

$D = 11$ SUGRA bosonic Lagrangian

$$3 \frac{2}{5}$$

$$\begin{cases} e_\mu^m & \text{vielbein } 44 \\ \lambda_{\mu\nu} \mathcal{F} & \text{3 potential } 84 \\ \mu \mathcal{I} & \text{Majorana gravitino } 2^7 = 128 \end{cases}$$

$$d^{11} x \sqrt{-G} \left(R - \frac{1}{48} \mathcal{F}^2 \right) + \frac{\sqrt{2}}{2^7 3^2} \mathcal{F} \mathcal{F}^2$$

$$2 (*R_{11} - \mathcal{L}_{11}) = \frac{2}{3} \mathcal{F}^2$$

$$SO_{1:10}$$

$$N = 1 \text{ SUSY } Q_\alpha$$

$$E_8 = 1$$

$$*\mathcal{F} + \frac{1}{2} \mathcal{F}^2 = 0$$

$$2 \frac{\mathcal{F}^\mu}{c} \frac{\mathcal{F}^a}{\mu} \eta_{ae} = \frac{\mathcal{F}^\mu \mathcal{F}^\nu}{c} \frac{\mathcal{F}^a}{\mu} \eta_{fb} - \eta_{cf} \frac{\mathcal{F}^\mu \mathcal{F}^\nu}{e} \frac{\mathcal{F}^a}{\mu} + \frac{\mathcal{F}^\mu \mathcal{F}^\nu}{c} \frac{\mathcal{F}^a}{\mu} \eta_{ae}$$

bosonic

$$V = \det V_M^A$$

$$F_{ABCD} = \partial_A V_{BCD} - \partial_D V_{BCA} + 3\omega_{AB}^E V_{CDE} - 3\omega_{CD}^E V_{ABE}$$

$$\partial_A = V_A^M \partial_M$$

$$R_{BMN}^A = \partial_M \omega_{NB}^A + \omega_{ME}^A \omega_{NB}^E - \partial_N \omega_{MB}^A - \omega_{NE}^A \omega_{MB}^E$$

$$R = V_A^M V_C^N R_{BMN}^A \eta^{BC} = \omega_{ABC} \omega^{CAB} - 2V^{-1} \partial_M (V V_A^M \omega^A)$$

VR

$$V F_{ABCD} F^{ABCD}$$

$$\varepsilon^{A_0 \dots A_{10}} F_{A_0 \dots A_3} F_{A_4 \dots A_7} V_{A_8 \dots A_{10}}$$

motion

$$M \in 11$$

$$\psi_M = 0$$

$$R_{MN} - \frac{1}{2} g_{MN} R = \frac{1}{3} F_{MPQR} F_N{}^{PQR} - \frac{1}{24} g_{MN} F_{PQRS} F^{PQRS}$$

$$\partial_M F^{MM_8 M_9 M_{10}} = -\frac{1}{576} \varepsilon^{M_0 \dots M_7 M_8 M_9 M_{10}} F_{M_0 \dots M_3} F_{M_4 \dots M_7}$$

DUF 50