

$$n \leq n \triangleleft \mathbb{K} = \left\{ \begin{array}{l} \mathbb{L} \in \mathbb{K}^{n \times n} \\ i > j \Rightarrow \mathbb{L}^j = 0 \end{array} \right. \quad \text{upper triangular matrix}$$

$$\mathbb{L} * \mathbb{Z} \in n \leq n \triangleleft \mathbb{K} \xleftarrow[\text{bilin}]{*} n \leq n \triangleleft \mathbb{K} \otimes n \leq n \triangleleft \mathbb{K} \ni \mathbb{L} : \mathbb{Z}$$

$$\mathbb{L} * \mathbb{Z}^k = \sum_j \mathbb{L}^j \mathbb{Z}^k \quad \text{matrix product}$$

$$\left\{ \begin{array}{l} j < i \quad \curvearrowright \mathbb{L}^j = 0 \\ k < j \quad \curvearrowright \mathbb{Z}^k = 0 \end{array} \right. \Rightarrow \mathbb{L} * \mathbb{Z}^k = \sum_j \mathbb{L}^j \mathbb{Z}^k = \sum_j \mathbb{L}^j \mathbb{Z}^k$$

$$I = \begin{array}{c|cc} 1 & \dots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \dots & 1 \end{array} \mathbb{L}^j = \begin{cases} 1 & i = j \\ 0 & i \neq j \end{cases}$$