



$$T_z \mathbb{Z}^d = \frac{\pi^{d/2}}{T_D^{1/2}} \mathcal{E}^{4\pi^2 z \bar{T} \star z} \bar{T} \frac{2\pi i \mathbb{Z}}{2z \bar{T}}_d$$

$$\begin{aligned} \text{LHS} &= \sum_{\mathfrak{r}} \mathcal{E}^{-\mathfrak{r} \star \bar{\Gamma}^* + \mathfrak{r} \star 2\pi i} = \sum_{\mathfrak{r}} \int_{\mathbb{R}^d} \mathcal{E}^{-\mathfrak{r} \star \mathfrak{r}} \mathcal{E}^{-\mathfrak{r} \star \bar{\Gamma}^* + \mathfrak{r} \star 2\pi i} = \sum_{\mathfrak{r}} \int_{\mathbb{R}^d} \mathcal{E}^{-\mathfrak{r} \star \bar{\Gamma}^*} \mathcal{E}^{\mathfrak{r} \star 2\pi i} \\ &= \frac{\pi^{d/2}}{T_D^{1/2}} \sum_{\mathfrak{r}} \mathcal{E}^{(\bar{\Gamma}^* + \mathfrak{r} \star 2\pi i) (\bar{\Gamma}^* + \mathfrak{r} \star 2\pi i)} \bar{\Gamma} \\ &= \sum_n \mathcal{E}^{-n T \star n + 2\pi i z \star n} = \sum_{\nu} \int_{\mathbb{R}^d} \mathcal{E}^{-y \star \nu} \mathcal{E}^{-y T \star y + 2\pi i z \star y} \\ &= \sum_{\nu} \int_{\mathbb{R}^d} \mathcal{E}^{-y T \star y} \mathcal{E}^{-y \star (\nu + 2\pi i z)} = \frac{\pi^{d/2}}{T_D^{1/2}} \sum_{\nu} \mathcal{E}^{-(\nu + 2\pi i z) \bar{T} \star (\nu + 2\pi i z)} \\ &= \frac{\pi^{d/2}}{T_D^{1/2}} \mathcal{E}^{4\pi^2 z \bar{T} \star z} \sum_{\nu} \mathcal{E}^{-\nu \bar{T} \star \nu - 4\pi i z \bar{T} \star \nu} = \text{RHS} \end{aligned}$$

$$\bar{\Gamma}^{\star -1} \Theta = \bar{\Gamma}^{1/2} \mathcal{E}^{\pi i \bar{\Gamma}^{\star -1} T} \bar{\Gamma} \Theta$$

$$\left[ \bar{\Gamma} + \bar{\Gamma}^* \right] \left[ \bar{\Gamma} + \bar{\Gamma}^* \right] \bar{\Gamma}$$