

$$\mathfrak{h} \triangleleft 2 \leftarrow \mathfrak{h} \triangleleft \mathfrak{h} \times \mathfrak{h} \triangleleft 2$$

$$\mathfrak{h} \xrightarrow{\mathfrak{r}} \mathfrak{h}$$

$$\text{Urbild } \bar{\mathfrak{r}}_{\mathcal{U}}^{-1} = \frac{\mathfrak{h} \in \mathfrak{h}}{\mathfrak{h} \mathfrak{r} \in \mathcal{U}} = \underbrace{\mathfrak{h} \mathfrak{r} \in \mathcal{U}}_{\mathfrak{h} \in \mathfrak{h}}$$

$$\mathcal{U} \subset \mathcal{V} \Rightarrow \bar{\mathfrak{r}}_{\mathcal{U}}^{-1} \subset \bar{\mathfrak{r}}_{\mathcal{V}}^{-1}$$

$$\bar{\mathfrak{r}}_{\mathcal{U} \cup \mathcal{V}}^{-1} = \bar{\mathfrak{r}}_{\mathcal{U}}^{-1} \cup \bar{\mathfrak{r}}_{\mathcal{V}}^{-1}$$

$$\subset: \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{U} \cup \mathcal{V}}^{-1} \Rightarrow \mathfrak{h} \mathfrak{r} \in \mathcal{U} \cup \mathcal{V} \Rightarrow \vee \begin{cases} \mathfrak{h} \mathfrak{r} \in \mathcal{U} \Rightarrow \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{U}}^{-1} \\ \mathfrak{h} \mathfrak{r} \in \mathcal{V} \Rightarrow \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{V}}^{-1} \end{cases} \Rightarrow \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{U}}^{-1} \cup \bar{\mathfrak{r}}_{\mathcal{V}}^{-1}$$

$$\supset: \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{U}}^{-1} \cup \bar{\mathfrak{r}}_{\mathcal{V}}^{-1} \Rightarrow \vee \begin{cases} \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{U}}^{-1} \Rightarrow \mathfrak{h} \mathfrak{r} \in \mathcal{U} \\ \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{V}}^{-1} \Rightarrow \mathfrak{h} \mathfrak{r} \in \mathcal{V} \end{cases} \Rightarrow \mathfrak{h} \mathfrak{r} \in \mathcal{U} \cup \mathcal{V} \Rightarrow \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{U} \cup \mathcal{V}}^{-1}$$

$$\bar{\mathfrak{r}}_{\mathcal{U} \cap \mathcal{V}}^{-1} = \bar{\mathfrak{r}}_{\mathcal{U}}^{-1} \cap \bar{\mathfrak{r}}_{\mathcal{V}}^{-1}$$

$$\subset: \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{U} \cap \mathcal{V}}^{-1} \Rightarrow \mathfrak{h} \mathfrak{r} \in \mathcal{U} \cap \mathcal{V} \Rightarrow \wedge \begin{cases} \mathfrak{h} \mathfrak{r} \in \mathcal{U} \Rightarrow \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{U}}^{-1} \\ \mathfrak{h} \mathfrak{r} \in \mathcal{V} \Rightarrow \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{V}}^{-1} \end{cases} \Rightarrow \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{U}}^{-1} \cap \bar{\mathfrak{r}}_{\mathcal{V}}^{-1}$$

$$\supset: \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{U}}^{-1} \cap \bar{\mathfrak{r}}_{\mathcal{V}}^{-1} \Rightarrow \wedge \begin{cases} \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{U}}^{-1} \Rightarrow \mathfrak{h} \mathfrak{r} \in \mathcal{U} \\ \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{V}}^{-1} \Rightarrow \mathfrak{h} \mathfrak{r} \in \mathcal{V} \end{cases} \Rightarrow \mathfrak{h} \mathfrak{r} \in \mathcal{U} \cap \mathcal{V} \Rightarrow \mathfrak{h} \in \bar{\mathfrak{r}}_{\mathcal{U} \cap \mathcal{V}}^{-1}$$

$$\text{Bild } {}^U \mathfrak{r} = \frac{\mathfrak{h} \mathfrak{r}}{\mathfrak{h} \in U} = \underbrace{\bigvee_{\mathfrak{h} \in \mathfrak{h}} \mathfrak{h}}_{\mathfrak{h}} = \mathfrak{h} \subset \mathfrak{h}$$

$$\text{Gesamt-Bild } {}^{\bar{h}}\mathcal{L} = \frac{{}^h\mathcal{L}}{h \in \bar{h}} = \frac{h' \in \bar{h}}{\bigvee_h h' = {}^h\mathcal{L}} \subset \bar{h}$$

$${}^{U \cup V}\mathcal{L} = {}^U\mathcal{L} \cup {}^V\mathcal{L}$$

$$\subset: h' \in {}^{U \cup V}\mathcal{L} \Rightarrow \bigvee_h {}^h\mathcal{L} = h' \Rightarrow \vee \begin{cases} h \in U & \Rightarrow h' \in {}^U\mathcal{L} \\ h \in V & \Rightarrow h' \in {}^V\mathcal{L} \end{cases} \Rightarrow h' \in {}^U\mathcal{L} \cup {}^V\mathcal{L}$$

$$\supset: h' \in {}^U\mathcal{L} \cup {}^V\mathcal{L} \Rightarrow \vee \begin{cases} h' \in {}^U\mathcal{L} & \Rightarrow \bigvee_U {}^{h_U}\mathcal{L} = h' \\ h' \in {}^V\mathcal{L} & \Rightarrow \bigvee_V {}^{h_V}\mathcal{L} = h' \end{cases} \Rightarrow \bigwedge_h {}^h\mathcal{L} = h' \Rightarrow h' \in {}^{U \cup V}\mathcal{L}$$

$${}^{U \cap V}\mathcal{L} \subset {}^U\mathcal{L} \cap {}^V\mathcal{L}$$

$$\subset: h' \in {}^{U \cap V}\mathcal{L} \Rightarrow \bigvee_h {}^h\mathcal{L} = h' \Rightarrow \wedge \begin{cases} h \in U & \Rightarrow h' \in {}^U\mathcal{L} \\ h \in V & \Rightarrow h' \in {}^V\mathcal{L} \end{cases} \Rightarrow h' \in {}^U\mathcal{L} \cap {}^V\mathcal{L}$$

$${}^h\mathcal{L} = b \text{ cst } : U \cap V = \emptyset \text{ disjunkt } : U \neq \emptyset \neq V \Rightarrow \emptyset = {}^{U \cap V}\mathcal{L} \subsetneq {}^U\mathcal{L} \cap {}^V\mathcal{L} = \underbrace{b}_{\neq \emptyset} \neq \emptyset$$

$$\bar{\tau}_U^{-1}\mathcal{L} = \bar{U} \cap \bar{h}\mathcal{L}$$

$$\subset: h' \in \bar{\tau}_U^{-1}\mathcal{L} \Rightarrow \bigvee_{h \in \bar{\tau}_U^{-1}} h' = {}^h\mathcal{L} \in \bar{U} \cap \bar{h}\mathcal{L}$$

$$\supset: h' \in \bar{U} \cap \bar{h}\mathcal{L} \Rightarrow \bigvee_{h \in \bar{h}} h' = {}^h\mathcal{L} \Rightarrow h \in \bar{\tau}_U^{-1} \Rightarrow h' \in \bar{\tau}_U^{-1}\mathcal{L}$$

$$\mathcal{U} \mid^U \mathcal{V} \supset U$$

$$h \in U \Rightarrow h \in \mathcal{U} \mid^U \mathcal{V} \Rightarrow h \in \mathcal{U}$$