

$$Q = \{1 \cdots q\} \supset I = \{i_1 < \cdots < i_m\} \Rightarrow \zeta_I = \zeta_{i_1} \cdots \zeta_{i_m}$$

$${}^{1|0}\mathbb{C}_{\nabla p|q} \mathbb{C} = \frac{\sum_I z^I \zeta_I}{\zeta^I \in {}^1\mathbb{C}_{\nabla p} \mathbb{C}} = \sum_{0 \leq k \leq q} {}^1\mathbb{C}_{\nabla p} \mathbb{C} \otimes \mathbb{C}_{q-k} \mathbb{C}^q$$

$${}^{1|0}\mathbb{C}_{\nabla p|q} \mathbb{C} = \frac{\zeta \in {}^{1|0}\mathbb{C}_{\nabla p|q} \mathbb{C}}{\Gamma_\nu \int_{dz/\pi^p} \int_{d\zeta} \frac{\overbrace{1 - z\bar{z} - \zeta\bar{\zeta}}^{\nu+q-p-1}}{\Gamma_{\nu+q-p}} z^{|\zeta^*|} \bar{z}^{|\zeta|} \zeta \bar{\zeta} < +\infty}$$

$$\zeta_L = \zeta_{\ell_1} \cdots \zeta_{\ell_k}$$

$$\zeta_L^* \zeta_L = \prod_{\ell} \bar{\zeta}_{\ell} \zeta_{\ell}$$

$$\frac{\overbrace{1 - z\bar{z} - \zeta\bar{\zeta}}^{\nu+q-p-1}}{\Gamma_{\nu+q-p}} = \sum_J \frac{\overbrace{1 - z\bar{z}}^{\nu+|J|-p-1}}{\Gamma_{\nu+|J|-p}} \zeta_{Q \setminus J}^* \zeta_{Q \setminus J}$$

$$\begin{aligned} \text{LHS} &= \frac{\overbrace{1 - z\bar{z}}^{\nu+q-p-1}}{\Gamma_{\nu+q-p}} \frac{\overbrace{\zeta\bar{\zeta}}^{\nu+q-p-1}}{1 - z\bar{z}} = \frac{\overbrace{1 - z\bar{z}}^{\nu+q-p-1}}{\Gamma_{\nu+q-p}} \sum_{\ell} \left[\begin{matrix} \nu+q-p-1 \\ \ell \end{matrix} \right] \frac{\overbrace{-\zeta\bar{\zeta}}^{\ell}}{\overbrace{1 - z\bar{z}}^{\ell} > q} \\ & \stackrel{j=q-\ell}{=} \frac{\overbrace{1 - z\bar{z}}^{\nu+q-p-1}}{\Gamma_{\nu+q-p}} \sum_{j=0}^q \left[\begin{matrix} \nu+q-p-1 \\ q-j \end{matrix} \right] \frac{\overbrace{-\zeta\bar{\zeta}}^{q-j}}{1 - z\bar{z}} = \sum_{j=0}^q \frac{\overbrace{1 - z\bar{z}}^{\nu+j-p-1}}{\Gamma_{\nu+q-p}} \frac{\Gamma_{\nu+q-p}}{\Gamma_{\nu+j-p} (q-j)!} \frac{\overbrace{q-j}}{-\zeta\bar{\zeta}} \\ &= \sum_{j=0}^q \frac{\overbrace{1 - z\bar{z}}^{\nu+j-p-1}}{\Gamma_{\nu+j-p}} \frac{1}{(q-j)!} \sum_{\substack{J \subset Q \\ |J|=j}} (q-j)! \prod_{\ell} \underbrace{-\zeta_{\ell} \bar{\zeta}_{\ell}}_{=\bar{\zeta}_{\ell} \zeta_{\ell}} = \sum_{j=0}^q \sum_{\substack{J \subset Q \\ |J|=j}} \frac{\overbrace{1 - z\bar{z}}^{\nu+j-p-1}}{\Gamma_{\nu+j-p}} \prod_{\ell} \bar{\zeta}_{\ell} \zeta_{\ell} = \text{RHS} \end{aligned}$$

$$\sum_K^{\subset Q} \mathfrak{L}^I \zeta_I \ni {}^{1|0}\mathbb{C}_{p|q}^2 \zeta \xrightarrow{\sim} {}^{1|0}\mathbb{C}_{p|q}^2 \zeta = \sum_{0 \leq k \leq q} {}^1\mathbb{C}_p^2 \zeta^{\nu+k} \mathfrak{X}_{q-k} \mathbb{C}^q = \sum_K^{\subset Q} {}^1\mathbb{C}_p^2 \zeta^{\nu+|K|} \ni \mathfrak{L}^K$$

$$\mathfrak{L}^J \zeta_J \mathfrak{X}_{\nu} \mathfrak{L}^J \zeta_J = \sum_K^{\subset Q} \frac{\Gamma_{\nu}}{\Gamma_{\nu+|K|}} \mathfrak{L}^K \mathfrak{X}_{\nu+|K|} \mathfrak{L}^K$$

$$\begin{aligned} \text{LHS} &= \int_{dz/\pi^p d\zeta} \left({}^{1|0}\mathbb{C}_{p|q} \right) \frac{\nu+q-p-1}{1-z\zeta^*- \zeta\zeta^*} \Gamma_{\nu} \overbrace{z\mathfrak{L}^I \zeta_I}^* z\mathfrak{L}^J \zeta_J = \int_{dz/\pi^p d\zeta} \left({}^{1|0}\mathbb{C}_{p|q} \right) \frac{\nu+q-p-1}{1-z\zeta^*- \zeta\zeta^*} \Gamma_{\nu} z\mathfrak{L}^I z\mathfrak{L}^J \zeta_I^* \zeta_J \\ &= \sum_K^{\subset Q} \int_{dz/\pi^p} {}^1\mathbb{C}_p^{\nu+|K|-p-1} \frac{1}{1-z\zeta^*} \Gamma_{\nu} \int_{d\zeta} {}^{1|0}\mathbb{C}_{|q} \zeta_{Q-K}^* \zeta_{Q-K} z\mathfrak{L}^I z\mathfrak{L}^J \zeta_I^* \zeta_J \\ &\stackrel{I \equiv K}{J \equiv K} = \sum_K^{\subset Q} \int_{dz/\pi^p} {}^1\mathbb{C}_p^{\nu+|K|-p-1} \frac{1}{1-z\zeta^*} \Gamma_{\nu} z\mathfrak{L}^K z\mathfrak{L}^K \underbrace{\int_{d\zeta} \zeta_{Q-K}^* \zeta_{Q-K} \zeta_K^* \zeta_K}_{\int_{d\zeta} {}^{1|0}\mathbb{C}_{|q} \zeta_Q^* \zeta_Q = 1} = \sum_K^{\subset Q} \int_{dz/\pi^p} {}^1\mathbb{C}_p^{\nu+|K|-p-1} \frac{1}{1-z\zeta^*} \Gamma_{\nu} z\mathfrak{L}^K z\mathfrak{L}^K \\ &= \sum_K^{\subset Q} \frac{\Gamma_{\nu}}{\Gamma_{\nu+|K|}} \int_{dz/\pi^p} \frac{1}{1-z\zeta^*} \Gamma_{\nu+|K|} z\mathfrak{L}^K z\mathfrak{L}^K = \text{RHS} \end{aligned}$$

$$\frac{\Gamma_{\nu}}{\underbrace{1-z\zeta^*}_{\nu}} = \sum_I^{\subset Q} \frac{\Gamma_{\nu+|I|}}{\underbrace{1-z\zeta^*}_{\nu+|I|}} \prod_i^I \zeta_i \bar{\omega}_i$$

$$\begin{aligned} \text{LHS} &= \frac{\Gamma_{\nu}}{\underbrace{1-z\zeta^*}_{\nu}} \overbrace{1 - \frac{\zeta\zeta^*}{1-z\zeta^*}}^{-\nu} = \frac{\Gamma_{\nu}}{\underbrace{1-z\zeta^*}_{\nu}} \sum_i^{\mathbb{N}} \begin{bmatrix} -\nu \\ i \end{bmatrix} \overbrace{\frac{-\zeta\zeta^*}{1-z\zeta^*}}_{=0 \leftarrow i > q} \\ &= \frac{\Gamma_{\nu}}{\underbrace{1-z\zeta^*}_{\nu}} \sum_{i=0}^q \begin{bmatrix} -\nu \\ i \end{bmatrix} (-1)^i \overbrace{\frac{\zeta\zeta^*}{1-z\zeta^*}}^i = \sum_{i=0}^q \frac{\Gamma_{\nu+i}}{\underbrace{1-z\zeta^*}_{\nu+i}} \frac{1}{i!} \sum_{|I|=i}^{I \subset Q} i! \prod_i^I \zeta_i \bar{\omega}_i = \text{RHS} \end{aligned}$$

$$\prod_i^I \zeta_i \bar{\omega}_i \omega_I = \bar{\omega}_I \omega_I \zeta_I$$

$$\begin{aligned} \zeta_{i_0} \bar{\omega}_{i_0} \left[\zeta_{i_1} \bar{\omega}_{i_1} \cdots \zeta_{i_k} \bar{\omega}_{i_k} \right] \text{ev } \omega_{i_0} \omega_{i_1} \cdots \omega_{i_k} &= \zeta_{i_0} \bar{\omega}_{i_0} \omega_{i_0} \underbrace{\zeta_{i_1} \bar{\omega}_{i_1} \cdots \zeta_{i_k} \bar{\omega}_{i_k} \omega_{i_1} \cdots \omega_{i_k}}_{\text{Ind}} \equiv \zeta_{i_0} \bar{\omega}_{i_0} \omega_{i_0} \underbrace{\bar{\omega}_{i_k} \cdots \bar{\omega}_{i_1} \omega_{i_1} \cdots \omega_{i_k} \zeta_{i_1} \cdots \zeta_{i_k}} \\ &= \zeta_{i_0} \bar{\omega}_{i_k} \cdots \bar{\omega}_{i_1} \left[\bar{\omega}_{i_0} \omega_{i_0} \right] \text{ev } \omega_{i_1} \cdots \omega_{i_k} \zeta_{i_1} \cdots \zeta_{i_k} = \left[\bar{\omega}_{i_k} \cdots \bar{\omega}_{i_1} \bar{\omega}_{i_0} \omega_{i_0} \omega_{i_1} \cdots \omega_{i_k} \right] \text{ev } \zeta_{i_0} \zeta_{i_1} \cdots \zeta_{i_k} \end{aligned}$$

$$\int_{dw/\pi^p}^{{}^1\mathbb{C}_p} \int_{d\omega}^{{}^{10}\mathbb{C}_{|q}} \frac{\nu+q-p-1}{1-w\bar{w}^*-\omega\bar{\omega}^*} \frac{\Gamma_\nu}{\Gamma_{\nu+q-p}} \frac{w|\omega}{1-z\bar{w}^*-\zeta\bar{\omega}^*} \eta = {}^z\zeta \eta$$

$$\begin{aligned} \int_{dw/\pi^p}^{{}^1\mathbb{C}_p} \int_{d\omega}^{{}^{10}\mathbb{C}_{|q}} \frac{\nu+q-p-1}{1-w\bar{w}^*-\omega\bar{\omega}^*} \frac{\Gamma_\nu}{\Gamma_{\nu+q-p}} \frac{w\mathfrak{L}^M}{1-z\bar{w}^*-\zeta\bar{\omega}^*} \omega_M &= \int_{dw/\pi^p}^{{}^1\mathbb{C}_p} \int_{d\omega}^{{}^{10}\mathbb{C}_{|q}} \frac{\nu+|J|-p-1}{1-w\bar{w}^*} \bar{\omega}_{Q \perp J} \omega_{Q \perp J} \frac{\Gamma_{\nu+|I|}}{\Gamma_{\nu+|I|}} \prod_i^I \zeta_i \bar{\omega}_i w\mathfrak{L}^M \omega_M \\ &\stackrel{J \equiv M}{J \equiv I} \int_{dw/\pi^p}^{{}^1\mathbb{C}_p} \frac{\nu+|I|-p-1}{1-w\bar{w}^*} \frac{\Gamma_{\nu+|I|}}{\Gamma_{\nu+|I|-p}} \frac{w\mathfrak{L}^I}{1-z\bar{w}^*} \int_{d\omega}^{{}^{10}\mathbb{C}_{|q}} \bar{\omega}_{Q \perp I} \omega_{Q \perp I} \underbrace{\prod_i^I \zeta_i \bar{\omega}_i \omega_I}_{= \bar{\omega}_I \omega_I \zeta_I} \\ &= \int_{dw/\pi^p}^{{}^1\mathbb{C}_p} \frac{\nu+|I|-p-1}{1-w\bar{w}^*} \frac{\Gamma_{\nu+|I|}}{\Gamma_{\nu+|I|-p}} \frac{w\mathfrak{L}^I}{1-z\bar{w}^*} \underbrace{\int_{d\omega}^{{}^{10}\mathbb{C}_{|q}} \bar{\omega}_{Q \perp I} \omega_{Q \perp I} \bar{\omega}_I \omega_I \zeta_I}_{=1} = \int_{dw/\pi^p}^{{}^1\mathbb{C}_p} \frac{\nu+|I|-p-1}{1-w\bar{w}^*} \frac{\Gamma_{\nu+|I|}}{\Gamma_{\nu+|I|-p}} \frac{w\mathfrak{L}^I}{1-z\bar{w}^*} \zeta_I = {}^z\mathfrak{L}^I \zeta_I \end{aligned}$$