

$$\tilde{\Omega} = \lim_{t \rightarrow \infty} \frac{\exp \frac{t}{2} \mathcal{H} + E_0 \Omega}{\tilde{\Omega} \star \Omega}$$

$$t_1 < \dots < t_n$$

$$\tilde{\Omega} \star \prod_j \underbrace{e^{t_j \mathcal{H}} f_j e^{-t_j \mathcal{H}}}_{\tilde{\Omega}} \tilde{\Omega} = \int_{d\mathbb{P}} \prod_j^{\mathbb{R}} f_j \left( {}^j t \mathbb{P} \right)$$

$$\begin{aligned} \text{LHS} & \underset{t \rightarrow \infty}{\sim} \frac{\exp \frac{t}{2} \mathcal{H} + E_0 \Omega}{\tilde{\Omega} \star \Omega} \star \exp(t_1 \mathcal{H}) f_1 \exp((t_2 - t_1) \mathcal{H}) f_2 \cdots \exp((t_n - t_{n-1}) \mathcal{H}) f_n \exp(-t_n \mathcal{H}) \frac{\exp \frac{t}{2} \mathcal{H} + E_0 \Omega}{\tilde{\Omega} \star \Omega} \\ & = \frac{\exp(tE_0) \Omega}{\tilde{\Omega} \star \Omega \Omega \star \tilde{\Omega}} \star \exp((t_1 + t/2) \mathcal{H}) f_1 \exp((t_2 - t_1) \mathcal{H}) f_2 \cdots \exp((t_n - t_{n-1}) \mathcal{H}) f_n \exp((t/2 - t_n) \mathcal{H}) \Omega \\ & = \frac{\exp(tE_0) \Omega}{\tilde{\Omega} \star \Omega \Omega \star \tilde{\Omega}} \int_{dx}^x \Omega \int_{d\dot{x}}^{\dot{x}} \Omega \left( e^{t\mathcal{H}/2} \prod_j \underbrace{e^{t_j \mathcal{H}} f_j e^{-t_j \mathcal{H}}}_{\tilde{\Omega}} e^{t\mathcal{H}/2} \right)_{\dot{x}} \\ & = \frac{\exp(tE_0) \Omega}{\tilde{\Omega} \star \Omega \Omega \star \tilde{\Omega}} \int_{dx}^x \Omega \int_{d\dot{x}}^{\dot{x}} \Omega \int_{d\mathbb{P}}^{-\frac{t}{2}:x|\frac{t}{2}:\dot{x}} \prod_j f_j \left( {}^j t \mathbb{P} \right) \underset{t \rightarrow \infty}{\sim} \text{RHS} \end{aligned}$$