

$$\begin{aligned}
\text{super-ball } W &= \begin{bmatrix} w \\ \eta \end{bmatrix} \\
\frac{1 - w\bar{w}}{-\eta\bar{w}} \begin{vmatrix} -\bar{\eta}w \\ 1 - \eta\bar{\eta} \end{vmatrix}^{-1} &= \frac{1}{1 - \bar{w}w - \bar{\eta}\eta} \frac{1 - \bar{\eta}\eta}{\eta\bar{w}} \begin{vmatrix} \bar{\eta}w \\ 1 - w\bar{w} - 2\bar{\eta}\eta \end{vmatrix} \\
\frac{1 - w\bar{w}}{-\eta\bar{w}} \begin{vmatrix} -\bar{\eta}w \\ 1 - \eta\bar{\eta} \end{vmatrix} \frac{1 - \bar{\eta}\eta}{\eta\bar{w}} \begin{vmatrix} \bar{\eta}w \\ 1 - w\bar{w} - 2\bar{\eta}\eta \end{vmatrix} &= \frac{1 - w\bar{w} - \bar{\eta}\eta}{0} \begin{vmatrix} 0 \\ 1 - w\bar{w} - \bar{\eta}\eta \end{vmatrix} \\
s_w^\alpha &= \frac{1}{1 - \bar{w}w - \bar{\eta}\eta} \frac{1 - \bar{\eta}\eta}{\eta\bar{w}} \begin{vmatrix} \bar{\eta}w \\ 1 - w\bar{w} - 2\bar{\eta}\eta \end{vmatrix} \frac{\alpha - w\bar{w}}{-\eta\bar{w}} \begin{vmatrix} -\bar{\eta}w \\ \alpha - \eta\bar{\eta} \end{vmatrix} \begin{vmatrix} (1 - \alpha) \begin{bmatrix} w \\ \eta \end{bmatrix} \\ 1 - \iota\bar{v}w - \alpha\bar{\eta}\eta \end{vmatrix} \\
&= \frac{1}{1 - \bar{w}w - \bar{\eta}\eta} \frac{\alpha(1 - \bar{\eta}\eta) - \bar{w}w}{(\alpha - 1)\eta\bar{w}} \begin{vmatrix} (\alpha - 1)w\bar{\eta} \\ \alpha(1 - w\bar{w}) + (1 - 2\alpha)\bar{\eta}\eta \end{vmatrix} \begin{vmatrix} (1 - \alpha)w \\ (1 - \alpha)\eta \end{vmatrix} \\
&\quad \frac{(\alpha - 1)\bar{w}}{(\alpha - 1)\bar{w}} \begin{vmatrix} (\alpha - 1)\bar{\eta} \\ 1 - \alpha(\bar{w}w + \bar{\eta}\eta) \end{vmatrix} \\
\det \frac{1 - z\bar{w}}{-\zeta\bar{w}} \begin{vmatrix} -z\bar{\eta} \\ 1 - \zeta\bar{\eta} \end{vmatrix} &= 1 - z\bar{w} + \zeta\bar{\eta}
\end{aligned}$$