

Maldacena

D3/3 decoupling

M theory limits $\begin{cases} \text{geom sing} \\ \text{brane/bulk decoupling} \end{cases}$

$$\text{IIB} \begin{cases} D_4^- & \text{parallel } N \\ g_s & \text{dist} = U g_s^2 \end{cases} \rightsquigarrow \text{YM} \begin{cases} D_4^- & U_N \\ \mathcal{N} = 4 \end{cases}$$

$$g_s \rightsquigarrow 0$$

s-conformal point $r=0$

N parallel coincident $D_4^- : t \frac{u^3}{v^3} s^3$

$${}^{vs}H^{1/2} \mathfrak{Q} = \underline{u}^2 - \underline{t}^2 + {}^{vs}H \left(\frac{u^2}{v^2} + \frac{2}{v^2} \underline{v} s^2 \right)$$

$${}^{vs}H = 1 + \frac{4\pi \alpha' g_s N}{v^4}$$

$$\mathcal{A} = \dots \Rightarrow \text{flux } N = \mathbb{S}_{v_s}^5 | \underline{\mathcal{A}}$$

decoupling limit

$$R^4 = 4\pi \alpha' g_s N$$

$$N \rightsquigarrow \infty$$

$$\text{AdS}_R^5 \times \mathbb{S}_R^5$$

$$\text{YM coupling } \frac{2\pi}{g_{\text{YM}}^2} + i \frac{\Theta}{4\pi} = \frac{1}{\mathfrak{Q}} + \frac{i}{2\pi} \emptyset \quad \text{IIB coupling}$$