

$$x:y\eta = \begin{cases} \frac{xy}{\sqrt{x^2+y^2}} & x:y \neq 0:0 \\ 0 & x:y = 0:0 \end{cases} \Rightarrow \begin{cases} \text{stet} \\ \text{part diff} \\ \text{keine Richtungsabl} \\ \text{nicht total diff} \end{cases}$$

$$x\eta_k = x:kx\eta = \frac{kx^2}{\sqrt{x^2+k^2x^2}} = \frac{k\sqrt{x}}{\sqrt{1+k^2}} = \begin{cases} \frac{kx}{\sqrt{1+k^2}} & x > 0 \\ -\frac{kx}{\sqrt{1+k^2}} & x < 0 \end{cases} \Rightarrow \text{keine Richtungsableitung for } k \neq 0:\infty$$

$$x:y\eta = e^y \underbrace{x^2 + 2xy}$$

$$[x\eta \quad y\eta] = e^y [2x + 2y \quad x^2 + 2xy + 2x]$$

$$[x\eta \quad y\eta] = [0 \quad 0] \Leftrightarrow \begin{cases} y = -x \\ 0 = x^2 + 2xy + 2x = x^2 - 2x^2 + 2x = 2x - x^2 \Rightarrow x = 0:2 \end{cases} \Rightarrow x:y = \begin{cases} 0:0 \\ 2:-2 \end{cases}$$

$$\frac{x\eta \mid x\eta}{x\eta \mid y\eta} = 2e^y \frac{1}{x+y+1} \mid \frac{x+y+1}{x^2/2+xy+2x} = 2 \begin{cases} \frac{1}{1} \mid \frac{1}{0} & x:y = 0:0 \text{ saddle} \\ e^{-2} \frac{1}{1} \mid \frac{1}{2} & x:y = 2:-2 \text{ min} \end{cases}$$

$$x:y\eta = xy \ln(x^2 + y^2) \text{ extr}$$

$$x:y\gamma = x + y + \sqrt{1 - x^2 - y^2} \text{ extr}$$

$$n > 0 \Rightarrow \int_{dx}^{a|\infty} \frac{\ln(x)}{x^{n+1}} = \frac{1}{na^n} \left( \ln(a) + \frac{1}{n} \right) : \int_{dx}^{1|\infty} \frac{\ln(x)}{x^{n+1}} = \frac{1}{n^2} \text{ part int}$$

$$n \int_{dx} \frac{\ln(x)}{x^{n+1}} = - \int_{dx} \ln(x) \frac{dx^{-n}}{dx} = - \frac{\ln(x)}{x^n} + \int_{dx} \frac{d \ln(x)}{dx} x^{-n} = - \frac{\ln(x)}{x^n} + \int_{dx} \frac{1}{x^{n+1}} = - \frac{\ln(x)}{x^n} - \frac{x^{-n}}{n}$$

$$n \int_{dx}^{a|\infty} \frac{\ln(x)}{x^{n+1}} = - \frac{\ln(x)}{x^n} - \frac{x^{-n}}{n} = \frac{\ln(a)}{a^n} + \frac{a^{-n}}{n}$$

$$\int_{dx}^{a|\infty} \frac{\ln(x)}{x} = \infty \text{ subst}$$

$$u = \ln(x) \Rightarrow du = \frac{dx}{x} \Rightarrow \int_{dx} \frac{\ln(x)}{x} = \int_{du} u = \frac{u^2}{2} = \frac{\ln^2(x)}{2}$$

$$x\gamma = \int_{dy}^{1|x^2} y \not\Rightarrow \begin{cases} \gamma \text{ diff} \\ x\gamma \end{cases}$$

$$\text{fund thm} \Rightarrow \int_{dx}^{0|\pi/4} \frac{1}{1+x^2}$$

$$y < R \Rightarrow \int_{dx}^{0|y} \sum_n^{\mathbb{N}} a_n x^n = \sum_n^{\mathbb{N}} a_n \frac{y^{n+1}}{n+1} \text{ unif conv}$$

$$\begin{cases} \mathbb{R} \xrightarrow{\gamma} \mathbb{R} \\ n+1 \text{ diff} \\ \gamma_{n+1} = 0 \end{cases} \Rightarrow \begin{cases} \gamma \text{ poly} \\ \deg \gamma \leq n \end{cases}$$

$$\bigwedge_{x:y}^{\mathbb{R}} \sqrt[2x_{\mathfrak{s}} - 2y_{\mathfrak{s}}]{} \leq 2 \sqrt{x - y}$$

$$\bigwedge_{-1 \leq y \leq 1} \bigvee_x^{\mathbb{R}} : y = {}^x \mathbf{c}$$

$$\left\{ \begin{array}{l} 0 \\ \xrightarrow[\text{stet}]{\gamma_n} \\ \sqrt[x]{\gamma} \leq 1/2^n \end{array} \right\} \mathbb{R} \Rightarrow \left\{ \begin{array}{l} \sum_n^{\mathbb{N}} {}^x \gamma_n \text{ glm conv} \\ 0 \\ \xrightarrow[\text{stet}]{\sum_n^{\mathbb{N}} \gamma_n} \\ \mathbb{R} \end{array} \right.$$