

$${}^s\gamma = 1 \mid s \frac{\overline{\alpha_2 \alpha_3 - \alpha_4} + \overline{\alpha_4 \alpha_3 - \alpha_2}}{\overline{\alpha_2 - \alpha_3 + \alpha_4 - \alpha_3}} \mid \frac{\overline{\alpha_2 - \alpha_4} \alpha_3}{\alpha_4 - \alpha_2}$$

$$A = \{\alpha_1 : \alpha_2 : \alpha_3 : \alpha_4\} \text{ dist}$$

$${}^s f = (s - \alpha_1) (s - \alpha_2) (s - \alpha_3) (s - \alpha_4)$$

$$\{\alpha_1 : \alpha_2 : \alpha_3 : \alpha_4\} \gamma = \{\varphi : -1 : 0 : 1\}$$

$${}^u g = \underline{u - \varphi} \underline{u + 1} \underline{u u - 1} :$$

$$\lambda = \frac{\overline{\overline{\alpha_4 - \alpha_2} \overline{\alpha_2 \alpha_3 - \alpha_4} + \overline{\alpha_4 \alpha_3 - \alpha_2} - \overline{\alpha_2 - \alpha_3 + \alpha_4 - \alpha_3} \overline{\alpha_2 - \alpha_4} \alpha_3}}{\prod_{\alpha \in A} a + \alpha \overline{\alpha_2 - \alpha_3 + \alpha_4 - \alpha_3}}$$

$${}^s \overline{\gamma \mid \gamma} = {}^s \gamma \mid \frac{{}^s \gamma \mathbf{1}}{\left(\overline{\alpha_2 \alpha_3 - \alpha_4} + \overline{\alpha_4 \alpha_3 - \alpha_2} + s \overline{\alpha_2 - \alpha_3 + \alpha_4 - \alpha_3} \right)^2} \in {}^s K_{\lambda f} \stackrel{\tilde{\gamma}}{\leftarrow} {}^u K_g \ni {}^u \gamma \mid {}^u \mathbf{1}$$

$$x^2 + y^2 = a^2 (1 + x^2 y^2)$$

$$x^2 - a^2 = (a^2 x^2 - 1) y^2$$

$$y^2 \overline{1 - a^2 x^2} = \underline{x^2 - a^2} \underline{1 - a^2 x^2} = (x - 1/a) (x + 1/a) (x - a) (x + a)$$

$$\begin{cases} {}^x \gamma + {}^x \mathfrak{r} (1 - a^2 x^2) y \\ \gamma \in k(x) \ni \mathfrak{r} \end{cases}$$

$$\underbrace{{}^x\gamma|{}^x\mathfrak{F}}_a \underbrace{{}^x\mathfrak{A}|{}^x\mathfrak{A}} = \underbrace{{}^x\gamma^x\mathfrak{A} + {}^x\mathfrak{F}^x\mathfrak{A}(x-1/a)(x+1/a)(x-a)(x+a)}_{|} \underbrace{{}^x\gamma^x\mathfrak{A} + {}^x\mathfrak{F}^x\mathfrak{A}}$$

$$\begin{aligned} & \left({}^x\gamma + {}^x\mathfrak{F}(1-a^2x^2)y \right) \left({}^x\mathfrak{A} + {}^x\mathfrak{A}(1-a^2x^2)y \right) \\ &= {}^x\gamma^x\mathfrak{A} + {}^x\mathfrak{F}^x\mathfrak{A}(1-a^2x^2)^2y^2 + \left({}^x\gamma^x\mathfrak{A} + {}^x\mathfrak{F}^x\mathfrak{A} \right) (1-a^2x^2)y \\ &= {}^x\gamma^x\mathfrak{A} + {}^x\mathfrak{F}^x\mathfrak{A}(1-a^2x^2)(x^2-a^2) + \left({}^x\gamma^x\mathfrak{A} + {}^x\mathfrak{F}^x\mathfrak{A} \right) (1-a^2x^2)y \end{aligned}$$

$$\begin{array}{ccc} {}^xK_{(a^2-x^2)/(1-a^2x^2)} & \ni & {}^x\gamma + \sqrt{(a^2-x^2)/(1-a^2x^2)}^x\mathfrak{A} = \gamma|\mathfrak{A} \\ \downarrow M_{a/(1-a^2x^2)} & & \\ {}^xK_{\pm a^\pm} & \ni & {}^x\mathfrak{A} + \sqrt{(x+a)(x-a)(x+1/a)(x-1/a)}^x\mathfrak{A} = \mathfrak{A}|\mathfrak{A} \\ \downarrow M_{a+uc}^{-2}C_\gamma & & \\ {}^uK_{0:\pm 1:\varphi} & \ni & {}^u\mathfrak{A} + \sqrt{(u-\varphi)(u+1)u(u-1)}^u\mathfrak{A} = \mathfrak{A}|\mathfrak{A} \\ \downarrow M_{a+sc}^{-2}C_\gamma & & \\ {}^sK_{\alpha_1:\alpha_2:\alpha_3:\alpha_4} & \ni & {}^s\mathfrak{A} + \sqrt{(s-\alpha_1)(s-\alpha_2)(s-\alpha_3)(s-\alpha_4)}^s\mathfrak{A} = \mathfrak{A}|\mathfrak{A} \end{array}$$

$$\begin{array}{ccc}
{}^x K_{(a^2 - x^2) / (1 - a^2 x^2)}^{y^2} & & \ni {}^x \mathfrak{I} + y {}^x \mathfrak{I} = \mathfrak{I} | \mathfrak{I} \\
\downarrow M_{a / (1 - a^2 x^2)} & & \\
{}^x K_{(x + a)(x - a)(x + 1/a)(x - 1/a)}^{z^2} & & \ni {}^x \mathfrak{I} + z {}^x \mathfrak{I} = \mathfrak{I} | \mathfrak{I} \\
\downarrow M_{a + uc}^{-2} C_\gamma & & \\
{}^u K_{(u - \varphi)(u + 1)u(u - 1)}^{v^2} & & \ni {}^u \mathfrak{I} + v {}^u \mathfrak{I} = \mathfrak{I} | \mathfrak{I} \\
\downarrow M_{a + sc}^{-2} C_\gamma & & \\
{}^s K_{(s - \alpha_1)(s - \alpha_2)(s - \alpha_3)(s - \alpha_4)}^{t^2} & & \ni {}^s \mathfrak{I} + t {}^s \mathfrak{I} = \mathfrak{I} | \mathfrak{I}
\end{array}$$