

$$\begin{cases} \mathcal{P}_1 \text{ feiner als } \mathcal{P}_2 \\ \mathcal{Q}_1 \text{ feiner als } \mathcal{Q}_2 \end{cases} \Rightarrow \mathcal{P}_1 \cap \mathcal{Q}_1 \text{ feiner als } \mathcal{P}_2 \cap \mathcal{Q}_2$$

$\mathcal{P}_n$  equidist partition von  $a|b$ : Intervalle explizit

$\mathcal{P}_n$  feiner als  $\mathcal{P}_m \Leftrightarrow m$  teilt  $n = mk$ : Intervall  $J \in \mathcal{P}_m$  Union von  $k$  Intervallen  $I \in \mathcal{P}_n$

Wann  $\mathcal{P}_m \cap \mathcal{P}_n$  equidist

$$\int \alpha \gamma = \alpha \int \gamma$$

$$\alpha > 0: \frac{\varepsilon}{\alpha}$$

$$\alpha < 0: \underline{\Sigma}_{\mathcal{P}}(-\gamma) = -\bar{\Sigma}_{\mathcal{P}}(\gamma)$$

$$a|c \xrightarrow{\gamma} \mathbb{R} \begin{cases} a|b \\ b|c \end{cases} \xrightarrow[\text{int}]{\gamma} \mathbb{R} \Rightarrow \begin{cases} a|c \xrightarrow{\gamma} \mathbb{R} \\ \text{int} \\ \int_a^c \gamma = \int_a^b \gamma + \int_b^c \gamma \end{cases}$$

nur Partitionen mit Teilpunkt  $b$

$$a|c \xrightarrow{\gamma/\vartheta} \mathbb{R} \begin{cases} \gamma \text{ int} \\ x\gamma = x\vartheta \quad x \neq b \end{cases} \Rightarrow \begin{cases} \vartheta \text{ int} \\ \int_a^c \gamma = \int_a^c \vartheta \end{cases}$$

nur Partitionen mit Teilpunkt  $b$

$$x^2/x^3 \text{ auf } 0|1 \Rightarrow n\text{-equidist } \underline{\Sigma}_n \text{ isoton} / \bar{\Sigma}_n \text{ antiton/integrierbar } \int_0^1 x^2 = \frac{1}{3}/x^3$$

$$\sum_k^{1|n} k^2 = \frac{1}{6}n(n+1)(2n+1)$$

$$\sum_k^{1|n} k^3 = \left(\frac{n(n+1)}{2}\right)^2$$

$$\alpha > 1: \quad {}^x\gamma = x^{-\alpha} \text{ antiton on } 1|\infty: \quad \alpha = 2$$

$$S_k = \sum_{n \geq k} \frac{1}{n^2}: \quad I_k = \int_k^\infty \frac{dx}{x^2} \Rightarrow S_{k+} \leq I_k \leq S_k: \quad \int_1^\infty \frac{dx}{x^\alpha} \text{ vgl } \sum_{n \geq 1} \frac{1}{n^\alpha}$$

$$a|b \begin{matrix} \left\{ \begin{matrix} \gamma \\ \gamma \end{matrix} \right. \\ \text{bes int} \end{matrix} \rightarrow \mathbb{R} \Rightarrow a|b \begin{matrix} \left\{ \begin{matrix} \overline{\gamma} \\ \gamma \max \gamma \\ \gamma \min \gamma \end{matrix} \right. \\ \text{bes int} \end{matrix} \rightarrow \mathbb{R}: \quad \overline{\int_a^b \gamma} \leq \int_a^b \overline{\gamma}$$

$$a|b \xrightarrow[\text{stet}]{\gamma} \mathbb{R}_+ \int^{a|b} \gamma = 0 \Rightarrow \gamma = 0: \quad \text{Ang } {}^c\gamma > 0 \Rightarrow \text{Stet/Widerspruch}$$

$$a|b \xrightarrow[\text{stet}]{\gamma} \mathbb{R} \xrightarrow[\text{ZWS}]{\text{int}} \bigvee_c^{a|b} {}^c\gamma = \frac{1}{b-a} \int_{dt}^{a|b} t\gamma: \quad \text{stet EWS/ZWS}$$

$$a|b \xrightarrow[\text{stet diff}]{\gamma} \mathbb{R} \xrightarrow[\text{MWS}]{\text{int}} \frac{b\gamma - a\gamma}{b-a} = \int_{dt}^{a|b} a+t(b-a)\underline{\gamma}$$

$${}^x\chi = \begin{cases} 1 & x \in \mathbb{Q} \\ 0 & x \in \mathbb{R} \setminus \mathbb{Q} \end{cases} \text{ Graph/Ober/Untersum/nicht integrierbar on } (0|1)$$

$${}^x\gamma = \begin{cases} x & x \in \mathbb{Q} \\ 0 & \text{else} \end{cases} \text{ ?int on } 0|1: \quad \int_0^1 \gamma$$

$$x\gamma_n = \begin{cases} 1 & x = k/n: \quad 0 \leq k \leq n \\ 0 & \text{sonst} \end{cases} \Rightarrow \text{Int}_{0|1}: \int \gamma_n = 0$$

$$\int_0^{\pi/2} x \cos^2: \int_0^{\pi/2} x \cos^2 + x \sin^2$$

momente

$$a|b \xrightarrow[\text{stet}]{\gamma} \mathbb{R}: \quad M_0 = \int_a^b \gamma = 0 \Rightarrow \bigvee_{a < x < b} x\gamma = 0$$

$$\bigwedge_{0 \leq n < N} M_n = \int_a^b x\gamma x^n = 0 \Rightarrow \bigvee_{a < x_0 \dots x_{N-1} < b} \bigwedge_i x_i\gamma = 0$$

$$a|b \xrightarrow[\text{+diff}]{\gamma} \mathbb{R} \Rightarrow \int_a^b x\gamma \cos nx \rightsquigarrow 0$$