

$$N \stackrel{\text{complex}}{\cong} \mathbb{C}^n \times \mathbb{R} \ni z:n$$

$$z:n, \dot{z}:\dot{n} = \underbrace{z + \dot{z}:n + \dot{n} + \frac{\dot{z} \times z - z \times \dot{z}}{4i}}_{}$$

$$\overline{(w:n)^\nu \uparrow}^z = {}^{z+w} \uparrow^z \mathcal{E}_w^{-\nu} n^\nu \mathcal{E}_w^{-\nu/2} n^\nu$$

$$\overline{\mathfrak{t}_w^\nu \uparrow}^z = {}^{z+w} \uparrow^z \mathcal{E}_w^{-\nu} w \mathcal{E}_w^{\nu/2}$$

$$\overline{(w:n)^\nu \uparrow}^z \times \overline{(w:n)^\nu \uparrow}^z = \uparrow \times \uparrow \text{ unitary}$$

$$\begin{aligned} \overline{\mathfrak{t}_w^\nu \uparrow}^z \times \overline{\mathfrak{t}_w^\nu \uparrow}^z &= \int_{\mathbb{C}^d} \frac{d\bar{z}dz}{(2\pi i)^d} {}^z e_z^{-\nu} \overline{\mathfrak{t}_w^\nu \uparrow}^{z*} \overline{\mathfrak{t}_w^\nu \uparrow}^z \\ &= \int_{\mathbb{C}^d} \frac{d\bar{z}dz}{(2\pi i)^d} {}^z \mathcal{E}_z^{-\nu} {}^{z+w} \uparrow^z {}^{z+w} \uparrow^z e_w^{-\nu} {}^z e_w^{-\nu} w e_z^{-\nu} \\ &= \int_{\mathbb{C}^d} \frac{d\bar{z}dz}{(2\pi i)^d} {}^{z+w} \uparrow^z {}^{z+w} \uparrow^z \mathcal{E}_{z+w}^{-\nu} = \uparrow \times \uparrow \end{aligned}$$