

$$\widehat{\pi}_g^x \gamma = {}^x \hat{\delta}_g^{1/2} \hat{g}(x) \gamma: \quad \hat{\pi}_g \gamma = \hat{\delta}_g^{1/2} \hat{\rho}_g \gamma$$

$$\hat{\pi}_\gamma = \frac{1}{2} \hat{\delta}_\gamma + \hat{\rho}_\gamma$$

$$\hat{\pi}_w \gamma = 2 \partial_{w\ddot{u}x} \gamma + \underline{w \star u + u \star w} \left(1 + \frac{\alpha - p}{2} + \alpha \partial_x \right) \gamma + \frac{1 + \alpha}{2} \underline{w \star x + x \star w} \frac{\rho}{\rho} \gamma$$

$$\begin{aligned} \hat{\pi}_w \gamma &= \frac{1}{2} \hat{\delta}_w \gamma + \hat{\rho}_w \gamma = \underbrace{1 + \frac{\alpha - p}{2} + t \frac{1 + \alpha}{2} t_{\rho/t} \rho}_{\text{coefficient}} \underline{w \star u + u \star w} \gamma + \overbrace{2 \partial_{w\ddot{u}x} + \alpha \underline{w \star u + u \star w} \partial_x} \gamma \\ &= 2 \partial_{w\ddot{u}x} \gamma + \underline{w \star u + u \star w} \left(1 + \frac{\alpha - p}{2} + t \frac{1 + \alpha}{2} t_{\rho/t} \rho + \alpha \partial_x \right) \gamma = \text{RHS} \end{aligned}$$

$$\begin{aligned} \phi \star \hat{\pi}_w \psi &= 2 \phi \star \overbrace{\partial_{w\ddot{u}x} \psi} + \phi \star \underline{w \star u} \left(1 + \frac{\alpha - p}{2} + \alpha \partial_x \right) \psi + \frac{1 + \alpha}{2} \phi \star \underline{w \star x} \frac{\rho}{\rho} \psi \\ &\quad + \underline{w \star u} \phi \star \underbrace{1 + \frac{\alpha - p}{2} + \alpha \partial_x}_{\text{coefficient}} \psi + \frac{1 + \alpha}{2} \underline{w \star x} \frac{\rho}{\rho} \phi \star \psi \end{aligned}$$

$$\text{LHS} = 2 \phi \star \overbrace{\partial_{w\ddot{u}x} \psi} + \phi \star \underline{w \star u + u \star w} \left(1 + \frac{\alpha - p}{2} + \alpha \partial_x \right) \psi + \frac{1 + \alpha}{2} \phi \star \underline{w \star x + x \star w} \frac{\rho}{\rho} \psi = \text{RHS}$$

$$2\phi \overline{\partial_{w\ddot{u}x}} \psi + \phi \overline{w \blacktriangleright u} \left(2 + \alpha - p + t(1 + \alpha) \frac{t_{\underline{\rho}}}{t_{\rho}} \right) \psi + \alpha \phi \overline{w \blacktriangleright u \partial_x} \psi + \alpha \overline{\partial_x \phi} \overline{w \blacktriangleright u} \psi = 0$$

$$\begin{aligned} 0 &= \phi \overline{\hat{\pi}_w} \psi + \overline{\hat{\pi}_w \phi} \overline{\blacktriangleright} \psi = \phi \overline{2\partial_{w\ddot{u}x}} \psi + \overline{w \blacktriangleright u + u \blacktriangleright w} \left(1 + \frac{\alpha - p}{2} + t \frac{1 + \alpha}{2} \frac{t_{\underline{\rho}}}{t_{\rho}} + \alpha \partial_x \right) \psi \\ &\quad + 2\partial_{w\ddot{u}x} \phi + \overline{w \blacktriangleright u + u \blacktriangleright w} \left(1 + \frac{\alpha - p}{2} + t \frac{1 + \alpha}{2} \frac{t_{\underline{\rho}}}{t_{\rho}} + \alpha \partial_x \right) \phi \overline{\blacktriangleright} \psi \\ 0 &= 2\phi \overline{\partial_{w\ddot{u}x}} \psi + \phi \overline{w \blacktriangleright u} \left(1 + \frac{\alpha - p}{2} + t \frac{1 + \alpha}{2} \frac{t_{\underline{\rho}}}{t_{\rho}} + \alpha \partial_x \right) \psi \\ &\quad + \overline{u \blacktriangleright w} \left(1 + \frac{\alpha - p}{2} + t \frac{1 + \alpha}{2} \frac{t_{\underline{\rho}}}{t_{\rho}} + \alpha \partial_x \right) \phi \overline{\blacktriangleright} \psi = \text{LHS} \end{aligned}$$

$$\partial_{w\ddot{u}x} \varphi + \overline{w \blacktriangleright u} \left(1 - \frac{p}{2} + \alpha \partial_x \right) \varphi + \frac{1 + \alpha}{2} \overline{w \blacktriangleright x} \left(\frac{t_{\underline{\rho}}}{t_{\rho}} \right) \varphi \in \mathcal{H}^\perp$$

$$2\partial_{w\ddot{u}x} \mathcal{E}_b^{m+} + \overline{w \blacktriangleright u} \left(2 - p + 2\alpha(m + 1) + t(1 + \alpha) \frac{t_{\underline{\rho}}}{t_{\rho}} \right) \mathcal{E}_b^{m+} \in \mathcal{H}^\perp$$

$$\begin{aligned} 0 &= 2\mathcal{E}_a^m \overline{\partial_{w\ddot{u}x}} \mathcal{E}_b^{m+} + \mathcal{E}_a^m \overline{w \blacktriangleright u} \left(2 + \alpha - p + t(1 + \alpha) \frac{t_{\underline{\rho}}}{t_{\rho}} \right) \mathcal{E}_b^{m+} \\ &\quad + \alpha \mathcal{E}_a^m \overline{w \blacktriangleright u \partial_x} \mathcal{E}_b^{m+} + \alpha \overline{\partial_x \mathcal{E}_a^m} \overline{w \blacktriangleright u} \mathcal{E}_b^{m+} \\ &= 2\mathcal{E}_a^m \overline{\partial_{w\ddot{u}x}} \mathcal{E}_b^{m+} + \mathcal{E}_a^m \overline{w \blacktriangleright u} \left(2 + \alpha - p + t(1 + \alpha) \frac{t_{\underline{\rho}}}{t_{\rho}} \right) \mathcal{E}_b^{m+} + \alpha(2m + 1) \mathcal{E}_a^m \overline{w \blacktriangleright u} \mathcal{E}_b^{m+} \\ &\quad c_{m+} \rho_{2m+1} \mathcal{E}_b^m \overline{w \blacktriangleright b} (2m + p + 2 + \alpha - p + \alpha(2m + 1) - (1 + \alpha)(2m + 2)) = 0 \end{aligned}$$

$$\begin{aligned} \hat{\pi}_w \mathcal{E}_b^{m+} &= 2\partial_{w\ddot{u}x} \mathcal{E}_b^{m+} + \overline{w \blacktriangleright u + u \blacktriangleright w} \left(1 + \frac{\alpha - p}{2} + t \frac{1 + \alpha}{2} \frac{t_{\underline{\rho}}}{t_{\rho}} + \alpha \partial_x \right) \mathcal{E}_b^{m+} \\ &= 2\partial_{w\ddot{u}x} \mathcal{E}_b^{m+} + \overline{w \blacktriangleright u + u \blacktriangleright w} \left(1 + \frac{\alpha - p}{2} + t \frac{1 + \alpha}{2} \frac{t_{\underline{\rho}}}{t_{\rho}} \right) \mathcal{E}_b^{m+} + \alpha(m + 1) \overline{w \blacktriangleright u + u \blacktriangleright w} \mathcal{E}_b^{m+} \\ &= 2\partial_{w\ddot{u}x} \mathcal{E}_b^{m+} + \overline{w \blacktriangleright u + u \blacktriangleright w} \left(1 + \frac{\alpha - p}{2} + \alpha(m + 1) + t \frac{1 + \alpha}{2} \frac{t_{\underline{\rho}}}{t_{\rho}} \right) \mathcal{E}_b^{m+} \\ &\quad \underbrace{2w\ddot{u}x + \alpha \overline{w \blacktriangleright u} x = \overline{e_i \blacktriangleright u} 2w\ddot{e}_i x + \alpha \overline{w \blacktriangleright e_i} x}_{\text{}} \end{aligned}$$

$$-\pi'_w \mathcal{E}_b^n = \underbrace{\beta_t + \alpha n}_{\text{}} \underbrace{w \star u + u \star w}_{\text{}} \mathcal{E}_b^n + 2 \underbrace{w \star u}_{\text{}} \mathcal{E}_b^n$$

$$x \mathcal{E}_b^n = \underbrace{x \star b}_{\text{}} \mathcal{E}_b^{n-} = n \mathcal{E}_b^n$$

$$\underbrace{2\beta_t + \alpha(2m+1)}_{\text{}} \underbrace{w \star u}_{\text{}} \mathcal{E}_b^{m+} + 2 \underbrace{w \star u}_{\text{}} \mathcal{E}_b^{m+} \in \mathcal{H}^\perp$$

$$\begin{aligned} \mathcal{E}_a^m \star \underbrace{\beta_t + \alpha n}_{\text{}} \underbrace{w \star u + u \star w}_{\text{}} \mathcal{E}_b^n + 2 \underbrace{w \star u}_{\text{}} \mathcal{E}_b^n &+ \underbrace{\beta_t + \alpha m}_{\text{}} \underbrace{w \star u + u \star w}_{\text{}} \mathcal{E}_a^m + 2 \underbrace{w \star u}_{\text{}} \mathcal{E}_a^m \star \mathcal{E}_b^n \\ &= -\mathcal{E}_a^m \star \underbrace{\pi'_w \mathcal{E}_b^n}_{\text{}} - \underbrace{\pi'_w \mathcal{E}_a^m}_{\text{}} \star \mathcal{E}_b^n = 0 \end{aligned}$$

$$\begin{aligned} 0 &= \mathcal{E}_a^m \star \underbrace{\beta_t + \alpha(m+1)}_{\text{}} \underbrace{w \star u}_{\text{}} \mathcal{E}_b^{m+} + 2 \underbrace{w \star u}_{\text{}} \mathcal{E}_b^{m+} + \underbrace{\beta_t + \alpha m}_{\text{}} \underbrace{u \star w}_{\text{}} \mathcal{E}_a^m \star \mathcal{E}_b^{m+} \\ &= \underbrace{2\beta_t + \alpha(2m+1)}_{\text{}} \mathcal{E}_a^m \star \underbrace{w \star u}_{\text{}} \mathcal{E}_b^{m+} + 2 \mathcal{E}_a^m \star \underbrace{w \star u}_{\text{}} \mathcal{E}_b^{m+} \\ &= \mathcal{E}_a^m \star \underbrace{2\beta_t + \alpha(2m+1)}_{\text{}} \underbrace{w \star u}_{\text{}} \mathcal{E}_b^{m+} + 2 \underbrace{w \star u}_{\text{}} \mathcal{E}_b^{m+} \end{aligned}$$

$$-\pi'_w \mathcal{E}_b^{m+} = \underbrace{\beta_t + \alpha(m+1)}_{\text{}} \underbrace{w \star u + u \star w}_{\text{}} \mathcal{E}_b^{m+} + 2 \underbrace{w \star u}_{\text{}} \mathcal{E}_b^{m+}$$

$$= \underbrace{2\beta_t + \alpha(2m+1)}_{\text{}} \underbrace{w \star u}_{\text{}} \mathcal{E}_b^{m+} + 2 \underbrace{w \star u}_{\text{}} \mathcal{E}_b^{m+} + \underbrace{\beta_t + \alpha m}_{\text{}} \underbrace{u \star w - w \star u}_{\text{}} \mathcal{E}_b^{m+} + \alpha \underbrace{u \star w}_{\text{}} \mathcal{E}_b^{m+}$$

$$\frac{2}{p} \underbrace{e_i \star x}_{\text{}} \mathcal{E}_b^n = n \mathcal{E}_b^n = E \mathcal{E}_b^n \text{ Euler}$$

$$\underbrace{e_i \star x}_{\text{}} \mathcal{E}_b^n = \underbrace{e_i \star x}_{\text{}} \star b \mathcal{E}_b^{n-} = \frac{p}{2} x \star b \mathcal{E}_b^{n-} = n \frac{p}{2} \mathcal{E}_b^n$$

$$\pi'_w \varphi = \underbrace{\alpha_w + \bar{\alpha}_w}_{\text{}} \varphi + \gamma_w \varphi$$

$$\begin{aligned} 0 &= \underbrace{\pi'_w \varphi}_{\text{}} \star \psi + \varphi \star \underbrace{\pi'_w \psi}_{\text{}} = \underbrace{\alpha_w + \bar{\alpha}_w}_{\text{}} \varphi + \gamma_w \varphi \star \psi + \varphi \star \underbrace{\alpha_w + \bar{\alpha}_w}_{\text{}} \psi + \gamma_w \psi \\ &= \varphi \star \underbrace{2\alpha_w \psi + \gamma_w \psi}_{\text{}} + \underbrace{2\alpha_w \varphi + \gamma_w \varphi}_{\text{}} \star \psi \\ &\Rightarrow \varphi \star \underbrace{2\alpha_w \psi + \gamma_w \psi}_{\text{}} = 0 = \underbrace{2\alpha_w \varphi + \gamma_w \varphi}_{\text{}} \star \psi \Rightarrow 2\alpha_w \varphi + \gamma_w \varphi \in \mathcal{H}^\perp \end{aligned}$$

$$\pi'_w \mathcal{E}_b^n = \underbrace{\alpha_w + \bar{\alpha}_w}_{\text{}} \mathcal{E}_b^n + \gamma_w \mathcal{E}_b^n = \pi'_w \mathcal{E}_b^n = \underbrace{2\alpha_w + \gamma_w}_{\text{}} \mathcal{E}_b^n + \underbrace{\bar{\alpha}_w - \alpha_w}_{\text{}} \mathcal{E}_b^n$$

$$P(\pi'_w \gamma) = P(\bar{\alpha}_w - \alpha_w \gamma) = T_{\bar{\alpha}_w - \alpha_w} \gamma$$

$$0 = \underbrace{\pi'_w \mathcal{E}_a^m}_{\mathcal{E}_a^m} \star \mathcal{E}_b^n + \mathcal{E}_a^m \star \underbrace{\pi'_w \mathcal{E}_b^n}_{\mathcal{E}_b^n} = \overline{\alpha_w + \bar{\alpha}_w \mathcal{E}_a^m + \hat{\gamma}_w \mathcal{E}_a^m} \star \mathcal{E}_b^n + \mathcal{E}_a^m \star \overline{\alpha_w + \bar{\alpha}_w \mathcal{E}_b^n + \hat{\gamma}_w \mathcal{E}_b^n}$$

$$= \overline{\alpha_w + \bar{\alpha}_w \mathcal{E}_a^m + \underbrace{w \dot{u} x}_{\mathcal{E}_a^m} + \alpha m \underline{w} \star u + u \star w \mathcal{E}_a^m} \star \mathcal{E}_b^n + \mathcal{E}_a^m \star \overline{\alpha_w + \bar{\alpha}_w \mathcal{E}_b^n + \underbrace{w \dot{u} x}_{\mathcal{E}_b^n} + \alpha n \underline{w} \star u + u \star w \mathcal{E}_b^n}$$

$$0 = \overline{\bar{\alpha}_w \mathcal{E}_a^m + \alpha \underline{u} \star w m \mathcal{E}_a^m} \star \mathcal{E}_b^n + \mathcal{E}_a^m \star \overline{\alpha_w \mathcal{E}_b^n + \underbrace{w \dot{u} x}_{\mathcal{E}_b^n} + \alpha \underline{w} \star u n \mathcal{E}_b^n}$$

$$= \mathcal{E}_a^m \star \overline{2\alpha_w + \alpha(m+n) \underline{w} \star u \mathcal{E}_b^n + \underbrace{w \dot{u} x}_{\mathcal{E}_b^n}} = \mathcal{E}_a^m \star \overline{2\alpha_w + \alpha(2n-1) \underline{w} \star u \mathcal{E}_b^n + \underbrace{w \dot{u} x}_{\mathcal{E}_b^n}}$$

$$\overline{2\alpha_w + \alpha(2n-1) \underline{w} \star u \mathcal{E}_b^n + \underbrace{w \dot{u} x}_{\mathcal{E}_b^n}} \in \mathcal{H}^\perp$$

$$\pi'_w \mathcal{E}_b^n = \alpha_w + \bar{\alpha}_w \mathcal{E}_b^n + \underbrace{w \dot{u} x}_{\mathcal{E}_b^n} + \alpha \underline{w} \star u + u \star w n \mathcal{E}_b^n$$

$$= \overline{2\alpha_w + \alpha(2n-1) \underline{w} \star u \mathcal{E}_b^n + \underbrace{w \dot{u} x}_{\mathcal{E}_b^n} + \bar{\alpha}_w - \alpha_w + \alpha \underline{w} \star u + \alpha(u \star w - w \star u) n \mathcal{E}_b^n}$$

$$P(\pi'_w \mathcal{E}_b^n) = P(\bar{\alpha}_w - \alpha_w + \alpha \underline{w} \star u \mathcal{E}_b^n + \alpha \underline{u} \star w - w \star u n \mathcal{E}_b^n)$$