

$$(1 - x^2) \underline{y} - 2x \underline{y} + 2y = 0: \quad \begin{cases} \mathbb{1}^1 = x \\ \mathbb{1}^0 = 1 - \sum_{m \geq 1} \frac{x^{2m}}{2m-1} \end{cases}$$

$$x^2 \underline{y} + x \underline{y} + \left(x^2 - \frac{9}{4}\right) y = 0: \quad \begin{cases} \mathbb{1}^1 = x^{3/2} \sum_{m \geq 0} a_m x^{2m} & a_m = \frac{(-1)^m}{m! 2^m} \prod_{1 \leq j \leq m} \frac{1}{2j+3} \\ \mathbb{1}^0 = x^{-3/2} \sum_{m \geq 0} a_m x^{2m} & a_m = \frac{(-1)^m}{m! 2^m} \prod_{1 \leq j \leq m} \frac{1}{2j-3} \end{cases}$$

$$(1 + x^2) \underline{y} + x \underline{y} - y = 0: \quad \begin{cases} \mathbb{1}^1 = x \\ \mathbb{1}^0 = 1 - \sum_{m \geq 1} (-1)^m \frac{1 \cdot 3 \cdot 5 \cdots (2m-3)}{m! 2^m} x^{2m} \end{cases}$$

$$x \underline{y} + \underline{y} - 4y = 0: \quad \begin{cases} \mathbb{1}^0 = \sum_{n \geq 0} \frac{4^n}{(n!)^2} x^n \\ \mathbb{1}^1 = \mathbb{1}^1 \left(\ln x - 8x + 20x^2 - \frac{1472}{27} x^3 + \dots \right) \end{cases}$$

$$U \xrightarrow[\text{stet}]{\mathbb{1}} \mathbb{K}^n$$

$$U \xrightarrow[\text{n-stet diff}]{\mathbb{1}} \mathbb{K} = \frac{\text{hom Lsg-Raum}}{n \underline{1} + \mathbb{1} \cdot \underline{1} = 0 = n \underline{1} + \sum_j \mathbb{1}^j \underline{1}^j}$$

$$U \xrightarrow{\mathbb{1}} \mathbb{K} \subset U \xrightarrow{\mathbb{1}} \mathbb{K} \text{ lin UR}$$

$$\begin{aligned} U \xrightarrow{\mathbb{1}} \mathbb{K} \ni \mathbb{1} \Rightarrow 0 = n \underline{1} + \mathbb{1} \cdot \underline{1} &\Rightarrow \overbrace{n \underline{1} + \mathbb{1} \cdot \underline{1}} + \overbrace{n \underline{1} + \mathbb{1} \cdot \underline{1}} = \overbrace{n \underline{1} + n \underline{1}} + \overbrace{\mathbb{1} \cdot \underline{1} + \mathbb{1} \cdot \underline{1}} \\ &= \overbrace{n \underline{1} + \mathbb{1} \cdot \underline{1}} + \overbrace{n \underline{1} + \mathbb{1} \cdot \underline{1}} = 0 + 0 = 0 \Rightarrow \mathbb{1} + \mathbb{1} \in U \xrightarrow{\mathbb{1}} \mathbb{K} \end{aligned}$$

$$\text{bel } t \in U \xrightarrow{\text{PicLin}} \bigvee U \xrightarrow[\text{hom Lsg}]{\begin{bmatrix} \mathbb{1}^0 \\ \mathbb{1}^{n-1} \end{bmatrix}} \mathbb{K}^n$$

$${}^t \underline{1}^j = \frac{\partial^i}{\partial t} \underline{1}^j = {}_i \mathbb{1}^j \text{ lin unabh}$$

$$\text{Wronski det} \begin{array}{c|c} \begin{array}{c} t \mathbb{1}^0 \\ \hline 0 \mathbb{1}^0 \\ \hline n-1 \mathbb{1}^0 \end{array} & \begin{array}{c} t \mathbb{1}^{n-1} \\ \hline 0 \mathbb{1}^{n-1} \\ \hline n-1 \mathbb{1}^{n-1} \end{array} \end{array} \neq 0$$

$$\mathbb{1}^0 \dots \mathbb{1}^{n-1} \underset{\text{basic}}{\in} U \begin{array}{c} U \\ \blacktriangleright_n \mathbb{K} \end{array}$$

$$\dim_{\mathbb{K}} U \begin{array}{c} U \\ \blacktriangleright_n \mathbb{K} \end{array} = n$$

$$\mathbb{1}^0 \dots \mathbb{1}^{n-1} \text{ free}$$

$${}_j \mathcal{C} \in \mathbb{K} \wedge 0 = \sum_j^n \mathbb{1}^j {}_j \mathcal{C} \Rightarrow 0 = \sum_j^n \mathbb{1}^j {}_j \mathcal{C} = \sum_j^n \mathbb{1}^j {}_j \mathcal{C} \Rightarrow {}_j \mathcal{C} = 0$$

$$\mathbb{1}^0 \dots \mathbb{1}^{n-1} \text{ hull}$$

$$1 \in U \begin{array}{c} U \\ \blacktriangleright_n \mathbb{K} \end{array} \Rightarrow \mathbb{1}^0 = \sum_j^n \mathbb{1}^j {}_j \mathcal{C} = \sum_j^n \mathbb{1}^j {}_j \mathcal{C} = \sum_j^n \mathbb{1}^j {}_j \mathcal{C}$$

$$\Rightarrow 1 - \sum_j^n \mathbb{1}^j {}_j \mathcal{C} \in U \begin{array}{c} U \\ \blacktriangleright_n \mathbb{K} \end{array} \wedge \mathbb{1}^0 - \sum_j^n \mathbb{1}^j {}_j \mathcal{C} = 0 \Rightarrow \text{eind} \quad 1 - \sum_j^n \mathbb{1}^j {}_j \mathcal{C} = 0 \Rightarrow 1 = \sum_j^n \mathbb{1}^j {}_j \mathcal{C}$$

$$U \begin{array}{c} U \\ \blacktriangleright_n \mathbb{K} \end{array}^n \ni \mathbb{1}^{\cdot} \cdot \mathcal{C} = \mathbb{1}^j {}_j \mathcal{C} = \begin{bmatrix} \mathbb{1}^{\cdot} \cdot \mathcal{C} \\ \mathbb{1}^{\cdot} \cdot \mathcal{C} \end{bmatrix} = \begin{bmatrix} \mathbb{1}^j {}_j \mathcal{C} \\ \vdots \\ \mathbb{1}^j {}_j \mathcal{C} \end{bmatrix} \text{ gen sol}$$