

$$\begin{aligned}
{}^\tau V &= {}^{\tau i L} \mathbf{e} V^{-\tau i L} \mathbf{e} \\
{}^x V &= x^L V x^{-L} \\
L_m \times {}^x V &= \underbrace{x^{m+1} \partial_x + m x^m}_{} {}^x V \\
{}^\tau V &= \overbrace{\exp k^\mu \eta_{\mu\nu} X^\nu + X_0^\nu \tau}^{= {}^\tau k} \mathbf{z} {}^\tau V = {}^\tau k \mathbf{z} {}^\tau V \\
{}^x V &= \overbrace{\exp k^\mu \eta_{\mu\nu} X^\nu - x \not\! X_0^\nu i}^{= {}^x k} \mathbf{z} {}^x V = {}^x k \mathbf{z} {}^x V \\
V &= k \mathbf{z} V \\
x^L V x^{-L} &= \underbrace{x^H \mathbf{z} x^L}_{} \underbrace{k \mathbf{z} V}_{} \underbrace{x^{-H} \mathbf{z} x^{-L}}_{} = \underbrace{x^H k x^{-H}}_{} \mathbf{z} \underbrace{x^L V x^{-L}}_{} \\
\text{tachyon } k^\mu \eta_{\mu\nu} k^\nu &= 2
\end{aligned}$$

$$(\tau)^k = \mathbf{e}^{k \cdot X i} \mathbf{e}^{x \not\! k \cdot (P + k/2)} \mathbf{z} \otimes_n^{>0} \mathbf{e}^{x^{nk} \cdot \partial_n} \mathbf{e}^{-x^{-nk} \cdot \partial_n}$$

$$\begin{aligned}
{}^\tau k &= \overleftarrow{{}^\tau X | k i} \mathbf{e} = \underbrace{\exp k^\mu \eta_{\mu\nu} X^\nu + P^\nu \tau}_{} \mathbf{z} \overbrace{\exp \sum_{n>0} \frac{1}{\sqrt{n}} \langle \mathbf{z} k^\mu \eta_{\mu\nu} \overset{*}{\partial}^{\nu \tau i} \mathbf{e}^n \mathbf{z} \rangle_n}_{} \exp - \overbrace{\sum_{n>0} \frac{1}{\sqrt{n}} \langle \mathbf{z} k^\mu \eta_{\mu\nu} \overset{*}{\partial}^{\nu -\tau i} \mathbf{e}^n \mathbf{z} \rangle_n}_{} \\
&= k \cdot X i \mathbf{e} x^{k \cdot (P + k/2)} \mathbf{z} \otimes_n^{>0} \underbrace{\exp k^\mu \eta_{\mu\nu} \frac{\overset{*}{\partial}^\nu}{\sqrt{n}} \tau i \mathbf{e}^n}_{} \exp - \underbrace{k^\mu \eta_{\mu\nu} \frac{\overset{*}{\partial}^\nu}{\sqrt{n}} -\tau i \mathbf{e}^n}_{} = \text{RHS}
\end{aligned}$$

$$x = {}^{\tau i} \mathbf{e}$$

$$\begin{aligned}
{}^x k &= \overleftarrow{{}^x X | k i} \mathbf{e} = \underbrace{\exp k^\mu \eta_{\mu\nu} X^\nu - x \not\! P^\nu i}_{} \mathbf{z} \otimes_n^{>0} \overbrace{\exp \sum_{n>0} k^\mu \eta_{\mu\nu} \overset{*}{\partial}^\nu x^n}_{} \exp - \overbrace{\sum_{n>0} k^\mu \eta_{\mu\nu} \overset{*}{\partial}^\nu x^{-n}}_{} \\
{}^0 k &= \overleftarrow{{}^0 X | k i} \mathbf{e} = \exp k^\mu \eta_{\mu\nu} X^\nu \mathbf{z} \otimes_n^{>0} \overbrace{\exp \sum_{n>0} k^\mu \eta_{\mu\nu} \frac{\overset{*}{\partial}^\nu}{\sqrt{n}}}_{} \exp - \overbrace{\sum_{n>0} k^\mu \eta_{\mu\nu} \frac{\overset{*}{\partial}^\nu}{\sqrt{n}}}_{}
\end{aligned}$$

$$\text{directon } k^\mu \eta_{\mu\nu} k^\nu = \zeta^\mu \eta_{\mu\nu} k^\nu = 0$$

$${}^z \overleftarrow{k | \zeta} = \zeta | dX^{X | k i} \mathbf{e} = \zeta | \overleftarrow{\partial_\tau X}^{z X | k i} \mathbf{e}$$

$$\text{unbroken symm } n = -1:0:1$$

$${}^{tL_n \mathbf{e}} y V y^n - {}^{tL_n \mathbf{e}} = {}^{y \cdot g} V y \underline{g}^n$$

$$\frac{{}^y V}{y} = \overbrace{a - cg \cdot y}^2 \frac{{}^g y V}{g \cdot y}$$