

$$z \rtimes \begin{bmatrix} \alpha & b & \beta \\ c & d & \acute{c} \\ \gamma & \acute{b} & \delta \end{bmatrix} = \frac{\varepsilon b + zd - z \acute{b} / 2\varepsilon}{\alpha + zc/\varepsilon - z \acute{\gamma} / 2\varepsilon^2}$$

$$[\varepsilon \quad z \quad -z \acute{z} / 2\varepsilon] \begin{bmatrix} \alpha & b & \beta \\ c & d & \acute{c} \\ \gamma & \acute{b} & \delta \end{bmatrix}$$

$$= [\varepsilon\alpha + zc - z \acute{\gamma} / 2\varepsilon \quad \varepsilon b + zd - z \acute{b} / 2\varepsilon \quad \varepsilon\beta + z\acute{c} - z \acute{z} \delta / 2\varepsilon] = \left[ \varepsilon \quad \frac{\varepsilon b + zd - z \acute{b} / 2\varepsilon}{\alpha + zc/\varepsilon - z \acute{\gamma} / 2\varepsilon^2} \quad \frac{\varepsilon\beta + z\acute{c} - z \acute{z} \delta / 2\varepsilon}{\alpha + zc/\varepsilon - z \acute{\gamma} / 2\varepsilon^2} \right]$$

$$\begin{bmatrix} \alpha & b & \beta \\ c & d & \acute{c} \\ \gamma & \acute{b} & \delta \end{bmatrix}^T \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} + \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} \alpha & b & \beta \\ c & d & \acute{c} \\ \gamma & \acute{b} & \delta \end{bmatrix} = 0 \Leftrightarrow \begin{bmatrix} \alpha & b & 0 \\ c & d & -\acute{b} \\ 0 & -\acute{c} & -\alpha \end{bmatrix}$$

$$z \rtimes \begin{bmatrix} \alpha & b & 0 \\ c & d & -\acute{b} \\ 0 & -\acute{c} & -\alpha \end{bmatrix} = \varepsilon b + zd + z \acute{z} \acute{c} / 2\varepsilon - \alpha z - zc / \varepsilon$$

$$\partial_t \frac{\varepsilon b_t + z d_t - z \acute{z} \acute{b}_t / 2\varepsilon}{\alpha_t + z c_t / \varepsilon - z \acute{z} \acute{\gamma}_t / 2\varepsilon^2}$$

$$= \frac{(\alpha_0 + z c_0 / \varepsilon - z \acute{z} \acute{\gamma}_0 / 2\varepsilon^2) (\varepsilon b + zd - z \acute{z} \acute{b} / 2\varepsilon) - (\alpha + zc / \varepsilon - z \acute{z} \acute{\gamma} / 2\varepsilon^2) (\varepsilon b_0 + z d_0 - z \acute{z} \acute{b}_0 / 2\varepsilon)}{(\alpha_0 + z c_0 / \varepsilon - z \acute{z} \acute{\gamma}_0 / 2\varepsilon^2)^2}$$

$$= \varepsilon b + zd - z \acute{z} \acute{b} / 2\varepsilon - (\alpha + zc / \varepsilon - z \acute{z} \acute{\gamma} / 2\varepsilon^2) z = \varepsilon b + zd - z \acute{z} \acute{b} / 2\varepsilon - \alpha z - zc / \varepsilon + z \acute{z} \acute{\gamma} z / 2\varepsilon^2$$

$$\left\{ \begin{array}{l} \mathfrak{D} | \mathbb{K} \times \mathbb{L} \times \mathbb{K} \\ \mathfrak{D} | \mathbb{K}^{1+n+1} \\ \mathfrak{D} | \mathbb{K}^{1+n+1} \end{array} \right\} \xrightarrow{\rtimes} \left\{ \begin{array}{l} \mathfrak{C} | \mathbb{L} \\ \mathfrak{C} | \mathbb{K}^n \end{array} \right\}$$

$$\mathbb{L} \rtimes \begin{bmatrix} \delta & \mathbb{L} & \gamma \\ \mathbb{T} & \mathbb{T} & \mathbb{T} \\ \beta & \mathbb{L} & \alpha \end{bmatrix} = \frac{\mathbb{L} + \mathbb{L} \mathbb{T} - \mathbb{L} \mathbb{L}^t / 2\mathbb{L}}{\delta + \mathbb{L} \mathbb{T} - \mathbb{L} \mathbb{L}^t / 2\beta}$$

$$\begin{aligned}
& \left\{ \begin{array}{l} \mathfrak{D}|\mathbb{K} \times \mathbb{L} \times \mathbb{K} \\ \mathfrak{D}_{1+n+1} \mathbb{K}^{1+n+1} \end{array} \right. \xrightarrow{\times} \left\{ \begin{array}{l} \mathfrak{G}|\circ \mathbb{L} \\ \mathfrak{G}|\circ \mathbb{K}^n \end{array} \right. \\
& \times \begin{bmatrix} -\alpha & \mathbb{L} & 0 \\ \mathbb{T} & \mathbb{T} & -\mathbb{L}^t \\ 0 & -\mathbb{T} & \alpha \end{bmatrix} = \underbrace{\mathbb{L} + \mathbb{L}\mathbb{T} - \mathbb{L}\mathbb{L}^t/2\mathbb{L} + \mathbb{L}\alpha - \mathbb{L}\mathbb{T}\mathbb{T}}_{\partial \mathbb{L}} \frac{\partial}{\partial \mathbb{L}} \\
& \left\{ \begin{array}{l} \mathfrak{D}|\mathbb{K} \times \mathbb{L} \times \mathbb{K} \\ \mathfrak{D}_{1+n+1} \mathbb{K}^{1+n+1} \end{array} \right. \xrightarrow{\times} \left\{ \begin{array}{l} \mathfrak{G}|\circ \mathbb{L} \\ \mathfrak{G}|\circ \mathbb{K}^n \end{array} \right. \\
& \quad \quad \quad \uparrow \mathbf{e} \quad \quad \quad \uparrow \mathbf{e} \\
& \left\{ \begin{array}{l} \mathfrak{D}|\mathbb{K} \times \mathbb{L} \times \mathbb{K} \\ \mathfrak{D}_{1+n+1} \mathbb{K}^{1+n+1} \end{array} \right. \xrightarrow{\times} \left\{ \begin{array}{l} \mathfrak{G}|\circ \mathbb{L} \\ \mathfrak{G}|\circ \mathbb{K}^n \end{array} \right.
\end{aligned}$$