

$$\mathbb{K} \triangleleft \mathbb{H} \rightarrow \mathbb{K} \triangleleft \mathbb{H} \underset{\omega}{\triangleleft} \mathbb{K} = \mathbb{H} \underset{\omega}{\triangleleft} \mathbb{K}$$

$$\mathbb{C} \triangleleft \mathbb{H} \rtimes \mathbb{C} \triangleleft \mathbb{H} \xleftarrow[\#p]{\#d} \mathbb{C} \triangleleft \mathbb{H} \text{ coab bigebr}$$

$$\mathfrak{b} \mathfrak{b} | \gamma \underset{\text{prod}}{=} \#d \left( \mathfrak{b} \mathfrak{z} \mathfrak{b} \right) | \gamma = \mathfrak{b} \mathfrak{z} \mathfrak{b} | | d \gamma = \mathfrak{b} | \gamma \rtimes \mathfrak{b} = \mathfrak{b} | \mathfrak{b} \rtimes \gamma$$

$$\#p \mathfrak{b} | | \gamma \mathfrak{z} \mathfrak{z} \mathfrak{z} \underset{\text{coprod}}{=} \mathfrak{b} | p \mathfrak{z} \mathfrak{z} \mathfrak{z} = \mathfrak{b} | \gamma \mathfrak{z}$$

$$\mathfrak{b}_1 \cdots \mathfrak{b}_n | \gamma = \partial_{t_1}^0 \cdots \partial_{t_n}^0 \epsilon^{t_1 b_1 \dots t_n b_n} \gamma$$

$$\mathfrak{b} | \gamma = \partial_t^0 \epsilon^{tb} \gamma$$

$$d \gamma = \sum_j \gamma_j \mathfrak{z}^j \Rightarrow {}^{st} \gamma = \sum_j {}^s \gamma_j {}^t \gamma^j$$

$$\Rightarrow \mathfrak{b} \mathfrak{b} | \gamma = \mathfrak{b} \mathfrak{z} \mathfrak{b} | | d \gamma = \sum_j \mathfrak{b} | \gamma_j \mathfrak{b} | \gamma^j = \sum_j \left( \partial_s^0 \epsilon^{bs} \gamma_j \right) \left( \partial_t^0 \epsilon^{bt} \gamma^j \right) = \partial_s \partial_t \epsilon^{bs} \epsilon^{bt} \gamma$$

$$\#p \mathfrak{b} = \mathfrak{b} \mathfrak{z} 1 + 1 \mathfrak{z} \mathfrak{b}$$

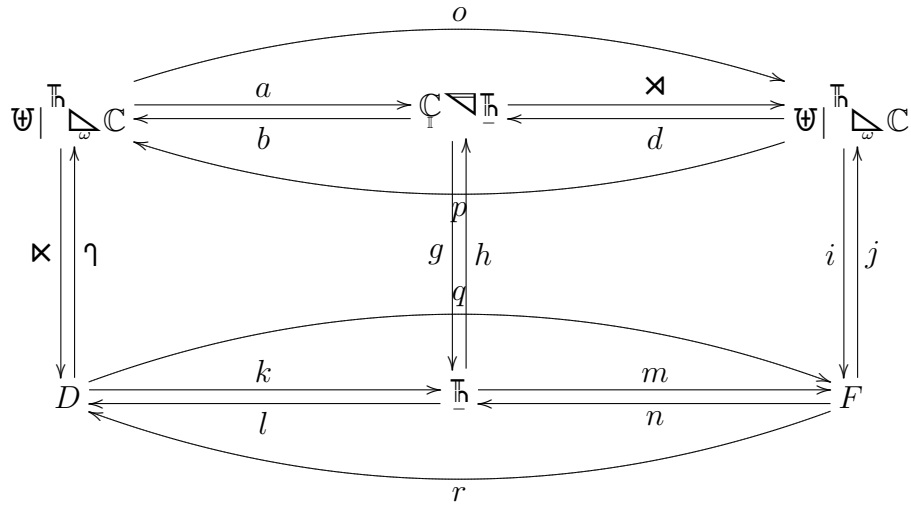
$$\#p \mathfrak{b} | \gamma \mathfrak{z} \mathfrak{z} \mathfrak{z} = \mathfrak{b} | \mathfrak{z} \mathfrak{z} \mathfrak{z} = \overline{\mathfrak{b} \rtimes \mathfrak{z} \mathfrak{z} \mathfrak{z}} = \overline{\mathfrak{b} \rtimes \mathfrak{z}} \epsilon^{\mathfrak{z}} + \epsilon^{\mathfrak{z}} \overline{\mathfrak{b} \rtimes \mathfrak{z} \mathfrak{z}} = \mathfrak{b} | \mathfrak{z} \mathfrak{z} \mathfrak{z} + \mathfrak{z} \mathfrak{z} \mathfrak{z} | \mathfrak{b} = \mathfrak{b} \mathfrak{z} 1 + 1 \mathfrak{z} \mathfrak{b} | | \mathfrak{z} \mathfrak{z} \mathfrak{z}$$

$$\mathbb{C} \underset{\gamma}{\triangleleft} \mathbb{H} \xleftarrow{\epsilon^{\mathfrak{g}}} \mathbb{C} \triangleleft \mathbb{H} \rightarrow \mathbb{H} | \underset{\omega}{\triangleleft} \mathbb{C}$$

$$P | \gamma = \overline{P \rtimes \gamma}$$

$$\mathfrak{b} | \gamma = \partial_t^0 \epsilon^{tb} \gamma$$

$$e | \gamma = \epsilon^{\mathfrak{z}} \gamma$$



$${}^s \overline{\mathbb{C} \rtimes \gamma} = \partial_t^0 {}^{se^{tb}} \gamma \Rightarrow \mathbb{C} \rtimes (\mathbb{C} \rtimes \gamma) - \mathbb{C} \rtimes (\mathbb{C} \rtimes \gamma) = (\mathbb{C} \rtimes \mathbb{C}) \rtimes \gamma$$

$${}^s \overline{\gamma \rtimes \mathbb{C}} = \partial_t^0 {}^{e^{tb}s} \gamma \Rightarrow (\gamma \rtimes \mathbb{C}) \rtimes \mathbb{C} - (\gamma \rtimes \mathbb{C}) \rtimes \mathbb{C} = \gamma \rtimes (\mathbb{C} \rtimes \mathbb{C})$$

$$\underline{P\dot{P}} | \gamma = P | \underline{\dot{P} \rtimes \gamma} = \dot{P} | \underline{\gamma \rtimes P}$$

$$\text{LHS} = \overline{{}^e P\dot{P} \rtimes \gamma} = \overline{{}^e P \rtimes \dot{P} \rtimes \gamma} = P | \underline{\dot{P} \rtimes \gamma}$$

$${}^s \overline{\mathbb{C}_1 \cdots \mathbb{C}_n \rtimes \gamma} = \partial_{t_1}^0 \cdots \partial_{t_n}^0 {}^{se^{t_1 b_1} \cdots e^{t_n b_n}} \gamma$$

$$\underline{\mathbb{C}_1 \cdots \mathbb{C}_n} | \gamma = \partial_{t_1}^0 \cdots \partial_{t_n}^0 {}^{e^{t_1 b_1} \cdots e^{t_n b_n}} \gamma$$

$${}^s \overline{\mathbb{C}_0 \mathbb{C}_1 \cdots \mathbb{C}_n \rtimes \gamma} = \overline{\mathbb{C}_0 \rtimes \underline{\mathbb{C}_1 \cdots \mathbb{C}_n \rtimes \gamma}} = \partial_{t_0}^0 {}^{se^{t_0 b_0}} \overline{\underline{\mathbb{C}_1 \cdots \mathbb{C}_n \rtimes \gamma}}^{\text{Ind}}$$

$$= \partial_{t_0}^0 \partial_{t_1}^0 \cdots \partial_{t_n}^0 {}^{se^{t_0 b_0} e^{t_1 b_1} \cdots e^{t_n b_n}} \gamma$$

$$\Delta P = \sum_i P_i \rtimes P^i \xrightarrow{\text{Leibniz}} P \rtimes \underline{\dot{\gamma}} = \sum_i \underline{P_i \rtimes \gamma} \underline{P^i \rtimes \dot{\gamma}}$$

$$\Delta \mathbb{C} = \mathbb{C} \rtimes e + e \rtimes \mathbb{C}$$

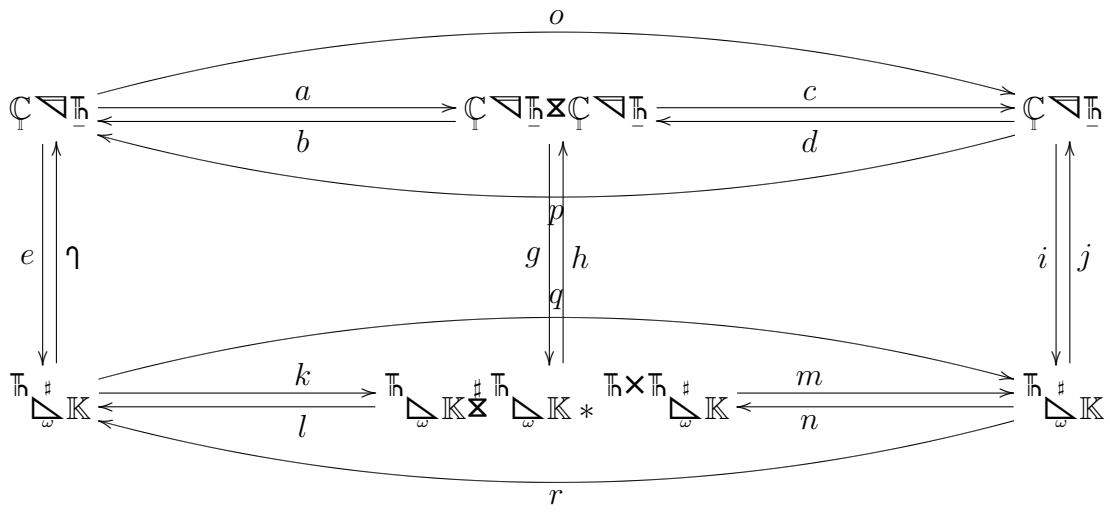
$$\mathbb{C} \rtimes \underline{\dot{\gamma}} = \underline{\mathbb{C} \rtimes \dot{\gamma}} + \underline{\gamma \rtimes \dot{\gamma}} = \underline{\mathbb{C} \rtimes \gamma} \underline{e \rtimes \dot{\gamma}} + \underline{e \rtimes \gamma} \underline{\mathbb{C} \rtimes \dot{\gamma}}$$

$$\Delta \dot{P} = \sum_{\dot{a}} \dot{P}_{\dot{a}} \times \dot{P}^{\dot{a}} \Rightarrow \Delta (P\dot{P}) = (\Delta P) (\Delta \dot{P}) = \sum_a \sum_{\dot{a}} P_a \dot{P}_{\dot{a}} \times P^a \dot{P}^{\dot{a}}$$

$$\underline{P\dot{P}} \times \underline{\gamma\dot{\gamma}} = P \times \overline{\dot{P} \times \dot{\gamma}} = P \times \sum_{\dot{a}} \underbrace{\dot{P}_{\dot{a}} \times \gamma}_{\dot{P}^{\dot{a}} \times \dot{\gamma}} = \sum_{a:\dot{a}} \overbrace{P_a \dot{P}_{\dot{a}} \times \gamma}^{P^a \dot{P}^{\dot{a}} \times \dot{\gamma}}$$

$$\Delta P || \underline{\gamma\dot{\gamma}} = P | \dot{\gamma}$$

$$\underline{P\dot{P}} | \gamma = \underline{P \times \dot{P}} || \Delta \gamma$$



$$\underline{P \times \dot{P}} || \underline{\gamma \dot{\gamma}} := P | \gamma \dot{P} | \dot{\gamma}$$

$$P | (\gamma \dot{\gamma}) = {}^e (P \times (\gamma \dot{\gamma})) = \sum_i {}^e (P_i \times \gamma) {}^e (P^i \times \dot{\gamma}) = \sum_i (P_i | \gamma) (P^i | \dot{\gamma}) = (\Delta P) || (\gamma \dot{\gamma})$$