

$$\begin{array}{ccc}
& \mathbb{G}_1^n & \\
Z_j & \supset U & \\
\downarrow \text{taut} & & \\
Gr_j(\mathbb{C}^r) = K_j^j & \ni U & \\
\det Z_j & \supset \Delta_U & \\
\downarrow & & \\
Gr_j(\mathbb{C}^r) = K_j^j & \ni U &
\end{array}$$