

$$\mathbb{H}_{\triangle_0} \mathbb{H}_{\triangle} \mathbb{K} \ni \eta = dx^j \eta \text{ int} \Leftrightarrow \begin{cases} \forall \gamma \in \mathbb{H}_{\triangle_0} \mathbb{K} \\ \eta = d\gamma \end{cases}$$

$$\Leftarrow : 0:I:1 \xrightarrow[\text{stet}]{\gamma:\eta} o:\mathbb{H}:x \Rightarrow \partial(\eta \ominus \gamma) = \partial\eta \ominus \partial\gamma = (x - o) - (x - o) = 0 \Rightarrow \int^{\eta} \eta - \int^{\gamma} \eta = \int^{\eta \ominus \gamma} \eta = 0$$

$$\Rightarrow : \quad x\eta = \int^{o|x} \eta \text{ well-def}$$

$$\eta \in \mathbb{H}_{\triangle_0} \mathbb{K} : \partial_i \eta = \eta_i$$

$$\bigwedge_{c \in C \subseteq \mathbb{H}} \bigvee_{\text{rund}} c \in C \Rightarrow \bigwedge_x \int^c o|x \ominus o|c = c|x \Rightarrow$$

$$\overline{x\eta - c\eta - [x^1 - c^1 \quad \dots \quad x^n - c^n] \begin{bmatrix} c\eta \\ 1 \\ + \\ c\eta \\ n \end{bmatrix}} = \overline{x\eta - c\eta - (x^j - c^j) \eta_j^c} = \overline{\int^{o|x} \eta - \int^{o|c} \eta - \int_j^{c|x} \eta dx^j}$$

$$= \overline{\int^{c|x} \eta - \int^{c|x} dx^j \eta} = \overline{\int^{c|x} dx^j \eta - \int^{c|x} dx^j \eta} = \overline{\int^{c|x} dx^j (\eta_j - \eta_j^c)} \leq \overline{x - c} \sum_j \overline{\eta_j - \eta_j^c} \rightsquigarrow 0$$

$$d\eta = \eta \text{ stet} \Rightarrow \eta \in \mathbb{H}_{\triangle_0} \mathbb{K}$$

$$\mathfrak{q} \in \begin{array}{c} \mathfrak{h} \\ \blacktriangleright \\ \mathfrak{h}^* \end{array} \text{ loc int}$$

$$\mathfrak{l} \in \begin{array}{c} H \\ \blacktriangleright \\ \mathfrak{h} \end{array}$$

$$\left\{ \begin{array}{l} H = \bigcup_k^K H^k \quad \bigwedge_k^K H^k \mathfrak{l} \subset \mathfrak{h}^k \subset \mathfrak{h} \\ \mathfrak{q} \stackrel{=}{=} d\gamma_k \quad \forall \gamma_k \in \mathfrak{h}^k \xrightarrow{\Gamma \neq 0} \mathbb{K} \end{array} \right. \Rightarrow \int \mathfrak{q} = \sum_k^K \mathfrak{l} \gamma_k | \partial H^k \text{ well-def}$$

$$\left\{ \begin{array}{l} H^k \mathfrak{h}^k : \gamma_k \\ k \in K \end{array} \right\} \Rightarrow \bigwedge_{k \in K} d(\gamma_k - \acute{\gamma}_k) = \mathfrak{q} - \mathfrak{q} \stackrel{=}{=} 0$$

$$\Rightarrow \mathfrak{h}^k \cap \acute{\mathfrak{h}}^k (\gamma_k - \acute{\gamma}_k) = c_{k:\acute{k}} \text{ cst} \Rightarrow \mathfrak{l} (\gamma_k - \acute{\gamma}_k) | \partial (H^k \cap \acute{H}^k) = 0$$

$$\Rightarrow \sum_k^K \mathfrak{l} \gamma_k | \partial H^k = \sum_k^K \sum_{\acute{k}}^{\acute{K}} \mathfrak{l} \gamma_k | \partial (H^k \cap \acute{H}^k) = \sum_k^K \sum_{\acute{k}}^{\acute{K}} \mathfrak{l} \acute{\gamma}_k | \partial (H^k \cap \acute{H}^k) = \sum_{\acute{k}}^{\acute{K}} \acute{\gamma}_k | \partial \acute{H}^k$$

$$\begin{aligned}
\mathfrak{A} &\in \mathfrak{H} \triangleleft_0 \mathfrak{H}^* \text{ loc int} \\
\mathbb{S} &\triangleleft_0 \mathfrak{H} \ni \mathfrak{L} \\
\mathfrak{L} &\in \begin{matrix} 0:H:1 \\ \triangleleft_0 \end{matrix} a:\mathfrak{H}:b \\
\mathfrak{L} &\underset{\text{htp}}{\sim} \mathfrak{L} \Rightarrow \int^{\mathfrak{L}} \mathfrak{A} = \int^{\mathfrak{L}} \mathfrak{A}
\end{aligned}$$

$$H \times H \ni (s:t) \xrightarrow[\text{stet}]{\Gamma} {}^t\Gamma \in \mathfrak{H}$$

$$\mathfrak{L} \neq \mathfrak{L} \Rightarrow \Gamma \text{ u-stet} \Rightarrow \bigvee_{\text{part}} \bigcup_{1 \leq i \leq m} s_{i-1} | s_i = H = \bigcup_{1 \leq j \leq n} t_{j-1} | t_j$$

$$\bigwedge_{i:j} \begin{matrix} t_{j-1} | t_j \Gamma \\ s_{i-1} | s_i \end{matrix} \subset \begin{matrix} \mathfrak{H} \\ j \text{ rund} \end{matrix} \subset \mathfrak{H} \left\{ \begin{array}{l} \gamma_j^i \in {}^j\mathfrak{H}^i \triangleleft_{1+0} \mathbb{K} \\ d\gamma_j^i = {}^j\mathfrak{H}^i \mathfrak{A} \end{array} \right.$$

$$\Rightarrow \bigwedge_{j < n} \gamma_j^i - \gamma_{j+1}^i \underset{{}^j\mathfrak{H}^i \cap {}_{j+1}\mathfrak{H}^i}{=} \underset{{}^j\mathfrak{H}^i \text{ 0-prim}}{=} c_j^i$$

$$\mathfrak{L} \text{ closed} \Rightarrow \gamma_n^i - \gamma_1^i \underset{{}^n\mathfrak{H}^i \cap {}_1\mathfrak{H}^i}{=} \underset{{}_1\mathfrak{H}^i \text{ prim}}{=} c_n^i$$

$$\bigwedge_i \int^{s_{i-1} \mathfrak{L}} \mathfrak{A} - \int^{s_i \mathfrak{L}} \mathfrak{A} = \sum_{1 \leq j \leq n} \left(\underset{s_{i-1} \mathfrak{L}}{\gamma_j^i} - \underset{s_i \mathfrak{L}}{\gamma_j^i} \right) | \partial t_{j-1} | t_j = \sum_{1 \leq j \leq n} \left(\underset{s_{i-1} \mathfrak{L}}{t_j \mathfrak{L} \gamma_j^i} - \underset{s_i \mathfrak{L}}{t_j \mathfrak{L} \gamma_j^i} - \underset{s_{i-1} \mathfrak{L}}{t_{j-1} \mathfrak{L} \gamma_j^i} + \underset{s_i \mathfrak{L}}{t_{j-1} \mathfrak{L} \gamma_j^i} \right)$$

$$= \sum_{1 \leq j < n} \overbrace{\left(\underset{s_{i-1} \mathfrak{L}}{t_j \mathfrak{L} \gamma_j^i} - \gamma_{j+1}^i - \underset{s_i \mathfrak{L}}{t_j \mathfrak{L} \gamma_j^i} + \gamma_{j+1}^i \right)} + \left\{ \begin{array}{l} \overbrace{\left(\underset{s_{i-1} \mathfrak{L}}{t_n \mathfrak{L} \gamma_n^i} - \underset{s_{i-1} \mathfrak{L}}{0 \mathfrak{L} \gamma_1^i} \right)} - \overbrace{\left(\underset{s_i \mathfrak{L}}{t_n \mathfrak{L} \gamma_n^i} - \underset{s_i \mathfrak{L}}{0 \mathfrak{L} \gamma_1^i} \right)} = c_n^i - c_n^i = 0 \\ \overbrace{\left(\underset{s_{i-1} \mathfrak{L}}{t_n \mathfrak{L} \gamma_n^i} - \underset{s_{i-1} \mathfrak{L}}{0 \mathfrak{L} \gamma_1^i} \right)} - \overbrace{\left(\underset{s_i \mathfrak{L}}{t_n \mathfrak{L} \gamma_n^i} - \underset{s_i \mathfrak{L}}{0 \mathfrak{L} \gamma_1^i} \right)} = 0 - 0 = 0 \end{array} \right. \begin{array}{l} {}^0\mathfrak{L} = {}^1\mathfrak{L} \\ {}^0\mathfrak{L} = a: {}^1\mathfrak{L} = b \end{array}$$