

$${}^{o\leq r}\mathfrak{h} = \frac{\mathfrak{h} \in \mathfrak{H}}{\mathfrak{h}|o \leq r}$$

$${}^{o\leq r}\mathfrak{h} = \frac{\mathfrak{h} \in \mathfrak{H}}{\mathfrak{h}|o < r}$$

$$\mathfrak{h}_{\leq R}^o \subset \mathfrak{H}$$

$$\mathfrak{h}_{\leq R}^o \Rightarrow \mathfrak{h}|o < R \Rightarrow R - \mathfrak{h}|o > 0$$

$$\mathfrak{h}_{\leq R - \mathfrak{h}|o}^h \subset \mathfrak{h}_{\leq R}^o$$

$$\mathfrak{h} \in \mathfrak{h}_{\leq R - \mathfrak{h}|o}^h \Rightarrow \mathfrak{h}|h < R - \mathfrak{h}|o \xrightarrow{\text{trans}} \mathfrak{h}|o \leq \underbrace{\mathfrak{h}|h}_{< R - \mathfrak{h}|o} + \mathfrak{h}|o < R$$