

$$\Gamma \mathcal{F}^\# = \begin{cases} \Gamma \mathcal{F}^t & \text{bilin} \\ \Gamma \mathcal{F}^* & \text{balin} \end{cases}$$

$$\varepsilon \text{ bilin } \varepsilon \mathcal{F} \mathcal{J} \mathcal{F}^t = \overbrace{\Gamma \mathcal{F}^t}^t = \mathcal{F} \mathcal{J} \mathcal{F}^t \Leftrightarrow \varepsilon \mathcal{J} = \mathcal{J}^t$$

$$\varepsilon \text{ alin } \varepsilon \mathcal{F} \mathcal{J} \mathcal{F}^* = \overbrace{\Gamma \mathcal{F}^*}^* = \mathcal{F} \mathcal{J} \mathcal{F}^* \Leftrightarrow \varepsilon \mathcal{J} = \mathcal{J}^*$$

involution

$$\tilde{\Gamma} \mathcal{J} = \begin{cases} \Gamma \mathcal{J} & \text{lin} \\ \bar{\Gamma} \mathcal{J} & \text{alin} \end{cases}$$

$$\Gamma \mathcal{J} \tilde{\mathcal{F}}^\# = \Gamma \mathcal{J} \mathcal{J} \tilde{\mathcal{F}}^\# \begin{cases} \Gamma \mathcal{J} \mathcal{F}^t & \text{lin-bilin} \\ \Gamma \mathcal{J} \mathcal{F}^* & \text{lin-balin} \\ \bar{\Gamma} \mathcal{J} \mathcal{F}^t & \text{alin-bilin} \\ \bar{\Gamma} \mathcal{J} \mathcal{F}^* & \text{alin-balin} \end{cases}$$

consistent

$$\tilde{\Gamma} \mathcal{J} \mathcal{J} \tilde{\mathcal{F}}^\# = \tilde{\Gamma} \mathcal{J} \mathcal{J} \tilde{\mathcal{F}}^\# = \mu \tilde{\Gamma} \mathcal{J} \tilde{\mathcal{F}}^\# = \mu \tilde{\Gamma} \mathcal{J} \tilde{\mathcal{F}}^\# \Leftrightarrow \mathcal{J} \mathcal{J} \mathcal{J} = \mu \mathcal{J} \begin{cases} \Gamma \mathcal{J} \mathcal{J} \mathcal{F}^\# = \underline{\Gamma} \mathcal{J} \mathcal{J} \mathcal{F}^\# = \mu \Gamma \mathcal{J} \mathcal{F}^\# & \Leftrightarrow \mathcal{J} \mathcal{J} \mathcal{J} = \mu \mathcal{J} \\ \bar{\Gamma} \mathcal{J} \mathcal{J} \mathcal{F}^\# = \underline{\bar{\Gamma}} \mathcal{J} \mathcal{J} \mathcal{F}^\# = \mu \bar{\Gamma} \mathcal{J} \mathcal{F}^\# = \mu \bar{\Gamma} \mathcal{J} \mathcal{F}^\# & \Leftrightarrow \mathcal{J} \mathcal{J} \mathcal{J} = \mu \bar{\mathcal{J}} \end{cases}$$

$$\begin{array}{c|cc} -1 & a & b \\ \hline & c & d \\ \hline a & b & \\ c & d & \end{array} \Big|_J -1 \quad \begin{array}{c|cc} -1 & a & b \\ \hline & c & d \\ \hline a & b & \\ c & d & \end{array} \Big|_B -1 = \begin{array}{cc|c} a & b & \\ \hline c & d & -1 \\ \hline -1 & & a & b \\ & & c & d \end{array} \Big|_D$$

$$\mathbb{R}_{p+q|p+q}$$

$$\begin{array}{c|cc} -1 & 1_p & 0 \\ \hline & 0 & -1_q \\ \hline 1_p & 0 & \\ 0 & -1_q & \end{array} \Big|_J -1 \quad \begin{array}{c|cc} -1 & 1_p & 0 \\ \hline & 0 & 1_q \\ \hline 1_p & 0 & \\ 0 & 1_q & \end{array} \Big|_B -1 = \begin{array}{cc|c} 1_p & 0 & \\ \hline 0 & -1_q & -1 \\ \hline -1 & & 1_p & 0 \\ & & 0 & -1_q \end{array} \Big|_D$$

$${}^{p+q} \mathbb{R}_{p+q}^{\mathbb{C}} \times {}^{p+q} \mathbb{R}_{p+q}^{\mathbb{C}} \quad {}^{p+q:p+q} \mathbb{R}_{p+q:p+q}^{\mathbb{U}} \quad {}^{2p:2q} \mathbb{R}_{2p:2q}^{\mathbb{U}}$$

$${}^{p:q} \mathbb{R}_{p:q}^{\mathbb{U}} \times {}^{p:q} \mathbb{R}_{p:q}^{\mathbb{U}}$$

$${}^{p:q} \mathbb{R}_{p:q}^{\mathbb{U}}$$

$$\mathbb{R}_{2n|n}$$

$$\begin{array}{c}
\begin{array}{cccc|cccc}
0 & 0 & 0 & 1_n & 0 & 0 & 1_n & 0 \\
0 & 0 & -1_n & 0 & 0 & 0 & 0 & 1_n \\
0 & 1_n & 0 & 0 & -1_n & 0 & 0 & 0 \\
-1_n & 0 & 0 & 0 & 0 & -1_n & 0 & 0
\end{array} & = & \begin{array}{cccc}
0 & -1_n & 0 & 0 \\
1_n & 0 & 0 & 0 \\
0 & 0 & 0 & 1_n \\
0 & 0 & -1_n & 0
\end{array} \\
\\
\begin{array}{cc|cc|cc|cc}
-1 & & 0 & 1_n & 0 & 0 & 1_n & 0 \\
& & -1_n & 0 & 0 & 0 & 0 & 1_n \\
0 & 1_n & & & -1_n & 0 & 0 & 0 \\
-1_n & 0 & & & 0 & -1_n & 0 & 0
\end{array} & = & \begin{array}{cccc}
0 & -1_n & 0 & 0 \\
1_n & 0 & 0 & 0 \\
0 & 0 & 0 & 1_n \\
0 & 0 & -1_n & 0
\end{array}
\end{array}$$

$$\mathbb{R}_{n|n}$$

$$\mathbb{R}_{n|n}$$

$$\mathbb{R}_{2n|n}$$

$$\mathbb{R}_{2n|n}$$

$$\mathbb{R}_{2n|n}$$

$$\mathbb{R}_{p+q|p+q}$$