathsf{C}^\perp$$

$$(\mathsf{L}\mathbb{L})^{-1}=(\mathsf{L}\mathbb{L})P_{\mathsf{L}\mathbb{L}}^{-1}=(\mathsf{L}\mathbb{L})\widehat{\overset{t}{\mathbb{L}}P_{\mathsf{L}}\mathbb{L}}^{-1}=\widehat{\mathbb{L}P_{\mathsf{L}}}^{-1}\overset{t-1}{\mathbb{L}}=\mathsf{L}^{-1}\overset{t-1}{\mathbb{L}}$$

$$\otimes \frac{B\left(u\!:\!v\right)=\overset{u}{B}_v}{\left(u\!:\!v\right)\in\mathbb{L}\!\times\!\mathbb{L}_{\mathsf{C}}\text{ qu-inv}}\sqsubset\mathsf{C}|\mathbb{L}$$

$$\ominus \frac{\overset{*}{\mathbb{L}}\mathbb{L}}{\mathbb{L}\in\mathbb{L}}\sqsubset\mathsf{E}|\mathbb{L}$$

$$\overset{u}{B}_v^*=\overset{v}{B}_u$$

$$\left(\overset{*}{uv}\right)^*=\overset{*}{v}u$$

$$(u\!:\!v)\in\mathbb{L}\!\times\!\mathbb{L}_{\mathsf{C}}\Rightarrow\overset{u}{B}_v\in\mathsf{C}|\mathbb{L}$$

$$\mathbb{L}\in\mathsf{C}|\mathbb{L}\Rightarrow\mathsf{L}^{-1}\overset{u}{B}_v\mathbb{L}=\overset{u}{\widetilde{\mathbb{L}}}B_{v\mathbb{L}}$$

$$\overset{*}{b}c\times\overset{*}{a}d=\overset{*}{b}\left(c\overset{*}{a}d\right)-\left(\overset{*}{a}db\right)c$$

$$\overset{*}{b}c\times\mathbb{L}=\overset{*}{b}c\mathbb{L}-\left(\overset{*}{b}\overset{*}{\mathbb{L}}\right)c$$

$$\exp 2\overset{*}{v}u=B\left(\sum_{1\leqslant n}\frac{1}{n!}u\big(\overset{*}{vu}\big)^{n-1}\colon-v\right)$$

$$P_{uP_v}=P_u\,P_v\,P_u$$

$$\begin{aligned}
eP_v = v^2 \in \mathbb{C}^{\perp} &\Rightarrow P_v \in \mathbb{C}^{\perp} \\
\overset{t}{P}_v &= P_v \\
P_v^* = Q_e P_v Q_e &= Q_e \left(Q_e Q_v Q_e \right) = Q_e Q_{v^*} = P_{v^*} \\
a:b \in \mathbb{C}^{\perp} &\Rightarrow P_b^* P_a = Q_e P_b Q_e P_a = Q_b Q_a = B \left(\overset{*}{b}:a + b^{-1} \right) \\
\mathbb{L} \in \mathbb{C}^{\perp} &\Rightarrow a\mathbb{L} \in \mathbb{C}^{\perp} \\
\mathbb{L}^{-1} P_a \mathbb{L} &= P_{e\mathbb{L}}^{-1} \overset{t}{\mathbb{L}} P_a \mathbb{L} = P_{e\mathbb{L}}^{-1} P_{a\mathbb{L}}
\end{aligned}$$

$$\otimes \frac{P_v}{v \in \mathbb{L}^U} = \otimes \frac{Q_u Q_{\dot{u}}}{\dot{u} \in \mathbb{L}^U} \sqsubset U | \mathbb{L}$$

$$\begin{aligned}
\dot{a} \in \mathbb{L}^U &\Rightarrow P_a^* = P_{a^*} = P_{a^{-1}} = P_a^{-1} \\
v Q_a^2 &= a \left(a \overset{*}{v} a \right) a = 2 \left(v \overset{*}{a} a \right) \overset{*}{a} a - v \overset{*}{a} \left(a Q_a \right) = v \\
&\Rightarrow \widehat{Q_a Q_{\dot{a}}}^* = \widehat{P_{a^*} P_{\dot{a}}}^* = P_{\dot{a}^*} P_a = P_{\dot{a}} P_{a^*} = \widehat{P_{a^*} P_{\dot{a}}}^t = \widehat{Q_a Q_{\dot{a}}}^t
\end{aligned}$$

$$\otimes \frac{P_v}{v \in \mathbb{L}^U} = \otimes \frac{Q_u Q_{\dot{u}}}{\dot{u} \in \mathbb{L}^U} \sqsubset U | \mathbb{L}$$

$$\begin{aligned}
\dot{a} \in \mathbb{L}^U &\Rightarrow P_a^* = P_{a^*} = P_{a^{-1}} = P_a^{-1} \\
v Q_a^2 &= a \left(a \overset{*}{v} a \right) a = 2 \left(v \overset{*}{a} a \right) \overset{*}{a} a - v \overset{*}{a} \left(a Q_a \right) = v \Rightarrow \widehat{Q_a Q_{\dot{a}}}^* = \widehat{P_{a^*} P_{\dot{a}}}^* = P_{\dot{a}^*} P_a = P_{\dot{a}} P_{a^*} = \widehat{P_{a^*} P_{\dot{a}}}^t = \widehat{Q_a Q_{\dot{a}}}^t
\end{aligned}$$