



$$\nabla \underline{1} = 0 \Rightarrow \bigvee^1_1 \begin{cases} \underline{\underline{1}} = 0 \\ \underline{\underline{1}} = \underline{\underline{1}} \end{cases}$$

$$\nabla_{\leftarrow} \underline{1} = \nabla_{\leftarrow} \underline{1} = 0 \underset{\text{mex}}{\Rightarrow} \bigvee^1_1 \underline{\underline{1}} = \underline{\underline{1}} \Rightarrow \nabla_{\leftarrow} \underline{1} = \nabla_{\leftarrow} \underline{1} = \underline{\underline{1}} = 0 \underset{\text{rex}}{\Rightarrow} \underline{\underline{1}} = 0$$

$$\nabla - \nabla \in \underline{\underline{1}} \begin{cases} \nabla = \nabla \nabla & \nabla = \nabla \nabla \\ \underline{\nabla} = \underline{\nabla} \nabla & \underline{\nabla} = \underline{\nabla} \nabla \end{cases} \Rightarrow \nabla - \nabla \in \underline{\underline{1}}$$

$$\begin{aligned} \nabla - \nabla = \underline{\underline{1}} &\underset{\text{lex}}{\Rightarrow} \bigvee^1_1 \nabla = \nabla \nabla \Rightarrow \nabla \underbrace{\nabla - \nabla - \underline{\underline{1}}}_{\underline{\underline{1}}} = \nabla - \nabla - \underline{\underline{1}} = 0 \underset{\text{mex}}{\Rightarrow} \bigvee^1_1 \nabla - \nabla - \underline{\underline{1}} = \underline{\underline{1}} \\ &\Rightarrow \nabla \underbrace{\nabla - \nabla - \underline{\underline{1}}}_{\underline{\underline{1}}} = \nabla - \nabla - \underline{\underline{1}} = \nabla - \nabla - \nabla - \nabla - \underline{\underline{1}} = \underline{\underline{1}} = 0 \underset{\text{rex}}{\Rightarrow} \nabla - \nabla = \underline{\underline{1}} \in \underline{\underline{1}} \end{aligned}$$

$$\begin{cases} \nabla \underline{1} = 0 \\ \underline{\underline{1}} = \underline{\underline{1}} \end{cases} \Rightarrow \overrightarrow{\nabla \underline{1}} + \overleftarrow{\underline{\underline{1}}} = \underline{1} + \underline{\underline{1}}$$

$$\text{Im } \mathcal{L}_* \subset \text{Ker } \omega$$

$$\overleftarrow{1} = 0 = \overline{1}0 \Rightarrow \overrightarrow{\overline{1}\overleftarrow{1} + \overleftarrow{1}} = 0 + \overleftarrow{1}$$

$$\text{Ker } \omega \subset \text{Im } \mathcal{L}_*$$

$$\begin{aligned} \begin{cases} \overleftarrow{\overline{1}} = 0 \\ \overleftarrow{1} = \overline{1} \end{cases} \quad 0 = \overrightarrow{\overline{1}\overleftarrow{1} + \overleftarrow{1}} = \overline{1} + \overleftarrow{1} \Rightarrow \overline{1} \in \overleftarrow{1} \Rightarrow \overline{1} = \overleftarrow{1} \Rightarrow \overline{1} - \overline{1}\overline{1} = \overleftarrow{1} - \overline{1}\overleftarrow{1} = \overleftarrow{1} - \overline{1} = 0 \\ \Rightarrow \begin{cases} \overline{1} - \overline{1}\overline{1} \in \overleftarrow{1} \\ \overline{1}\overline{1} - \overline{1}\overline{1} = \overline{1} - \underbrace{\overline{1}\overline{1}}_{=0} = \overline{1} \end{cases} \Rightarrow \overline{1} \overrightarrow{\overline{1} - \overline{1}\overline{1} + \overleftarrow{1}} = \overline{1}\overleftarrow{1} + \overleftarrow{1} \end{aligned}$$

$$\text{Im } \omega \subset \text{Ker } \mathcal{L}_*$$

$$\begin{cases} \overleftarrow{1} = 0 \\ \overline{1} = \overleftarrow{1} \end{cases} \Rightarrow \overline{1} \overrightarrow{\overline{1}\overleftarrow{1} + \overleftarrow{1}} = \overline{1} (\overline{1} + \overleftarrow{1}) = \overline{1}\overleftarrow{1} + \overleftarrow{1} = \overleftarrow{1} + \overleftarrow{1} = 0 + \overleftarrow{1}$$

$$\text{Ker } \mathcal{L}_* \subset \text{Im } \omega$$

$$\begin{cases} \overleftarrow{1} = 0 \\ 0 = \overline{1} \overrightarrow{\overline{1} + \overleftarrow{1}} = \overline{1}\overleftarrow{1} + \overleftarrow{1} \end{cases} \Rightarrow \overline{1} \in \overleftarrow{1} \Rightarrow \overline{1} = \overleftarrow{1} \Rightarrow \overline{1} + \overleftarrow{1} = \overrightarrow{\overline{1} + \overleftarrow{1}}$$