

$$\begin{aligned}
 & U \xrightarrow[\text{stet}]{\mathcal{A}} {}_n\mathbb{K}^n \\
 & U \xrightarrow[\text{stet}]{\mathcal{A}} {}_n\mathbb{K} \\
 & U \xrightarrow[\text{stet diff}]{\mathcal{A}} {}_n\mathbb{K} \\
 U_{+ \begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} &= \frac{U \xrightarrow[\text{stet diff}]{\mathcal{A}} {}_n\mathbb{K}}{\mathcal{A} = \mathcal{A}_i \cdot \mathcal{A} + \mathcal{A}; \quad \mathcal{A} = \mathcal{A}_i^j \cdot \mathcal{A} + \mathcal{A}} \text{ inhom Lsg-Raum}
 \end{aligned}$$

$$U_{+ \begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} + U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} \subset U_{+ \begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K}$$

$$U_{+ \begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} - U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} \subset U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K}$$

$$\mathcal{A} \in U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} \wedge \mathcal{A} \in U_{+ \begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} \Rightarrow \underline{\mathcal{A} + \mathcal{A}} = \mathcal{A} + \mathcal{A} = \overbrace{\mathcal{A} \cdot \mathcal{A}} + \overbrace{\mathcal{A} \cdot \mathcal{A} + \mathcal{A}} = \mathcal{A} \cdot \overbrace{\mathcal{A} + \mathcal{A}} + \mathcal{A} \Rightarrow \mathcal{A} + \mathcal{A} \in U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K}$$

$$\mathcal{A} \in U_{+ \begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} \Rightarrow \underline{\mathcal{A} - \mathcal{A}} = \mathcal{A} - \mathcal{A} = \overbrace{\mathcal{A} \cdot \mathcal{A} + \mathcal{A}} - \overbrace{\mathcal{A} \cdot \mathcal{A} + \mathcal{A}} = \mathcal{A} \cdot \overbrace{\mathcal{A} - \mathcal{A}} \Rightarrow \mathcal{A} - \mathcal{A} \in U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K}$$

$$\text{part Lsg } \mathcal{A} \in U_{+ \begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} \Rightarrow U_{+ \begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} = \mathcal{A} + U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K}$$

$$\subset: U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} - \mathcal{A} \subset U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} - U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} \subset U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K}$$

$$\supset: \mathcal{A} + U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} \subset U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} + U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K} \subset U_{\begin{smallmatrix} \blacktriangle \\ \uparrow \\ n \end{smallmatrix}} \mathbb{K}$$

$$x \cdot y = x \cdot \mathbb{A} \int_0^x \mathbb{A}^{-1} \cdot \mathcal{A} \text{ part sol}$$

$$\begin{aligned} \text{Ansatz } x \cdot y &= x \cdot \mathbb{A} \cdot x u \Rightarrow x \cdot \mathcal{A} \cdot x \cdot \mathbb{A} \cdot x u + x \cdot \mathcal{A} = x \cdot \mathcal{A} \cdot x \cdot y + x \cdot \mathcal{A} = x \cdot y = x \cdot \mathbb{A} \cdot u = x \cdot \mathbb{A} \cdot x u + x \cdot \mathbb{A} \cdot x u \\ &= x \cdot \mathcal{A} \cdot x \cdot \mathbb{A} \cdot x u + x \cdot \mathbb{A} \cdot x u \Rightarrow x \cdot \mathcal{A} = x \cdot \mathbb{A} \cdot x u \Rightarrow x \cdot \mathbb{A}^{-1} \cdot x \cdot \mathcal{A} = x u \Rightarrow \int \mathbb{A}^{-1} \cdot \mathcal{A} = x u \end{aligned}$$

$$U_{\mathbb{A}^{-1} \cdot \mathcal{A}} \mathbb{K} \ni x \cdot \mathbb{A} \cdot \underbrace{\int_0^x \mathbb{A}^{-1} \cdot \mathcal{A} + \cdot c}_o = x \cdot \mathbb{A}^j \cdot \underbrace{\int_j^x \mathbb{A}^{-1} \cdot \mathcal{A} + \cdot c}_o = \begin{bmatrix} x \cdot \mathbb{A}^1 \cdot \underbrace{\int_0^x \mathbb{A}^{-1} \cdot \mathcal{A} + \cdot c}_o \\ x \cdot \mathbb{A}^n \cdot \underbrace{\int_0^x \mathbb{A}^{-1} \cdot \mathcal{A} + \cdot c}_o \end{bmatrix} = \begin{bmatrix} x \cdot \mathbb{A}^j \cdot \underbrace{\int_j^x \mathbb{A}^{-1} \cdot \mathcal{A} + \cdot c}_o \\ x \cdot \mathbb{A}^j \cdot \underbrace{\int_j^x \mathbb{A}^{-1} \cdot \mathcal{A} + \cdot c}_o \end{bmatrix} \text{ gen sol}$$