

$$\frac{1}{2} \frac{3}{4} \frac{(2n-1)}{(2n)} \rightsquigarrow \text{anti}$$

$$a_n = \frac{n!}{n^{1/2}} \left(\frac{e}{n}\right)^n \underset{\text{STIR}}{\rightsquigarrow} \sqrt{2\pi}$$

$$\frac{1+x}{1-x} = \underbrace{1+x}_{\sum_0^1} \sum_n^{\mathbb{N}} x^n = 1 + 2x + 2x^2 + \sum_{n \geq 3} 2x^n < 1 + 2x + 2x^2 + \sum_{n \geq 3} \frac{2^n}{n!} x^n = e^{2x}$$

$$e \frac{a_n}{a_{n+1}} = \left(\frac{n+1}{n}\right)^{n+1/2} = \left(\frac{1 + \frac{1}{2n+1}}{1 - \frac{1}{2n+1}}\right)^{n+1/2} < \left(\exp \frac{2}{2n+1}\right)^{n+1/2} = \exp \frac{2(n+1/2)}{2n+1} = e$$

$$\Rightarrow \frac{a_n}{a_{n+1}} < 1 \Rightarrow a_n \downarrow$$

$$\lim_{x \downarrow 0} x^x$$

$$(n!)^{-1/n} \text{ konv?}$$