

$$\mathfrak{h}_{\triangleleft_w} \mathbb{C}^\times$$

$$\mathfrak{h} = \frac{z \in \mathbb{C}}{\Re z > 1}$$

$$\zeta(z) \rightsquigarrow \prod_{p \in \mathbb{P}} \overbrace{1 - p^{-z}}^{-1} \in \mathfrak{h}_{\triangleleft_w} \mathbb{C}$$

$$\mathfrak{h} = \frac{z \in \mathbb{C}}{\Re z > 1} \text{ normal conv}$$

$$\zeta(z) \rightsquigarrow \sum_{1 \leq n} n^{-z} \in \mathfrak{h}_{\triangleleft_w} \mathbb{C}$$

$$n = \prod_{p \in \mathbb{P}} p^{n_p}$$

fast alle $n_p = 0$

geom series

$$\mathbb{Q} \xrightarrow{p} \mathbb{R}$$

$$\cup \quad \cup$$

$$\mathbb{Z} \longrightarrow \mathbb{Z}$$

$${}_p^s \mathbb{Q}^{-1} = 1 - p^{-s}$$

$${}_8^s \mathbb{Q} = \prod_p {}_p^s \mathbb{Q} = \prod_p \frac{1}{1 - 1/p^s} = \sum_{n \geq 1} \frac{1}{n^s} = \underline{\mathbb{N}}_{-s}^\times$$

$${}_\infty^s \mathbb{Q} = \frac{\Gamma_{s/2}}{\pi^{s/2}} = \frac{\Gamma_{s/2}}{\Gamma_{1/2}^s} = \int_{du/u}^{\mathbb{R}} -\pi u \mathbf{e}^{-u} u^{s/2} = \underline{\mathbb{R}}_{s/2}^>$$

$${}^s \mathbb{Q} = {}_\infty^s \mathbb{Q} \prod_p {}_p^s \mathbb{Q} = {}_8^s \mathbb{Q} {}_\infty^s \mathbb{Q}$$

$${}_{1/2+s} \mathbb{Q} = {}_{1/2-s} \mathbb{Q}$$

$\mathbb{Z} \backslash \mathbb{Z}p$ finite field $|\mathbb{Z} \backslash \mathbb{Z}p| = p$

$${}^s\mathbb{Q} = \int_{du/u}^{\mathbb{R}^+} \frac{u\mathbb{Z} - 1}{2} u^{s/2}$$

$$\frac{u\mathbb{Z} - 1}{2} = \sum_{n \geq 1} -\pi u_n \mathbf{e}^n$$

$$\int_{du/u}^{\mathbb{R}} \frac{u\mathbb{Z} - 1}{2} u^{s/2} = \int_{du/u}^{\mathbb{R}} \sum_{n \geq 1} -\pi n^2 u \mathbf{e} u^{s/2} = \sum_{n \geq 1} \int_{du/u}^{\mathbb{R}} -\pi n^2 u \mathbf{e} u^{s/2}$$

$$= \sum_{n \geq 1} \frac{1}{\pi^{s/2} n^s} \int_{dv/v}^{\mathbb{R}} -v \mathbf{e} v^{s/2} = \frac{1}{\pi^{s/2}} \int_{dv/v}^{\mathbb{R}} -v \mathbf{e} v^{s/2} \sum_{n \geq 1} \frac{1}{n^s} = \frac{\Gamma_{s/2}}{\pi^{s/2}} \sum_{n \geq 1} \frac{1}{n^s}$$

$$\overline{c\tau + d}^{-1} \overline{a\tau + b} \eta = \overline{c\tau + d}^k \tau \eta: \quad \begin{array}{c|c} a & b \\ \hline c & d \end{array} \in {}^2\mathbb{Z}_2^{\mathbb{C}}$$

$${}^2\overline{\mathbb{Q}}_2^{\mathbb{C}} \times {}^2\mathbb{Q}_2^{\mathbb{C}} \supseteq {}^2\overline{\mathbb{Q}}_2^{\mathbb{C}} \triangleleft {}^2\mathbb{C}$$