

$$R = \bar{a} \underline{\mathbb{L}}^0 + \bar{a} \underline{\mathbb{L}}^1 + a \underline{\mathbb{L}}^0$$

$$\underline{\mathbb{L}}^0 \underline{\mathbb{L}}^1 - \underline{\mathbb{L}}^1 \underline{\mathbb{L}}^0 \neq 0$$

$${}^x \mathfrak{I} = - {}^x \mathbb{L}^0 \int_{dt}^x \frac{t \underline{\mathbb{L}}^1 t R}{t W t a} + {}^x \mathbb{L}^1 \int_{dt}^x \frac{t \underline{\mathbb{L}}^0 t R}{t W t a} = - {}^x \mathbb{L}^0 \int \frac{\underline{\mathbb{L}}^1 R}{W a} + {}^x \mathbb{L}^1 \int \frac{\underline{\mathbb{L}}^0 R}{W a}$$

$$\text{Ansatz } {}^x \mathfrak{I} = {}^x u_0 {}^x \mathbb{L}^0 + {}^x u_1 {}^x \mathbb{L}^1$$

$$\underline{u}_0 \underline{\mathbb{L}}^0 + \underline{u}_1 \underline{\mathbb{L}}^1 = 0$$

$$\underline{\mathbb{L}}^0 = \underline{u}_0 \underline{\mathbb{L}}^0 + \underline{u}_1 \underline{\mathbb{L}}^1$$

$$\Rightarrow \underline{\mathbb{L}}^0 = \underline{u}_0 \underline{\mathbb{L}}^0 + u_0 \underline{\mathbb{L}}^0 + \underline{u}_1 \underline{\mathbb{L}}^1 + u_1 \underline{\mathbb{L}}^1 = u_0 \underline{\mathbb{L}}^0 + \underbrace{\underline{u}_0 \underline{\mathbb{L}}^0 + \underline{u}_1 \underline{\mathbb{L}}^1}_{=0} + u_1 \underline{\mathbb{L}}^1 = u_0 \underline{\mathbb{L}}^0 + u_1 \underline{\mathbb{L}}^1$$

$$\Rightarrow \underline{\mathbb{L}}^0 = \underline{u}_0 \underline{\mathbb{L}}^0 + u_0 \underline{\mathbb{L}}^0 + \underline{u}_1 \underline{\mathbb{L}}^1 + u_1 \underline{\mathbb{L}}^1$$

$$\Rightarrow R = \bar{a} \underline{\mathbb{L}}^0 + \bar{a} \underline{\mathbb{L}}^1 + a \underline{\mathbb{L}}^0 = \bar{a} \left(\underline{u}_0 \underline{\mathbb{L}}^0 + u_0 \underline{\mathbb{L}}^0 + \underline{u}_1 \underline{\mathbb{L}}^1 + u_1 \underline{\mathbb{L}}^1 \right) + \bar{a} \left(u_0 \underline{\mathbb{L}}^0 + u_1 \underline{\mathbb{L}}^1 \right) + a \left(u_0 \underline{\mathbb{L}}^0 + u_1 \underline{\mathbb{L}}^1 \right)$$

$$= u_0 \underbrace{\bar{a} \underline{\mathbb{L}}^0 + \bar{a} \underline{\mathbb{L}}^1 + a \underline{\mathbb{L}}^0}_{=0} + u_1 \underbrace{\bar{a} \underline{\mathbb{L}}^1 + \bar{a} \underline{\mathbb{L}}^0 + a \underline{\mathbb{L}}^1}_{=0} + a \left(u_0 \underline{\mathbb{L}}^0 + u_1 \underline{\mathbb{L}}^1 \right)$$

$$\Rightarrow \underline{u}_0 \underline{\mathbb{L}}^0 + \underline{u}_1 \underline{\mathbb{L}}^1 = R/a \Rightarrow \begin{array}{c|cc} \underline{\mathbb{L}}^0 & \underline{\mathbb{L}}^1 & \\ \hline \underline{\mathbb{L}}^0 & \underline{u}_0 & \\ \underline{\mathbb{L}}^1 & \underline{u}_1 & \end{array} = \frac{0}{R/a}$$

$$\Rightarrow \frac{\underline{u}_0}{\underline{u}_1} = \frac{\underline{\mathbb{L}}^0 \quad \underline{\mathbb{L}}^1}{\underline{\mathbb{L}}^0 \quad \underline{\mathbb{L}}^1} \frac{0}{R/a} = \frac{1}{\underline{\mathbb{L}}^0 \underline{\mathbb{L}}^1 - \underline{\mathbb{L}}^0 \underline{\mathbb{L}}^0} \frac{\underline{\mathbb{L}}^1}{-\underline{\mathbb{L}}^0} \frac{-\underline{\mathbb{L}}^1}{\underline{\mathbb{L}}^0} \frac{0}{R/a}$$

$$\Rightarrow \begin{cases} \underline{u}_0 = - \frac{\underline{\mathbb{L}}^1 R}{a (\underline{\mathbb{L}}^0 \underline{\mathbb{L}}^1 - \underline{\mathbb{L}}^1 \underline{\mathbb{L}}^0)} \\ \underline{u}_1 = \frac{\underline{\mathbb{L}}^0 R}{a (\underline{\mathbb{L}}^0 \underline{\mathbb{L}}^1 - \underline{\mathbb{L}}^0 \underline{\mathbb{L}}^0)} \end{cases} \Rightarrow \begin{cases} u_0 = - \int dx \frac{\underline{\mathbb{L}}^1 R}{a (\underline{\mathbb{L}}^0 \underline{\mathbb{L}}^1 - \underline{\mathbb{L}}^0 \underline{\mathbb{L}}^0)} \\ u_1 = \int dx \frac{\underline{\mathbb{L}}^0 R}{a (\underline{\mathbb{L}}^0 \underline{\mathbb{L}}^1 - \underline{\mathbb{L}}^0 \underline{\mathbb{L}}^0)} \end{cases}$$

$${}^x \mathfrak{I} = - {}^x \mathbb{L}^0 \left(c_0 + \int_{dt}^x \frac{t \underline{\mathbb{L}}^1 t R}{t W t a} \right) + {}^x \mathbb{L}^1 \left(c_1 + \int_{dt}^x \frac{t \underline{\mathbb{L}}^0 t R}{t W t a} \right) = - {}^x \mathbb{L}^0 \left(c_0 + \int \frac{\underline{\mathbb{L}}^1 R}{W a} \right) + {}^x \mathbb{L}^1 \left(c_1 + \int \frac{\underline{\mathbb{L}}^0 R}{W a} \right)$$

$$\begin{aligned}
& \underline{\underline{y}} + y = \sec x \Rightarrow \begin{cases} {}^x \underline{\underline{L}}^0 \\ {}^x \underline{\underline{L}}^1 \end{cases} = \begin{cases} {}^x \mathfrak{c} \\ {}^x \mathfrak{s} \end{cases} \Rightarrow {}^x W = 1 \\
& \Rightarrow {}^x \mathfrak{N} = -{}^x \mathfrak{c} \int \frac{{}^x \mathfrak{s} \sec x}{1} dx + {}^x \mathfrak{s} \int \frac{{}^x \mathfrak{c} \sec x}{1} dx = -{}^x \mathfrak{c} \int {}^x \mathfrak{t} dx + {}^x \mathfrak{s} \int 1 dx = -{}^x \mathfrak{c} \ln({}^x \mathfrak{c}) + x {}^x \mathfrak{s} \\
& \underline{\underline{y}} - 2\underline{y} + y = \frac{e^x}{x^2 + 1} \Rightarrow \begin{cases} {}^x \underline{\underline{L}}^0 \\ {}^x \underline{\underline{L}}^1 \end{cases} = \begin{cases} e^x \\ xe^x \end{cases} \Rightarrow {}^x W = e^{2x} \\
& \Rightarrow {}^x \mathfrak{N} = -e^x \int \frac{xe^x}{e^{2x}} \frac{e^x}{x^2 + 1} dx + x e^x \int \frac{e^x}{e^{2x}} \frac{e^x}{x^2 + 1} dx = -e^x \int \frac{x}{x^2 + 1} dx + x e^x \int \frac{1}{x^2 + 1} dx = -e^x \frac{\ln(x^2 + 1)}{2} + x e^x \tan^{-1} x \\
& \underline{\underline{y}} + 2\underline{y} + y = e^{-x} {}^x \mathfrak{c} \Rightarrow \begin{cases} {}^x \underline{\underline{L}}^0 \\ {}^x \underline{\underline{L}}^1 \end{cases} = \begin{cases} e^{-x} \\ xe^{-x} \end{cases} \Rightarrow {}^x W = e^{-2x} \\
& \Rightarrow {}^x \mathfrak{N} = -e^{-x} \int \frac{xe^{-x}}{e^{-2x}} e^{-x} {}^x \mathfrak{c} dx + x e^{-x} \int \frac{e^{-x}}{e^{-2x}} e^{-x} {}^x \mathfrak{c} dx = -e^{-x} \int x {}^x \mathfrak{c} dx + x e^{-x} \int {}^x \mathfrak{c} dx \\
& \qquad \qquad \qquad = -e^{-x} \underbrace{{}^x \mathfrak{c} + x {}^x \mathfrak{s}}_{+} + x e^{-x} {}^x \mathfrak{s} = -e^{-x} {}^x \mathfrak{c} \\
& x^2 \underline{\underline{y}} - 4x \underline{y} + 6y = x^4 {}^x \mathfrak{s} \Rightarrow \begin{cases} {}^x \underline{\underline{L}}^0 \\ {}^x \underline{\underline{L}}^1 \end{cases} = \begin{cases} x^2 \\ x^3 \end{cases} \Rightarrow {}^x W = x^4 \\
& \Rightarrow {}^x \mathfrak{N} = -x^2 \int \frac{x^3}{x^4} \frac{x^{4x} \mathfrak{s}}{x^2} dx + x^3 \int \frac{x^2}{x^4} \frac{x^{4x} \mathfrak{s}}{x^2} dx = -x^2 \int x {}^x \mathfrak{s} dx + x^3 \int {}^x \mathfrak{s} dx = -x^2 \underbrace{{}^x \mathfrak{s} - x {}^x \mathfrak{c}}_{+} - x^3 {}^x \mathfrak{c} = -x^2 {}^x \mathfrak{s} \\
& U \xrightarrow[\text{stet}]{\mathfrak{H}} \mathbb{K}^n \\
& U \xrightarrow[\text{stet}]{\mathbf{1}} \mathbb{K} \\
& U \xrightarrow[\text{2-stet diff}]{\mathfrak{Y}} \mathbb{K} \\
& {}_+ \blacktriangleright_n \mathbb{K} = \frac{U}{\mathfrak{Y} = \mathfrak{H} \mathfrak{Y} + \mathbf{1} = \mathfrak{H}_j \mathfrak{Y} + \mathbf{1}} \text{ inhom Lsg-Raum}
\end{aligned}$$

$$\mathbf{y} \in {}_+^U \blacktriangleleft_n \mathbb{K} \Rightarrow {}_+^U \blacktriangleleft_n \mathbb{K} = \mathbf{y} + {}_+^U \blacktriangleleft_n \mathbb{K}$$

$$\supset : \quad 1 \in {}_+^U \blacktriangleleft_n \mathbb{K} \wedge \mathbf{y} \in {}_+^U \blacktriangleleft_n \mathbb{K} \Rightarrow \underline{\underline{1+y}} = \underline{\underline{1}} + \underline{\underline{y}} = \widehat{\mathbf{1}} \cdot \underline{\underline{1}} + \widehat{\mathbf{1}} \cdot \underline{\underline{y}} + \mathbf{1} = \mathbf{1} \cdot \widehat{\underline{\underline{1+y}}} + \mathbf{1} \Rightarrow 1+y \in {}_+^U \blacktriangleleft_n \mathbb{K}$$

$$\subset : \quad \mathbf{y} \in {}_+^U \blacktriangleleft_n \mathbb{K} \Rightarrow \underline{\underline{y-y}} = \underline{\underline{y}} - \underline{\underline{y}} = \widehat{\mathbf{1}} \cdot \underline{\underline{y}} + \mathbf{1} - \widehat{\mathbf{1}} \cdot \underline{\underline{y}} + \mathbf{1} = \mathbf{1} \cdot \widehat{\underline{\underline{y-y}}} \Rightarrow y-y \in {}_+^U \blacktriangleleft_n \mathbb{K}$$