

$$\overset{\circ}{\mathcal{U}}|\mathbb{1} = \frac{\mathcal{L} \in \mathcal{U}|\mathbb{1}}{\overline{\mathcal{L}|\mathbb{1}}_{\mathbb{K}}} \stackrel{\text{abg } * \text{-ideal}}{\subseteq} \mathcal{U}|\mathbb{1}$$

$$\mathcal{L} \in \overset{\circ}{\mathcal{U}}|\mathbb{1} \Rightarrow \overline{\mathcal{L}|\mathbb{1}}_{\mathbb{K}} \text{ cpt} \Rightarrow \mathcal{L}|\mathbb{1} \text{ bes} \Rightarrow \mathcal{L} \text{ stet}$$

$$\mathcal{L} \in \overline{\overset{\circ}{\mathcal{U}}|\mathbb{1}}$$

$$\mathcal{L}|\mathbb{1} \text{ precpt}$$

$$\bigwedge_{\varepsilon > 0} \bigvee_{\mathbb{K}} \overline{\mathcal{L} - \mathbb{K}} \leq \varepsilon$$

$$\overline{\mathcal{L}|\mathbb{1}}_{\mathbb{K}} \text{ cpt} \Rightarrow \mathbb{K}|\mathbb{1} \text{ pre-cpt} \Rightarrow \bigvee_{\text{fin } \mathbb{K} \subset \mathbb{1}} \mathbb{K}|\mathbb{1} \subset \bigcup_{\mathbb{K} \in \mathbb{K}} \mathbb{1}_{\mathbb{K}}^{\mathbb{K}}$$

$$\mathcal{L}|\mathbb{1} \subset \bigcup_{\mathbb{K} \in \mathbb{K}} \mathbb{1}_{\mathbb{K}}^{\mathbb{K}}$$

$$\mathcal{L} \in \mathbb{1} \Rightarrow \mathbb{K}|\mathbb{1} \in \mathbb{K}|\mathbb{1} \Rightarrow \bigvee_{\mathbb{K} \in \mathbb{K}} \overline{\mathbb{K}|\mathbb{1} - \mathbb{K}|\mathbb{1}} \leq \varepsilon$$

$$\Rightarrow \overline{\mathcal{L}|\mathbb{1} - \mathcal{L}|\mathbb{1}} \leq \overline{\mathcal{L}|\mathbb{1} - \mathbb{K}|\mathbb{1}} + \overline{\mathbb{K}|\mathbb{1} - \mathbb{K}|\mathbb{1}}^{\leq \varepsilon} + \overline{\mathbb{K}|\mathbb{1} - \mathcal{L}|\mathbb{1}} \leq \overline{\mathcal{L} - \mathbb{K}}^{\leq \varepsilon} \stackrel{\leq 1}{\leq} \varepsilon + \varepsilon + \overline{\mathbb{K} - \mathcal{L}}^{\leq 1} \leq 3\varepsilon$$

$$\Rightarrow \text{voll metr } \mathbb{1} \supset \mathcal{L}|\mathbb{1} \text{ precpt}$$

$$\stackrel{\text{Thm}}{\Rightarrow} \overline{\mathcal{L}|\mathbb{1}}_{\mathbb{K}} \text{ cpt} \Rightarrow \mathcal{L} \in \overset{\circ}{\mathcal{U}}|\mathbb{1}$$

$$\overset{\circ}{\mathcal{U}}|\mathbb{1} \stackrel{\text{hull}}{\subseteq} \overset{\circ}{\mathcal{U}}|\mathbb{1} = \overline{\overset{\circ}{\mathcal{U}}|\mathbb{1}}$$

$$\mathcal{L} \in \overset{\circ}{\mathcal{U}}|\mathbb{1} \Rightarrow \overline{\mathcal{L}|\mathbb{1}}_{\mathbb{K}} \text{ cpt met} \Rightarrow \overline{\mathcal{L}|\mathbb{1}}_{\mathbb{K}} \text{ met abz} \Rightarrow \mathbb{1} \supset \overline{\mathcal{L}|\mathbb{1}} \text{ met abz} \Rightarrow \bigvee_{\text{abz ONB}} \mathcal{L}^i \in \overline{\mathcal{L}|\mathbb{1}}$$

$$\bigwedge_N P_N = \sum_i^N \mathcal{L}^i \mathcal{L}^i \in \overset{\circ}{\mathcal{U}}|\mathbb{1} \ni P_N \mathcal{L} = \sum_i^N \mathcal{L}^i \mathcal{L}^i \mathcal{L} = \sum_i^N \mathcal{L}^i \left(\overset{*}{\mathcal{L}|\mathbb{1}} \right)$$

$$\bigwedge_{\Gamma \in \mathbb{I}} \Gamma \Vdash \Gamma = \sum_i \Gamma^i \overline{\Gamma^i \times \Gamma} \underset{N \rightsquigarrow \infty}{\approx} \sum_i^N \Gamma^i \overline{\Gamma^i \times \Gamma} = \overline{P_N \Gamma}$$

$$\Gamma \in \overline{\emptyset | \mathbb{I}}$$

$$\bigwedge_{\varepsilon > 0} \bigwedge_{\Gamma \in \overline{\Gamma | \mathbb{I}}} \bigvee_{\Gamma \in \mathbb{I}} \overline{\Gamma - \Gamma} < \varepsilon \Rightarrow \overline{\Gamma | \mathbb{I}} \subset \bigcup_{\Gamma \in \mathbb{I}} \overline{\Gamma}^{\leq \varepsilon} \text{ off deck}$$

$$\stackrel{\text{cpt}}{\Rightarrow} \bigvee_{\text{fin } \mathbb{Y} \subset \mathbb{I}} \overline{\Gamma | \mathbb{I}} \subset \bigcup_{\mathbb{Y} \in \mathbb{Y}} \overline{\mathbb{Y} + \varepsilon}$$

$$\bigwedge_{\mathbb{Y} \in \mathbb{Y}} \bigvee_{N_{\mathbb{Y}}} \bigwedge_{N \supset N_{\mathbb{Y}}} \overline{\mathbb{Y} - P_N \mathbb{Y}} \leq \varepsilon$$

$$\overline{\Gamma - P_N \Gamma} \leq \varepsilon$$

$$\bigwedge_{\Gamma \in \mathbb{I}} \bigvee_{\mathbb{Y} \in \mathbb{Y}} \overline{\Gamma - \mathbb{Y}} \leq \varepsilon \Rightarrow \bigwedge_{N \supset \bigcup_{\mathbb{Y} \in \mathbb{Y}} N_{\mathbb{Y}}} \overline{P_N \Gamma - \mathbb{Y}} \leq \overline{P_N}^{\leq 1} \overline{\Gamma - \mathbb{Y}}^{\leq \varepsilon} \leq \varepsilon$$

$$\Rightarrow \overline{\Gamma - P_N \Gamma} \leq \overline{\Gamma - \mathbb{Y}}^{\leq \varepsilon} + \overline{\mathbb{Y} - P_N \mathbb{Y}}^{\leq \varepsilon} + \overline{P_N \mathbb{Y} - P_N \Gamma}^{\leq \varepsilon} \leq 3\varepsilon \stackrel{\text{bel}}{\Rightarrow} \overline{\Gamma - P_N \Gamma} \leq \varepsilon$$

$$\stackrel{\varepsilon \text{ bel}}{\Rightarrow} \Gamma \in \overline{\emptyset | \mathbb{I}}$$