

$$p, q \in \mathbb{N} \Rightarrow \int_0^1 x^p (1-x)^q = \frac{p!q!}{(p+q+1)!} = \frac{\Gamma_{p+1}\Gamma_{q+1}}{\Gamma_{p+q+2}} = B_{p+1, q+1}$$

$$0 = q: \int_0^1 x^p = \frac{x^{p+1}}{p+1} \Big|_0^1 = \frac{1}{p+1} = \frac{p!0!}{(p+0+1)!}$$

$$\begin{aligned} 0 \leq q \rightsquigarrow q+1: \int_0^1 x^p (1-x)^{q+1} &= \frac{x^{p+1}}{p+1} (1-x)^{q+1} \Big|_0^1 - \frac{q+1}{p+1} (-1) \int_0^1 x^{p+1} (1-x)^q \\ &= \frac{q+1}{p+1} \int_0^1 x^{p+1} (1-x)^q \stackrel{\text{ind}}{=} \frac{q+1}{p+1} \frac{(p+1)!q!}{(p+q+2)!} = \frac{p!(q+1)!}{(p+q+2)!} \end{aligned}$$

$$\frac{d\bar{z}dz}{2i} = dx dy = r dr d\vartheta$$

$$d\bar{z}dz = (dx - idy) \wedge (dx + idy) = 2i dx dy$$

$$\Gamma_\nu = \int_0^\infty e^{-t} t^{\nu-1} dt$$

$$\nu \Gamma_\nu = \Gamma_{\nu+1}$$

$$\Gamma_{n+1} = n!$$

$$\text{Poch: } (\nu)_m = \frac{\Gamma_{\nu+m}}{\Gamma_\nu} = \nu(\nu+1)\cdots(\nu+m-1)$$

$$(1-x)^{-\nu} = \sum_m^{\mathbb{N}} \frac{(\nu)_m}{m!} x^m = \sum_m^{\mathbb{N}} (\nu)_m \frac{x^m}{m!}$$

$$(1+x)^\alpha = \sum_m^{\mathbb{N}} \begin{bmatrix} \alpha \\ m \end{bmatrix} x^m$$

$$\begin{bmatrix} \alpha \\ m \end{bmatrix} = \frac{\alpha!}{m!(\alpha-m)!} = \frac{\alpha(\alpha-1)\cdots(\alpha+1-m)}{m!}$$

$$(1-x)^{-\nu} = \sum_m^{\mathbb{N}} \begin{bmatrix} -\nu \\ m \end{bmatrix} (-1)^m x^m$$

$$\begin{bmatrix} -\nu \\ m \end{bmatrix} (-1)^m = (-1)^m \frac{(-\nu)(-\nu-1)\cdots(-\nu+1-m)}{m!} = \frac{\nu(\nu+1)\cdots(\nu-1+m)}{m!} = \frac{(\nu)_m}{m!}$$

$$\nu \int_{\mathbb{B}} \frac{d\bar{z}dz}{2\pi i} (1-z\bar{z})^{\nu-2} \bar{z}^m z^m = \frac{m!}{(\nu)_m}$$

$$\text{LHS} = \frac{\nu}{\pi} \int_{d\vartheta}^{0|2\pi} \int_{dr}^{0|1} r (1-r^2)^{\nu-2} r^{2m} = 2\nu \int_{dr}^{0|1} r (1-r^2)^{\nu-2} r^{2m}$$

$$= \nu \int_{dx}^{0|1} (1-x)^{\nu-2} x^m = \nu \frac{(\nu-2)!m!}{(\nu+m-1)!} = \nu \frac{\Gamma_{\nu-1}m!}{\Gamma_{\nu+m}} = \frac{\Gamma_\nu m!}{\Gamma_{\nu+m}} = \text{RHS}$$

$$\text{W-Mass } \mu_\nu(dz) = \nu \frac{d\bar{z}dz}{2\pi i} (1-z\bar{z})^{\nu-2}$$

$$\text{ONB : } \underline{z^m}_\nu = \frac{(\nu)_m^{1/2}}{\sqrt{m!}} z^m$$

$$\text{kernel } {}^z K_w^\nu = (1 - z\bar{w})^{-\nu}$$

$$\text{LHS} = \sum_m^{\mathbb{N}} \frac{z^m}{m!} \frac{\bar{w}^m}{m!} = \sum_m^{\mathbb{N}} \frac{(\nu)_m}{m!} (z\bar{w})^m = (1 - z\bar{w})^{-\nu}$$