

$$\sum_{n \geq 0} \frac{\binom{n}{-1}}{n} x^{2n+1}$$

$$a_n = \frac{\binom{n}{-1} x^{2n+1}}{n} = \frac{\overline{x}^{2n+1}}{n}$$

$$\Rightarrow \frac{a_{n+1}}{a_n} = \frac{\overline{x}^{2n+3}}{n+1} \frac{n}{\overline{x}^{2n+1}} = \frac{n}{n+1} \overline{x}^2 \rightsquigarrow \overline{x}^2 < 1 \Leftrightarrow \overline{x} < 1$$

$$x = 1 \xrightarrow{\text{Leib}} \sum_{n \geq 0} \frac{\binom{n}{-1}}{n} \text{ conv}$$

$$x = -1 \Rightarrow \sum_{n \geq 0} \frac{\binom{n}{-1}}{n} (-1)^{2n+1} \stackrel{\text{Leib}}{=} - \sum_{n \geq 0} \frac{\binom{n}{-1}}{n} \text{ conv}$$

$$\sum_n \frac{2^n}{n!} x^n: \mathbb{R}$$

$$\sum_n \frac{n!}{4^n} x^n: 0$$

$$\sum_n \frac{x^n}{n2^n}: -2 \leq x < 2$$

$$\sum_n \frac{4^n}{n^2 \pi^n} x^n: -\frac{\pi}{4} \leq x \leq \frac{\pi}{4}$$

$$\sum_n \frac{x^n}{n^2}: -1 \leq x \leq 1$$

$$\sum_n \frac{n}{4^n} x^n: -4 < x < 4$$

$$\sum_n \frac{2^n (n+1)}{n^n} x^n: \mathbb{R}$$

$$\sum_n \frac{x^n}{n^3 3^n}: -3 \leq x \leq 3$$

$$\sum_n \frac{2^n}{n^2+1} x^n: \quad -\frac{1}{2} \leq x \leq \frac{1}{2}$$

$$\sum_n \frac{x^n}{n10^{n-1}}: \quad -10 \leq x < 10$$

$$\sum_n \frac{n^2}{3^n(n^3+3)} x^n: \quad -3 \leq x < 3$$

$$\sum_n \frac{\sqrt{n}4^n}{n+1} x^n: \quad -\frac{1}{4} \leq x < \frac{1}{4}$$

$$\sum_n \frac{(-1)^n}{n^2+1} x^n: \quad -1 \leq x \leq 1$$

$$\sum_n \frac{(-3)^n}{n} x^n: \quad -\frac{1}{3} < x \leq \frac{1}{3}$$

$$\sum_n \left(\frac{3^n+1}{4^n}\right)^n x^n: \quad \mathbb{R}$$

$$\sum_n \frac{4^n+5^n+6^n}{n} x^n: \quad -\frac{1}{6} \leq x < \frac{1}{6}$$

$$\sum_n \frac{(n+1)^2}{5^n+6^n+7^n} x^n: \quad -7 < x < 7$$

$$\sum_n \frac{(-1)^n}{\sqrt{n}3^{n-1}} x^n: \quad -3 < x \leq 3$$

$$\sum_n \frac{n!}{2^n} x^n: \quad 0$$

$$\sum_n \frac{(n!)^2}{(2n)!} x^n: \quad -4 < x < 4$$

$$\sum_n \frac{3^{2n}\sqrt{n}}{2^n n^{1/3}} x^n: \quad -\frac{2}{9} < x < \frac{2}{9}$$

$$\sum_n \frac{n!}{(2n)!} x^n: \quad \mathbb{R}$$

$$\sum_n \frac{x^n}{n^2 10^{2n}}: \quad -100 \leq x \leq 100$$

$$\sum_n \frac{5\sqrt{n}}{n^4 2^n} x^n: \quad -2 \leq x \leq 2$$

$$\sum_n \frac{2^n}{3n^{1/4}} x^n: \quad -\frac{1}{2} \leq x < \frac{1}{2}$$

$$\sum_n \frac{n-1}{n^3 2^n} x^n: \quad -2 \leq x \leq 2$$

$$\sum_n \frac{7^{\sqrt{n}}}{n^3} x^n: \quad -1 < x < 1$$

$$\sum_n \frac{n3^n}{(n+1)^2} (x-1)^n: \quad \frac{2}{3} \leq x < \frac{4}{3}$$

$$\sum_n \frac{(n+1)^2}{n3^n} (x-1)^n: \quad -2 < x < 4$$

$$\sum_n \frac{n3^n}{\sqrt{n+1}} (x-2)^n: \quad \frac{5}{3} < x < \frac{7}{3}$$

$$\sum_n \frac{(x-1)^n}{n2^n}: \quad -1 \leq x < 3$$

$$\sum_n \frac{n}{3^{n+1}} (x-2)^n: \quad -1 < x < 5$$

$$\sum_n \frac{(x+3)^n}{n^2}: \quad -4 \leq x \leq -2$$

$$\sum_n \frac{(-1)^n}{(2n+1)^2} (x-1)^n: \quad 0 \leq x \leq 2$$

$$\sum_n \frac{(-2)^{n+1}}{9(n^5+3)n} (x+3)^n: \quad -\frac{13}{2} \leq x \leq \frac{1}{2}$$

$$\sum_n \frac{n^2}{3^n(n^3+2)} (x+2)^n: \quad -5 \leq x < 1$$

$$\sum_n \frac{(-3)^n}{(2n+1)^2} (x-1)^n: \quad \frac{2}{3} \leq x \leq \frac{4}{3}$$

$$\sum_n \frac{2^n}{n^2+2} (x+3)^n: \quad -\frac{7}{2} \leq x \leq -\frac{5}{2}$$

$$\sum_n \frac{(-1)^n}{(2n+1)^2} (x-1)^n: \quad 0 \leq x \leq 2$$

$$\sum_n 2^{n^2} \left( \frac{n+1}{2n+4} \right)^n (x+2)^n: \quad -2$$

$$\sum_n \frac{n^2}{n^3+3^n} (x-3)^n: \quad 0 < x < 6$$

$$\sum_n \frac{n+1}{9n^2n} x^{2n}: \quad -2 < x < 2$$

$$\sum_n \frac{n9^{n+1}}{n+1} x^{2n}: \quad -\frac{1}{3} < x < \frac{1}{3}$$

$$\sum_n \frac{n4^n}{\sqrt{n+1}} x^{2n}: \quad -\frac{1}{2} < x < \frac{1}{2}$$

$$\sum_n \left( \frac{1^n}{5} + \frac{1^n}{6} \right) x^{2n}: \quad -\sqrt{5} < x < \sqrt{5}$$

$$\sum_n \frac{n}{(n^2+1)16^{n+1}} x^{2n}: \quad -4 < x < 4$$

$$\sum_n \frac{(-4)^n}{n+1} x^{2n}: \quad -\frac{1}{2} \leq x \leq \frac{1}{2}$$

$$\sum_n \frac{n^2}{16^n} x^{2n}: \quad -4 < x < 4$$

$$\sum_n \frac{n^2 9^n}{x^{2n}}: \quad -3 \leq x \leq 3$$

$$\sum_n^{\mathbb{N}} \frac{z^n}{n^n}$$

$$\sum_{2 \leq n} \frac{1}{n} x^n$$

$$\sum_n^{\mathbb{N}} \frac{(2n)!}{(n!)^2} (x-1)^n$$

$$\sum_n^{\mathbb{N}} 1 \cdot 3 \cdot 5 \cdots (2n-1) x^n$$

$$\sum_n^{\mathbb{N}} \pi^{n/2} x^n$$

$$\sum_n^{\mathbb{N}} \frac{1+2+\dots+n}{n} x^{2n-1}$$

$$\sum_n^{\mathbb{N}} \frac{1 \cdot 5 \cdot 9 \cdots (4n-3)}{2 \cdot 4 \cdot 6 \cdots 2n} x^n$$