

$$g_{\mathbb{R}} = \frac{m}{q} \Big| \frac{p}{n} \in {}_2\mathbb{R}_r^{\Omega}$$

$$z = x + iy = \overset{\dagger}{z}$$

$$g_{\mathbb{R}}(z) = \underbrace{mz + p}_{-1} \overbrace{qz + n}^{-1} \in G_{\mathbb{R}}$$

$$\overset{\dagger}{m}q = \overset{\dagger}{q}m: \quad \overset{\dagger}{p}n = \overset{\dagger}{n}p: \quad \overset{\dagger}{m}n - \overset{\dagger}{q}p = 1 = \overset{\dagger}{n}m - \overset{\dagger}{p}q$$

$$\Rightarrow \underbrace{z\overset{\dagger}{m} + \overset{\dagger}{p}}_{-1} \overbrace{qz + n}^{-1} = z\overset{\dagger}{m}qz + \overset{\dagger}{p}n + z\overset{\dagger}{m}n + \overset{\dagger}{p}qz = z\overset{\dagger}{q}mz + \overset{\dagger}{n}p + z\overset{\dagger}{q}p + \overset{\dagger}{n}mz = \underbrace{z\overset{\dagger}{q} + \overset{\dagger}{n}}_{-1} \overbrace{mz + p}^{-1}$$

$$\Rightarrow \overbrace{g_{\mathbb{R}}(z)}^{+} = \underbrace{z\overset{\dagger}{q} + \overset{\dagger}{n}}_{-1} \underbrace{z\overset{\dagger}{m} + \overset{\dagger}{p}}_{-1} = \underbrace{mz + p}_{-1} \overbrace{qz + n}^{-1} = g_{\mathbb{R}}(z)$$

$$\gamma_{\mathbb{R}}(z) = \alpha z + \beta - z\gamma z - z\delta \in \mathfrak{g}_{\mathbb{R}}$$

$$\overbrace{\gamma_{\mathbb{R}}(z)}^{+} = z\overset{\dagger}{\alpha} + \overset{\dagger}{\beta} - z\overset{\dagger}{\gamma}z - \overset{\dagger}{\delta}z = \alpha z + \beta - z\gamma z - z\delta = \gamma_{\mathbb{R}}(z)$$

$$\gamma_{\mathbb{C}}(w) = \overline{\alpha + \delta + i\beta - \gamma} w + \overline{\alpha - \delta - i\beta + \gamma} - w \overline{\alpha - \delta + i\beta + \gamma} - \overline{\alpha + \delta + i\gamma - \beta} w$$