

$$\begin{aligned} \underline{w} \alpha_w \beta_w^* &= \underline{\alpha - \bar{\alpha}} \underline{w} \overline{u^{-1} \beta^* + \beta^t + \dot{w} \beta^* - \beta^t} - \frac{1}{2} \overline{\alpha + \bar{\alpha} + \underline{\alpha - \bar{\alpha}} w} \overline{u^{-1} (\underline{w} + \dot{w})} \overline{u^{-1} \beta^* + \beta^t + \dot{w} \beta^* - \beta^t} \\ &\quad + \overline{\alpha + \bar{\alpha} + \underline{\alpha - \bar{\alpha}} w} \overline{u^{-1} \dot{w} \beta^* - \beta^t} \end{aligned}$$

$$-\underline{w} \alpha_w \beta_w^* / 2 = \bar{\alpha} \underline{w} \beta^* + \alpha \underline{\dot{w}} \beta^t$$

$$\begin{aligned} \underline{w} \alpha_w \beta_w^* / 2 &= \underline{\alpha - \bar{\alpha}} \underline{w} \beta^* - \alpha (\underline{w} + \dot{w}) \beta^* + \alpha \underline{\dot{w}} \beta^* - \beta^t \\ &= \alpha \underline{w} \beta^* - \bar{\alpha} \underline{w} \beta^* - \alpha \underline{w} \beta^* - \alpha \underline{\dot{w}} \beta^* + \alpha \underline{\dot{w}} \beta^* - \alpha \underline{\dot{w}} \beta^t = -\text{RHS} \end{aligned}$$

$$\underline{w} \zeta_w \sigma_w^* - \sigma_w \sigma_w^* / 2 - \zeta_w \zeta_w^* / 2 = \underline{\zeta - \bar{\sigma}} \underline{w} \underline{\zeta^* - \sigma^*} + \underline{\zeta - \sigma} \underline{\dot{w}} \underline{\zeta^t - \sigma^t}$$

$$\text{LHS} = \bar{\sigma} \underline{w} \sigma^* + \sigma \underline{\dot{w}} \sigma^t + \bar{\zeta} \underline{w} \zeta^* + \zeta \underline{\dot{w}} \zeta^t - 2\bar{\zeta} \underline{w} \sigma^* - 2\zeta \underline{\dot{w}} \sigma^t$$

$$\bar{\sigma} \underline{w} \zeta^* = \overbrace{\bar{\sigma} \underline{w} \zeta^*}^t = \bar{\zeta} \underline{\dot{w}} \sigma^* = \bar{\zeta} \underline{w} \sigma^*$$

$$\sigma \underline{\dot{w}} \zeta^t = \overbrace{\sigma \underline{\dot{w}} \zeta^t}^t = \zeta \underline{\dot{w}}^t \sigma^t = \zeta \underline{\dot{w}} \sigma^t$$

$$\zeta \overline{w_e E_\sigma} = \underline{w} \zeta_e E_\sigma = e^{\zeta \bar{\sigma} - \sigma \bar{\sigma} / 2 - \zeta \zeta^* / 2} \overline{\underline{\zeta - \sigma} \underline{\dot{w}} \underline{\zeta^t - \sigma^t} + \underline{\zeta - \bar{\sigma}} \underline{w} \underline{\zeta^* - \sigma^*}}$$

$$\text{LHS} = \zeta_e E_\sigma \overline{\underline{\zeta - \bar{\sigma}} \underline{w} \underline{\zeta^* - \sigma^*} + \underline{\zeta - \sigma} \underline{\dot{w}} \underline{\zeta^t - \sigma^t}} = \text{RHS}$$

$${}^\zeta \mathcal{K}_\sigma^* = {}^\sigma \bar{\mathcal{K}}_\zeta$$

$$\int \int_{d\zeta d\sigma} \overline{{}^\zeta \mathcal{K}_\sigma^* \sigma \varphi^\zeta \psi} = \int_{d\zeta} \overline{{}^\zeta \bar{\mathcal{K}}_\varphi \zeta \psi} = \overline{{}^* \mathcal{K} \varphi \bar{\mathbf{x}} \psi} = \overline{\varphi \bar{\mathbf{x}} \mathcal{K} \psi} = \int_{d\sigma} \overline{\sigma \bar{\varphi} \sigma \mathcal{K} \psi} = \int_{d\sigma} \overline{\sigma \bar{\varphi}} \int_{d\zeta} \overline{\sigma \mathcal{K}_\zeta \zeta \psi} = \int_{d\sigma} \int_{d\zeta} \overline{\sigma \bar{\mathcal{K}}_\zeta \sigma \varphi^\zeta \psi}$$

$$\overline{{}^* \underline{w}_e \underline{E}} = \underline{w}_e \underline{E}$$

$$\begin{aligned} \overline{{}^\zeta \underline{w}_e \underline{E}}_\sigma &= \overline{{}^\sigma \underline{E}_\zeta} = \overline{{}^\sigma \underline{E}_\zeta \overline{\sigma - \zeta \underline{w} \underline{\sigma} - \underline{\zeta}} + \overline{\sigma - \zeta \underline{w} \underline{\sigma} - \underline{\zeta}}} \\ &= \underline{{}^\zeta E}_\sigma \overline{\zeta - \sigma \underline{w} \underline{\zeta} - \underline{\sigma}} + \overline{\zeta - \sigma \underline{w} \underline{\zeta} - \underline{\sigma}} = \underline{w} \underline{{}^\zeta E}_\sigma \end{aligned}$$

$$\overline{\underline{w}_e \underline{E}} \underline{e^{-\zeta^*/2} \gamma} = \underline{e^{-\zeta^*/2} \zeta - \partial \underline{w} \underline{\zeta} - \underline{\partial} \gamma}$$

$$\begin{aligned} \underline{w} \underline{{}^\zeta E}_\sigma &= \underline{{}^\zeta E}_\sigma \overline{\overline{\sigma - \zeta \underline{w} \underline{\sigma} - \underline{\zeta}} + \overline{\sigma - \zeta \underline{w} \underline{\sigma} - \underline{\zeta}}} = \underline{e^{\zeta^* - \sigma \sigma^*/2 - \zeta^*/2}} \overline{\overline{\sigma - \zeta \underline{w} \underline{\sigma} - \underline{\zeta}} + \overline{\sigma - \zeta \underline{w} \underline{\sigma} - \underline{\zeta}}} \\ \underline{e^{\zeta^*/2} \zeta} \overline{\underline{w}_e \underline{E}} \underline{\gamma} &= \underline{e^{\zeta^*/2}} \int_{d\sigma} \underline{e^{\zeta^* - \sigma \sigma^*/2 - \zeta^*/2}} \overline{\overline{\sigma - \zeta \underline{w} \underline{\sigma} - \underline{\zeta}} + \overline{\sigma - \zeta \underline{w} \underline{\sigma} - \underline{\zeta}}} \underline{\sigma \gamma} \underline{e^{-\sigma \sigma^*/2}} \\ &= \int_{d\sigma} \underline{e^{\zeta^* - \sigma \sigma^*}} \overline{\overline{\sigma - \zeta \underline{w} \underline{\sigma} - \underline{\zeta}} + \overline{\sigma - \zeta \underline{w} \underline{\sigma} - \underline{\zeta}}} \underline{\sigma \gamma} = \underline{\zeta} \overline{\overline{\partial - \zeta \underline{w} \underline{\partial} - \underline{\zeta}} \gamma} + \underline{\zeta} \overline{\overline{\partial - \zeta \underline{w} \underline{\partial} - \underline{\zeta}} \gamma} \end{aligned}$$

$$\overline{\zeta - \partial \underline{w} \underline{\zeta} - \underline{\partial}} = \underline{\alpha \zeta^* - \partial_\alpha} \overline{\beta \zeta^* - \partial_\beta}$$

$$\begin{aligned} \text{LHS} &= \begin{bmatrix} \partial_1 - \zeta_1 & \partial_n - \zeta_n \end{bmatrix} \begin{bmatrix} 1a \\ na \end{bmatrix} \begin{bmatrix} b_1 & b_n \end{bmatrix} \begin{bmatrix} \partial_1 - \zeta_1 \\ \partial_n - \zeta_n \end{bmatrix} = \overline{\partial_i - \zeta_i} \underline{a} \underline{b_j} \underline{\partial_j - \zeta_j} \\ \overline{\partial_i - \zeta_i} \underline{a} &= \partial_i \underline{a} - \zeta_i \underline{a} = \partial_a - \zeta \underline{a}: \quad \underline{b_j} \underline{\partial_j - \zeta_j} = \underline{b_j} \underline{\partial_j} - \underline{b_j} \underline{\zeta_j} = \underline{\partial_b} - \zeta \underline{b} \end{aligned}$$