

$$\bigwedge_{L^j}^{\mathbb{R}^n > 0} \bigwedge_{\varepsilon}^{\mathbb{Z}} \bigvee_{p^j}^{\mathbb{Z}_{>}} \bigvee_q L^j - \varepsilon < \frac{p^j}{q} \leq L^j < \frac{p^j + 1}{q} < L^j + \varepsilon$$

$$\bigwedge_j^n \bigvee_{a^j}^{\mathbb{Z}} \bigvee_{b^j}^{\mathbb{Z}_{>}} L^j - \varepsilon < \frac{a^j}{b^j} \leq L^j$$

$$\bigvee_{b^n}^{\mathbb{Z}_{>}} \frac{1}{b^n} < \varepsilon \Rightarrow L^j - \varepsilon < \frac{b^0 \cdot b^{j-1} a^j b^{j+1} \cdot b^{n-1} b^n}{b^0 \dots b^n} \leq L^j$$

$$0 < \frac{1}{b^0 \dots b^n} < \varepsilon \Rightarrow \bigwedge_j^n \frac{c \in \mathbb{Z}}{L^j - \varepsilon < \frac{c}{b^0 \dots b^n} \leq L^j} \neq \emptyset$$

$$\Rightarrow \bigvee_{p^j}^{\mathbb{Z}} L^j - \varepsilon < \frac{p^j}{b^0 \dots b^n} \leq L^j < \frac{p^j + 1}{b^0 \dots b^n}$$

$$\frac{p^j + 1}{b^0 \dots b^n} - L^j \leq \frac{p^j + 1}{b^0 \dots b^n} - \frac{p^j}{b^0 \dots b^n} = \frac{1}{b^0 \dots b^n} \leq \frac{1}{b^n} < \varepsilon \Rightarrow \frac{p^j + 1}{b^0 \dots b^n} < L^j + \varepsilon$$

$$\bigwedge_{t^j}^{\mathbb{Z}^n} Q_t^j = \frac{L^j \in \mathbb{R}^n}{\frac{2t^j}{t} \leq L^j < \frac{2t^j + 2}{t}}$$

$$\bar{\lambda} \subset \bigcup_{Q_t^{v'} \subset \bar{\lambda}} Q_t^{v'} = \bigcup_t^{\mathbb{Z}_{>}} \bigcup_{Q_t^{v'} \subset \bar{\lambda}} Q_t^{v'}$$

$$\begin{aligned} L \in \bar{\lambda} &\Rightarrow \bigvee_{\varepsilon}^{>0} \frac{h'}{L^j - \varepsilon < h' < L^j + \varepsilon} \subset \bar{\lambda} \\ &\Rightarrow \bigvee_{p'}^{\mathbb{Z}^n} \bigvee_q^{\mathbb{Z}_{>}} L^j - \varepsilon < \frac{p^j}{q} \leq L^j < \frac{p^j + 1}{q} < L^j + \varepsilon \\ &\Rightarrow L' \in Q_{2q}^{p'} \subset \frac{h'}{L^j - \varepsilon < h' < L^j + \varepsilon} \subset \bar{\lambda} \end{aligned}$$

$$\left\{ \begin{array}{l} \mathbb{R}^n \supset_{\text{conv}} \bar{\lambda} = -\bar{\lambda} \\ \overline{\bar{\lambda}} > 2^n \end{array} \right. \xrightarrow{\text{MIN}} \bar{\lambda} \cup \mathbb{Z}^n \neq \emptyset$$

$$2^n < \overline{\bar{\lambda}} = \overline{\bar{\lambda}} \underset{t \sim_{\infty}}{\approx} \overline{\bigcup_{Q_t^{v'} \subset \bar{\lambda}} Q_t^{v'}}$$

$$\Rightarrow \bigvee_t^{\mathbb{Z}_{>}} 2^n < \overline{\bigcup_{Q_t^{v'} \subset \bar{\lambda}} Q_t^{v'}} \leq \left(\frac{2}{t}\right)^n \overline{\mathbb{Z}^n \cap \frac{\bar{\lambda}t}{2}} \Rightarrow \overline{\mathbb{Z}^n \cap \frac{\bar{\lambda}t}{2}} > t^n$$

$$\Rightarrow v' = qt + r' \in \underbrace{\mathbb{Z}^n \cap \frac{\bar{\lambda}t}{2}}_{\text{not inj}} \rightarrow t^n \ni r'$$

$$\Rightarrow \bigvee_{v'}^{\text{dist}} \begin{cases} 2v' \in \bar{\lambda} \ni 2v' \\ v' - qt = r' = r' = v' - qt \Rightarrow 0 \neq v' - v' = \underbrace{q' - q}_t t \end{cases}$$

$$\xrightarrow[\text{symm}]{\bar{\lambda}} -2v'/t \in \bar{\lambda} \xrightarrow[\text{conv}]{\bar{\lambda}} \bar{\lambda} \ni \frac{2v'/t + \overline{-2v'/t}}{2} = \frac{v' - v'}{t} = \underbrace{q' - q}_{\neq 0} \in \mathbb{Z}^n$$