

$$\frac{dx}{dt} = g\left(\frac{x}{t}\right)$$

$$z = \frac{x}{t} \Rightarrow x = zt \Rightarrow z g = \underline{x} = \underline{z}t + z \Rightarrow \frac{dz}{z g - z} = \frac{dt}{t} \text{ sep}$$

$$\Rightarrow \int \frac{dz}{z g - z} = \int \frac{dt}{t} = C + \log t$$

$$x \underline{y} - 2y = 3x \Rightarrow \underline{y} = 3 + 2\frac{y}{x} \Rightarrow \underline{z} = \frac{3+z}{x} \Rightarrow \sqrt{z+3} = Ae^x \Rightarrow z = Ae^x - 3 \Rightarrow y = Axe^x - 3x$$

$$2xy \underline{y} - y^2 + x^2 = 0 \Rightarrow \underline{y} = \frac{1}{2} \left(\frac{y}{x} - \frac{x}{y} \right) \Rightarrow \underline{z} = -\frac{1}{2} \frac{z+z^{-1}}{x} \Rightarrow \cancel{7x} + C = -2 \int \frac{z}{z^2+1} = -\cancel{z^2+1}$$

$$\Rightarrow z^2 + 1 = \frac{1}{Ax} \Rightarrow y = \sqrt{\frac{x}{A} - x^2} \quad y(5)=2 \Rightarrow A = \frac{5}{29}$$

$$x^2 dy - \underline{y^2 + 2xy} dx = 0 \Rightarrow \underline{y} = \left(\frac{y}{x}\right)^2 + 2\frac{y}{x} \Rightarrow \underline{z} = \frac{z^2+z}{x} \Rightarrow \cancel{7x} + C = \int \frac{1}{z(z+1)} = \int \frac{1}{z} - \int \frac{1}{z+1} = \frac{\cancel{z}}{z+1}$$

$$\Rightarrow \frac{z}{z+1} = Ax \Rightarrow z = \frac{Ax^2}{1-Ax} \Rightarrow y = \frac{Ax^3}{1-Ax}$$

$$x dy - y dx = (xy)^{1/2} dx \Rightarrow \underline{y} = \left(\frac{y}{x}\right)^{1/2} + \frac{y}{x} \Rightarrow y = x \left(\frac{\cancel{7x} + C}{2} \right)^2 \Rightarrow y = x + \frac{x}{C - \cancel{7x}}$$

$$x^2 \underline{y} = x^2 - xy + y^2$$

$$\underline{y} = \frac{x+3y}{x-y} = \frac{1+3y/x}{1-y/x} \Rightarrow \cancel{7x} + C = \int \frac{1-z}{(z+1)^2} = -\int \frac{z+1}{(z+1)^2} + 2 \int \frac{1}{(z+1)^2} = -\cancel{z+1} + \frac{2}{z+1}$$

$$x^2 dy + \underline{y^2 - xy} dy = 0$$