

$$\mathbb{H}_{\omega}^2 \mathbb{C} \xleftarrow[\mathcal{P}]{\mathcal{C}} \mathbb{H}_{\omega}^2 \mathbb{C}$$

$$\mathbb{H}_{\omega}^2 \mathbb{C} \ni 1_n \text{ ONB} \Rightarrow \sum_n 1_n 1_n^* \gamma = \gamma$$

$${}^z \mathcal{P}_w \simeq \sum_n {}^z 1_n {}^w 1_n^* \text{ cpt conv } \mathbb{H} \times \mathbb{H}$$

$$\bigwedge \gamma \in \mathbb{H}_{\omega}^2 \mathbb{C} \curvearrowright {}^z \gamma = \int_{dw/\pi}^{\mathbb{H}} {}^z \mathcal{P}_w {}^w \gamma$$

$$\int_{dw/\pi}^{\mathbb{H}} {}^z \mathcal{P}_w {}^w \gamma = \int_{dw/\pi}^{\mathbb{H}} \sum_n {}^z 1_n {}^w 1_n^* {}^w \gamma = \sum_n {}^z 1_n \int_{dw/\pi}^{\mathbb{H}} {}^w 1_n^* {}^w \gamma = \sum_n {}^z 1_n 1_n^* \gamma = \overbrace{\sum_n 1_n 1_n^* \gamma}^z = {}^z \gamma$$