

$$\begin{aligned}\hat{S} \left({}^k\mathbb{C}_k \right) &= {}^k\mathbb{C}_k^{\mathbb{U}} \\ S_k \left({}^{k+m}\mathbb{C}_{k+n} \right) &= \frac{{}^{k+m}\mathbb{C}_{k+m}^{\mathbb{U}} \times {}^{k+n}\mathbb{C}_{k+n}^{\mathbb{U}}}{m\mathbb{C}_m^{\mathbb{U}} \times {}^k\mathbb{C}_k^{\mathbb{U}} \times {}^n\mathbb{C}_n^{\mathbb{U}}} \\ Gr_k \left(\mathbb{C}_{k+m} \right) \times Gr_k \left(\mathbb{C}_{k+n} \right) &= \frac{{}^{k+m}\mathbb{C}_{k+m}^{\mathbb{U}} \times {}^{k+n}\mathbb{C}_{k+n}^{\mathbb{U}}}{{}^k\mathbb{C}_k^{\mathbb{U}} \times {}^m\mathbb{C}_m^{\mathbb{U}} \times {}^n\mathbb{C}_n^{\mathbb{U}}} \\ \frac{1}{0} \left| \frac{0}{0} \right. &= \frac{a}{c} \left| \frac{b}{d} \right. \frac{1}{0} \left| \frac{0}{0} \right. \frac{\alpha}{\gamma} \left| \frac{\beta}{\delta} \right. = \frac{a}{c} \left| \frac{0}{0} \right. \frac{\alpha}{\gamma} \left| \frac{\beta}{\delta} \right. = \frac{a\alpha}{c\alpha} \left| \frac{a\beta}{c\beta} \right. \\ &\Rightarrow a\alpha = 1; \beta = 0 = c\end{aligned}$$

$$\begin{aligned}\frac{1}{0} \left| \frac{0}{0} \right. &= \frac{a^{-1}}{c} \left| \frac{b}{d} \right. \frac{1}{0} \left| \frac{0}{0} \right. \frac{\alpha^{-1}}{\gamma} \left| \frac{\beta}{\delta} \right. = \frac{\overset{*}{a}}{\overset{*}{b}} \left| \frac{\overset{*}{c}}{\overset{*}{d}} \right. \frac{1}{0} \left| \frac{0}{0} \right. \frac{\overset{*}{\alpha}}{\overset{*}{\beta}} \left| \frac{\overset{*}{\gamma}}{\overset{*}{\delta}} \right. = \frac{\overset{*}{a}}{\overset{*}{b}} \left| \frac{0}{0} \right. \frac{\overset{*}{\alpha}}{\overset{*}{\beta}} \left| \frac{\overset{*}{\gamma}}{\overset{*}{\delta}} \right. = \frac{\overset{*}{a}\overset{*}{\alpha}}{\overset{*}{b}\overset{*}{\alpha}} \left| \frac{\overset{*}{a}\overset{*}{\gamma}}{\overset{*}{b}\overset{*}{\gamma}} \right. \\ &\Rightarrow \overset{*}{a}\overset{*}{\alpha} = 1; \gamma = 0 = b \\ &\Rightarrow \frac{a}{c} \left| \frac{b}{d} \right. \frac{1}{0} \left| \frac{0}{0} \right. \frac{\alpha}{\gamma} \left| \frac{\beta}{\delta} \right. = \frac{a}{c} \left| \frac{b}{d} \right. \frac{1}{0} \left| \frac{0}{0} \right. \frac{\alpha}{\gamma} \left| \frac{\beta}{\delta} \right. \in {}^m\mathbb{C}_m^{\mathbb{U}} \times {}^k\mathbb{C}_k^{\mathbb{U}} \times {}^n\mathbb{C}_n^{\mathbb{U}}\end{aligned}$$

$$\begin{aligned}\hat{S} \left({}^k\mathbb{C}_k^{\mathfrak{D}} \right) &= \frac{{}^k\mathbb{C}_k^{\mathbb{U}}}{{}^k\mathbb{R}_k^{\mathbb{U}}} \\ S_k \left({}^{k+n}\mathbb{C}_{k+n}^{\mathfrak{D}} \right) &= \frac{{}^{k+n}\mathbb{C}_{k+n}^{\mathbb{U}}}{{}^k\mathbb{R}_k^{\mathbb{U}} \times {}^n\mathbb{C}_n^{\mathbb{U}}} \\ Gr_k \left(\mathbb{C}_{k+n} \right) &= \frac{{}^{k+n}\mathbb{C}_{k+n}^{\mathbb{U}}}{{}^k\mathbb{C}_k^{\mathbb{U}} \times {}^n\mathbb{C}_n^{\mathbb{U}}} \\ \frac{1}{0} \left| \frac{0}{0} \right. &= \frac{a}{c} \left| \frac{b}{d} \right. \frac{1}{0} \left| \frac{0}{0} \right. \frac{a^{\#}}{b^{\#}} \left| \frac{c^{\#}}{d^{\#}} \right. = \frac{a}{c} \left| \frac{0}{0} \right. \frac{a^{\#}}{b^{\#}} \left| \frac{c^{\#}}{d^{\#}} \right. = \frac{aa^{\#}}{ca^{\#}} \left| \frac{ac^{\#}}{cc^{\#}} \right. \\ &\Rightarrow aa^{\#} = 1; c = 0 \Rightarrow \bar{a} = a \Rightarrow \frac{a}{c} \left| \frac{b}{d} \right. = \frac{a}{c} \left| \frac{b}{d} \right. \in {}^k\mathbb{R}_k^{\mathbb{U}} \times {}^n\mathbb{C}_n^{\mathbb{U}}\end{aligned}$$

$$\begin{aligned}\frac{1}{0} \left| \frac{0}{0} \right. &= \frac{a^{-1}}{c} \left| \frac{b}{d} \right. \frac{1}{0} \left| \frac{0}{0} \right. \frac{a^{\#}}{b^{\#}} \left| \frac{c^{\#}}{d^{\#}} \right. = \frac{\overset{*}{a}}{\overset{*}{b}} \left| \frac{\overset{*}{c}}{\overset{*}{d}} \right. \frac{1}{0} \left| \frac{0}{0} \right. \frac{\bar{a}}{\bar{c}} \left| \frac{\bar{b}}{\bar{d}} \right. = \frac{\overset{*}{a}}{\overset{*}{b}} \left| \frac{0}{0} \right. \frac{\bar{a}}{\bar{c}} \left| \frac{\bar{b}}{\bar{d}} \right. = \frac{\overset{*}{a}\bar{a}}{\overset{*}{b}\bar{a}} \left| \frac{\overset{*}{a}\bar{b}}{\overset{*}{b}\bar{b}} \right. \\ &\Rightarrow \overset{*}{a}\bar{a} = 1; b = 0 \\ &\Rightarrow \frac{a}{c} \left| \frac{b}{d} \right. = \frac{a}{c} \left| \frac{b}{d} \right. \in {}^k\mathbb{R}_k^{\mathbb{U}} \times {}^n\mathbb{C}_n^{\mathbb{U}}\end{aligned}$$