

$$a|b \xrightarrow[\text{diff}]{\gamma} \mathbb{R}: \quad x \gamma \begin{cases} > 0 & \geq 0 \\ = 0 & \\ \leq 0 & < 0 \end{cases} \xrightarrow{\text{MWS}} \gamma \begin{cases} \text{s-iso} & \text{w-iso} \\ \text{cst} & \\ \text{w-anti} & \text{s-anti} \end{cases}$$

x^n s-iso on \mathbb{R}_+

γ stet/diff/bij / ${}^y \gamma^{-1}$

$x \in \mathbb{R} \rightarrow \mathbb{R} \ni x^{2k+1}$: streng isoton/bij $\mathbb{R}^{2k+1} = \mathbb{R}$: $g(y) = {}^{2k+1}\sqrt{y}$ nicht diff in 0/ speziell x^3

$$g(f(x)) = x \implies g'(0) f'(0) = 1: \quad f'(0) = 0$$

$$0|\frac{\pi}{2} \xrightarrow{\gamma = \cos^3 - \sin^3} -1|1: \quad {}^0 \gamma^{-1}$$

$$x \in \mathbb{R} \xrightarrow{\gamma} \mathbb{R} \ni x \sin - 2x: \quad {}^0 \gamma^{-1}$$

$$(0|\pi) \xrightarrow{\cot} \mathbb{R}: \quad \mathbb{R} \xrightarrow[\text{diff}]{\cot^{-1}} (0|\pi): \quad {}^y \cot^{-1}$$

$$-\frac{\pi}{2}|\frac{\pi}{2} \xrightarrow[\text{diff/bij}]{\tan} \mathbb{R}: \quad \text{Abl}: \quad \mathbb{R} \xrightarrow[\text{diff}]{\tan^{-1}} -\frac{\pi}{2}|\frac{\pi}{2}: \quad {}^y \tan^{-1}$$

$$-\frac{\pi}{2}|\frac{\pi}{2} \xrightarrow{\sin} -1|1 \text{ streng mon wachsend/surj}: \quad -1|1 \xrightarrow[\text{diff}]{\sin^{-1}} -\frac{\pi}{2}|\frac{\pi}{2}: \quad {}^y \sin^{-1} = \frac{1}{\sqrt{1-y^2}}$$

$$e^x \text{ streng isoton on } \mathbb{R}: \quad e^{\mathbb{R}} = \mathbb{R}_{>}: \quad \exp = \exp: \quad e^x > 0$$

$$a > 0: \quad a^x = e^{x \log a} \text{ on } \mathbb{R}: \quad \text{Monotonie/Wertebereich } a^{\mathbb{R}} \begin{cases} a < 1 \\ a = 1 \\ a > 1 \end{cases}$$

$$j(x) = \frac{1}{x} \text{ beweis diff on } \mathbb{R}^{\times}: \quad \text{Ableitung}$$