

$$\underbrace{-i-j} \underbrace{{}^n\mathbb{C}_n}_{\text{unit}} \underbrace{i+j} \xrightarrow{j} {}^n\mathbb{H}_n$$

$$\begin{aligned} \Gamma \in {}^n\mathbb{C}_n &\Rightarrow \underbrace{-i-j} \Gamma \underbrace{i+j} \underbrace{-i-j}_{*} \Gamma \underbrace{i+j} = \underbrace{-i-j} \Gamma \underbrace{i+j \overbrace{-i-j}^{=j}} \Gamma \underbrace{i+j} \\ &= \underbrace{-i-j} \Gamma j \Gamma \underbrace{i+j} = \underbrace{-i-j} \underbrace{\Gamma \Gamma}_{=1} j \underbrace{i+j} = \underbrace{-i-j} j \underbrace{i+j} = i \\ &\begin{cases} {}^n\mathbb{C}_n \times i = 0 \\ i+j \underbrace{-i-j} = j \end{cases} \Rightarrow \underbrace{-i-j} \underbrace{{}^n\mathbb{C}_n}_{i+j} \times j = 0 \end{aligned}$$