

$$n+1 \xrightarrow{\text{monometric}} \mathbb{R}^n$$

$${}_0\mathbb{L} \cdots {}_n\mathbb{L} \in \mathbb{R}^n$$

$$\overline{{}_i\mathbb{L} - {}_j\mathbb{L}} = 1$$

$$\overline{{}_i^2\mathbb{L}} = \frac{n}{2(n+1)}$$

$$\Rightarrow \left(\mathbb{L}^i : \frac{-1}{\sqrt{2(n+1)(n+2)}} \right) \in \mathbb{R}^{1+n} \ni \left(0 : \sqrt{\frac{n+1}{2(n+2)}} \right)$$

$$L_{n+1}^2 = \overline{\left(\frac{2L_n^2 - 1}{2\sqrt{1 - L_n^2}} : \mathbb{L}^i \right)} = \frac{\overline{2L_n^2 - 1}}{4\sqrt{1 - L_n^2}} + \overline{{}_i^2\mathbb{L}} = \frac{\overline{2L_n^2 - 1}}{4\sqrt{1 - L_n^2}} + L_n^2 = \frac{1}{4\sqrt{1 - L_n^2}} = \overline{\left(\frac{1}{2\sqrt{1 - L_n^2}} : 0 \right)}$$

$$\frac{1}{4\sqrt{1 - L_n^2}} < \frac{1}{2}$$

$$\overline{\left(\frac{2L_n^2 - 1}{2\sqrt{1 - L_n^2}} : \mathbb{L}^i \right) - \left(\frac{2L_n^2 - 1}{2\sqrt{1 - L_n^2}} : \mathbb{L}^j \right)} = \overline{{}_i\mathbb{L} - {}_j\mathbb{L}} = 1$$

$$\overline{\left(\frac{2L_n^2 - 1}{2\sqrt{1 - L_n^2}} : \mathbb{L}^i \right) - \left(\frac{1}{2\sqrt{1 - L_n^2}} : 0 \right)} = \frac{\overline{2L_n^2 - 1}}{2\sqrt{1 - L_n^2}} - \frac{1}{2\sqrt{1 - L_n^2}} + \overline{{}_i^2\mathbb{L}} = \frac{\overline{2L_n^2 - 1}}{2\sqrt{1 - L_n^2}} - \frac{1}{2\sqrt{1 - L_n^2}} + L_n^2 = 1$$