

$$A \in {}_d\mathbb{K}^d$$

$$\|A\| < 1 \Rightarrow \overline{I - A}^{-1} = \sum_n^{\mathbb{N}} A^n$$

$$X \in {}_d\mathbb{K}^d \xrightarrow{F_A} {}_d\mathbb{K}^d \ni {}^X F_A = I + AX$$

$$F_A \text{ contr}_{\|A\|}$$

$$\|{}^X F_A - {}^Y F_A\| = \|\overline{I + AX} - \overline{I + AY}\| = \|AX - AY\| = \|A \overline{X - Y}\| \leq \|A\| \|X - Y\|$$

$${}_d\mathbb{K}^d \text{ voll} \xRightarrow{\text{Ban}} \bigvee_{\text{eind}} {}_d\mathbb{K}^d \ni B = {}^B F_A = I + AB$$

$$B = \overline{I - A}^{-1}$$

$$\overline{I - AB} = B - AB = I$$

$${}^I F_A^n = I + A + \dots + A^n$$

$${}^I F_A^0 = {}^I \text{id} = I$$

$${}^I F_A^{n+1} = I + A {}^I F_A^n = I + A + \dots + A^n \stackrel{\text{ind}}{=} I + A \overline{I + A + \dots + A^n} = I + A + A^2 + \dots + A^{n+1}$$

$$I + A + \dots + A^n = {}^I F_A^n \rightsquigarrow B = \overline{I - A}^{-1}$$