

$$x|y + u|v = \frac{xv + yu}{a(1 + xyuv)} \Big| \frac{yv - xu}{a(1 - xyuv)}$$

$$az = \frac{xv + yu}{1 + xyuv}; \quad aw = \frac{yv - xu}{1 - xyuv}$$

$$f \left( \frac{xv + yu}{1 + xyuv} \right) + \frac{yv - xu}{1 - xyuv} g \left( \frac{xv + yu}{1 + xyuv} \right)$$

$$\frac{xv + yu}{1 + xyuv} = \frac{yu \sqrt{1 - u^2 \varphi x^2} + xv \sqrt{1 - x^2 \varphi u^2}}{1 - x \varphi^u \varphi x^2 u^2}$$

$$\frac{yv - xu}{1 - xyuv} = \frac{yv \sqrt{1 - x^2 u^2} - xu \sqrt{1 - x^2 \varphi^u \varphi}}{1 - x \varphi^u \varphi x^2 u^2}$$

$$\underbrace{xv + yu}_{2m} \underbrace{1 - x \varphi^u \varphi x^2 u^2}_{2n} = \underbrace{yu \sqrt{1 - u^2 \varphi x^2} + xv \sqrt{1 - x^2 \varphi u^2}}_{2i} \underbrace{1 + xyuv}_{2j}$$

$$\underbrace{yv - xu}_{2m+1} \underbrace{1 - x \varphi^u \varphi x^2 u^2}_{2n} = \underbrace{yv \sqrt{1 - x^2 u^2} - xu \sqrt{1 - x^2 \varphi^u \varphi}}_{2i+1} \underbrace{1 - xyuv}_{2j+1}$$

$$\underbrace{1 - x \varphi^u \varphi x^2 u^2}_{2m} \left( \frac{xv + yu}{1 + xyuv} \right)^{2n} = \sum_{i+j=m} x^i \varphi^j u^j \underbrace{1 - u^2 \varphi x^2}_{2i} \underbrace{1 - x^2 \varphi u^2}_{2j} + yv \sum_{i+j=m-1} x^i \varphi^j u^j \underbrace{1 - u^2 \varphi x^2}_{2i+1} \underbrace{1 - x^2 \varphi u^2}_{2j+1}$$

$$\underbrace{1 - x \varphi^u \varphi x^2 u^2}_{2m+1} \left( \frac{xv + yu}{1 + xyuv} \right)^{2n+1} = y \sum_{i+j=m} x^i \varphi^j u^j \underbrace{1 - u^2 \varphi x^2}_{2i+1} \underbrace{1 - x^2 \varphi u^2}_{2j} + v \sum_{i+j=m} x^i \varphi^j u^j \underbrace{1 - u^2 \varphi x^2}_{2i} \underbrace{1 - x^2 \varphi u^2}_{2j+1}$$

$$\text{LHS} = \underbrace{yu \sqrt{1 - u^2 \varphi x^2} + xv \sqrt{1 - x^2 \varphi u^2}}_{2n} = \text{RHS}$$

$$\text{LHS} = \underbrace{yv \sqrt{1 - x^2 u^2} - xu \sqrt{1 - x^2 \varphi^u \varphi}}_{(2n+1)} = \text{RHS}$$

$$\begin{aligned}
& \frac{\overline{2m+1}}{1-x\varphi^u\varphi x^2u^2} \frac{yv-xu}{1-xyuv} \left( \frac{\overline{2m}}{xv+yu} \right) \\
= & \left( \overline{1-x^2u^2} \sum_{i+j}^{m-1} x^i \overline{\varphi^{1u^j} \varphi^{+1}} \overline{u} \overline{1-u\varphi x^2} \overline{x} \overline{1-x\varphi u^2} - xu \overline{1-x\varphi^u\varphi} \sum_{i+j}^m x \overline{\varphi^i u^j} \overline{u} \overline{1-u\varphi x^2} \overline{x} \overline{1-x\varphi u^2} \right) \\
& + yv \left( \overline{1-x^2u^2} \sum_{i+j}^m x \overline{\varphi^i u^j} \overline{u} \overline{1-u\varphi x^2} \overline{x} \overline{1-x\varphi u^2} - xu \overline{1-x\varphi^u\varphi} \sum_{i+j}^{m-1} x \overline{\varphi^i u^j} \overline{u} \overline{1-u\varphi x^2} \overline{x} \overline{1-x\varphi u^2} \right) \\
& \frac{\overline{2m+2}}{1-x\varphi^u\varphi x^2u^2} \frac{yv-xu}{1-xyuv} \left( \frac{\overline{2m+1}}{xv+yu} \right) \\
= & y \left( \overline{1-x^2u^2} \sum_{i+j}^m x \overline{\varphi^i u^j} \overline{\varphi^{+1}} \overline{u} \overline{1-u\varphi x^2} \overline{x} \overline{1-x\varphi u^2} - xu \overline{1-x\varphi^u\varphi} \sum_{i+j}^m x \overline{\varphi^i u^j} \overline{u} \overline{1-u\varphi x^2} \overline{x} \overline{1-x\varphi u^2} \right) \\
& + v \left( \overline{1-x^2u^2} \sum_{i+j}^m x^i \overline{\varphi^{1u^j} \varphi^j} \overline{u} \overline{1-u\varphi x^2} \overline{x} \overline{1-x\varphi u^2} - xu \overline{1-x\varphi^u\varphi} \sum_{i+j}^m x \overline{\varphi^i u^j} \overline{u} \overline{1-u\varphi x^2} \overline{x} \overline{1-x\varphi u^2} \right)
\end{aligned}$$

$$\begin{aligned}
& \text{LHS} = \overline{yv \overline{1-x^2u^2} - xu \overline{1-x\varphi^u\varphi}} \\
& \left( \sum_{i+j}^m x \overline{\varphi^i u^j} \overline{u} \overline{1-u\varphi x^2} \overline{x} \overline{1-x\varphi u^2} + yv \sum_{i+j}^{m-1} x \overline{\varphi^i u^j} \overline{u} \overline{1-u\varphi x^2} \overline{x} \overline{1-x\varphi u^2} \right) = \text{RHS} \\
& \text{LHS} = \overline{yv \overline{1-x^2u^2} - xu \overline{1-x\varphi^u\varphi}} \\
& \left( y \sum_{i+j}^m x \overline{\varphi^i u^j} \overline{u} \overline{1-u\varphi x^2} \overline{x} \overline{1-x\varphi u^2} + v \sum_{i+j}^m x \overline{\varphi^i u^j} \overline{u} \overline{1-u\varphi x^2} \overline{x} \overline{1-x\varphi u^2} \right) = \text{RHS}
\end{aligned}$$