

$$D = 7$$

$$E_8^4 = SL_5^{\mathbb{R}}: \quad \text{scalar coset } SL_5^{\mathbb{R}} /$$

$$E_7^4 GL_3^{\mathbb{R}}: \quad \text{scalar coset } GL_3^{\mathbb{R}} / O_3$$

$$E_6^4 = GL_2^{\mathbb{R}}: \quad \text{scalar coset } GL_2^{\mathbb{R}} / O_2$$

$$E_5^4 = \mathbb{R}: \quad \text{scalar coset } O_{1,1} \ni \mathbb{Q} \text{ dilaton}$$

$$\begin{cases} \mathbb{V} \\ \mathbb{Q} \\ \mathbb{Z} \end{cases} = \boxed{\mathbb{V}} + \frac{2}{\mathbb{Q}} - e^{2\sqrt{2/5}\mathbb{Q}} \frac{2}{\mathbb{Z}}$$

7-dim bosonic string

$$E_4^4 = 1$$

pure gravity

$$F_4^4 = 1$$

$$D_8^4 = O_{3,3} \times O_{1,1}: \quad \text{scalar coset } O_{3,3} / O_3 \times O_3 \times \mathbb{R}_>$$