

$$\mathbf{e}_u \star^b \mathbf{e}_v = \int_{dz/\pi^d}^{\mathbb{C}^d} u \mathbf{e}_z^z \mathbf{e}_z^{-b} z \mathbf{e}_v = \int_{dz/\pi^d}^{\mathbb{C}^d} z \mathbf{e}_z^{-b} \bar{v} |u \mathbf{e} \Big|_{\bar{z}|z} = \sqrt[b]{-1} u \mathbf{e}_v^{b-1}$$

$$\mathbf{e}_u \star_{\nu}^b \mathbf{e}_v = \int_{dz/\pi^d}^{\mathbb{C}^d} u_{\nu} \mathbf{e}_z^z \mathbf{e}_z^{-b} z_{\nu} \mathbf{e}_v = \int_{dz/\pi^d}^{\mathbb{C}^d} z_{\nu} \mathbf{e}_z^{-b} \bar{v} |u_{\nu} \mathbf{e} \Big|_{\bar{z}|z} = \sqrt[b]{-1} u_{\nu} \mathbf{e}_v^{b-1}$$

$$\text{LHS} = \int_{dz}^{\mathbb{C}^d} \exp z \Big| \bar{z} \frac{0}{-b/2} \Big| \frac{-b/2}{0} \frac{\frac{t}{z}}{\frac{t}{z}} \exp 2 \frac{u}{2} \Big| \frac{v}{2} \frac{\frac{t}{z}}{\frac{t}{z}} = \left(\frac{\pi}{2}\right)^d \sqrt[b]{-1} \exp \frac{u}{2} \Big| \frac{v}{2} \frac{0}{2b^{-1}} \Big| \frac{2b^{-1}}{0} \frac{\frac{t}{2}}{\frac{t}{2}} = \text{RHS}$$

$$\Re M > 0 \Rightarrow \int_{dz/\pi^d}^{d\mathbb{C}} z \mathbf{e}_z^{-\nu M} x \mathbf{e}_z^{\nu} z \mathbf{e}_y^{\nu} = (\nu M)^{-d} x \mathbf{e}_y^{\nu/M}$$

$$\frac{\nu M/2}{0} \Big| \frac{0}{\nu M/2} \Big|^{-1} = \frac{2/\nu M}{0} \Big| \frac{0}{2/\nu M} \Big|$$

$$\int_{dz}^{\mathbb{C}^d} z \mathbf{e}_z^{-\nu M} w \mathbf{e}_z^{\nu} z \mathbf{e}_{\zeta}^{\nu} = \left(\frac{\pi}{\nu M}\right)^d w \mathbf{e}_{\zeta}^{\nu/M}$$

$$\text{LHS} = \int_{dz}^{\mathbb{C}^d} z \mathbf{e}_z^{-\nu M/2} \bar{z} \mathbf{e}_{\bar{z}}^{-\nu M/2} \nu w \mathbf{e}_z^z \mathbf{e}_{\nu \zeta} = \left(\frac{\pi}{2}\right)^d \overbrace{\frac{\nu M/2}{0} \Big| \frac{0}{\nu M/2} \Big|}^{-1/2} \nu w \mathbf{e}_{\nu \zeta}^{1/2\nu M} \bar{\zeta} \mathbf{e}_{\bar{w}}^{1/2\nu M}$$

$$= \left(\frac{\pi}{2}\right)^d \left(\frac{2}{\nu M}\right)^d w \mathbf{e}_{\zeta}^{\nu/2M} \bar{\zeta} \mathbf{e}_{\bar{w}}^{\nu/2M} = \text{RHS}$$