

$\bigcap_0 \mathbb{K} \ni \mathbb{1}$ voll treu

$$\mathbb{1} \supset \mathfrak{A} \text{ pre-comp} \Leftrightarrow \bigwedge_U \bigvee_{\mathfrak{A}_1 \dots \mathfrak{A}_n} \bigcup_i \mathfrak{A}_i \subset \underbrace{\mathfrak{A}_i + U}$$

$$\Rightarrow : \bigwedge_{\gamma} \bigvee_{\mathfrak{A}} \gamma - \mathfrak{A} \in U \Rightarrow \gamma \in \mathfrak{A} + U \Rightarrow \overline{\mathfrak{A}'} \subset \bigcup_{\mathfrak{A}} \underbrace{\mathfrak{A} + U} \xrightarrow{\overline{\mathfrak{A}'} \text{ cpt}} \bigvee_{\mathfrak{A}_1 \dots \mathfrak{A}_n} \subset \bigcup_i \mathfrak{A}_i + U \supset \overline{\mathfrak{A}'} \supset \mathfrak{A}$$

$$\Leftarrow : \mathcal{P}(\overline{\mathfrak{A}'}) \supset \mathcal{M} \text{ UltFil}$$

$$\mathcal{M} \underset{\text{CauFil}}{\sim}$$

$$\begin{aligned} \bigwedge_U^U \bigvee_V V - V \subset U &\Rightarrow \bigvee_W^U \mathbb{1} \supset W \subset V \xrightarrow{\text{Vor}} \bigvee_{\varphi_1 \dots \varphi_n}^{\varphi} \varphi \subset \bigcup_i \overline{\varphi_i + W} \\ &\Rightarrow \overline{\varphi} \subset \overline{\bigcup_i \varphi_i + W} = \bigcup_i \overline{\varphi_i + W} = \bigcup_i \overline{\varphi_i + \overline{W}} = \bigcup_i \overline{\varphi_i + W} \end{aligned}$$

$$\bigvee_j^{\mathcal{M}} \bigwedge_M \overline{\varphi_j + W} \cap M \neq \emptyset$$

$$\nexists \bigwedge_i^{\mathcal{M}} \bigvee_{M_i} \overline{\varphi_i + W} \cap M_i = \emptyset$$

$$\Rightarrow M_i \subset \overline{\varphi} \perp \overline{\varphi_i + W} \Rightarrow \bigcap_i M_i \subset \bigcap_i \overline{\varphi} \perp \overline{\varphi_i + W} = \overline{\varphi} \perp \overline{\bigcup_i \varphi_i + W} = \emptyset \Rightarrow \mathcal{M} \ni \bigcap_i M_i = \emptyset \nexists$$

$$\mathcal{B} = \frac{\overline{\varphi_j + W} \cap M}{M \in \mathcal{M}} \text{ FilBasis}$$

$$\bigwedge_M^{\mathcal{M}} \overline{\varphi_j + W} \cap M \neq \emptyset$$

$$\overline{\varphi_j + W} \cap M \cap \overline{\varphi_j + W} \cap M' \supset \overline{\varphi_j + W} \cap \frac{M \cap M'}{\in \mathcal{M}}$$

$$\langle \mathcal{B} \rangle = \mathcal{M}$$

$$M \in \mathcal{M} \Rightarrow M \supset M \cap \overline{\varphi_j + W} \in \mathcal{B} \Rightarrow M \in \langle \mathcal{B} \rangle \Rightarrow M \subset \langle \mathcal{B} \rangle \xrightarrow{\text{ultra}} \mathcal{M} = \langle U \rangle$$

$$\overline{\varphi} \in \mathcal{M} \Rightarrow \overline{\varphi} \cap \overline{\varphi_j + W} \in \mathcal{B} \subset \mathcal{M} \Rightarrow \overline{\varphi} \cap \overline{\varphi_j + W} \in \mathcal{M}$$

$$\bigwedge_i \overline{\varphi} \cap \overline{\varphi_j + W} \cap W \bigvee_i \mathbb{1} = \varphi_j + \mathbb{1} \Rightarrow \mathbb{1} - \mathbb{1} = \overline{\varphi_j + \mathbb{1}} - \overline{\varphi_j + \mathbb{1}} = \mathbb{1} - \mathbb{1} \in W - W \subset V - V \subset U \Rightarrow M - M \subset U$$

$$\Rightarrow \mathcal{M} \underset{\sim}{\sim} \mathbb{1} \in \mathbb{1} \text{ voll} \Rightarrow \mathbb{1} \in \overline{\varphi} \subset \mathbb{1} \Rightarrow \overline{\varphi} \text{ cpt}$$