

$$Z = X \times Y \xrightarrow{F} \mathbb{R}$$

$$\mathcal{L}_F = 0$$

$$F(xy) = f(x)g(y)$$

$\mathcal{L}_F = \Delta = \Delta_X \otimes \mathbf{i}_Y + \mathbf{i}_X \otimes \Delta_Y$ second/first order diff op
tangential

$$\Phi(xy) = \sum_n \varphi_n(x) \psi_n(y)$$

$$\Delta_Y \psi_n = \lambda_n \psi_n$$

$$0 = \mathcal{L}_F \Phi = \Delta \Phi = \sum_n \underbrace{\Delta_X \varphi_n \otimes \psi_n + \varphi_n \otimes \Delta_Y \psi_n}_{\text{free}} = \sum_n \underbrace{\Delta_X \varphi_n \otimes \psi_n + \varphi_n \otimes \lambda_n \psi_n}_{\text{free}} = \sum_n \underbrace{\Delta_X + \lambda_n}_{\text{free}} \varphi_n \otimes \underbrace{\psi_n}_{\text{free}}$$

$$\Rightarrow \underbrace{\Delta_X + \lambda_n}_{\text{free}} \varphi_n = 0 \Rightarrow \Delta_X \varphi_n = -\lambda_n \varphi_n \text{ mass}$$

$$\Rightarrow \text{massless spec } \Phi(xy) = \varphi^i(x) \psi_i(y): \psi_i \in \ker \Delta_Y$$

$$\Rightarrow X \xrightarrow[\sigma \text{ model}]{\varphi^i} \ker \Delta_Y \text{ fin dim}$$