

Borcherds

$$\text{modular } {}^q\eta = \sum q^n \prod_n^{\infty i} \eta$$

$$\Delta_{\text{eff}}(T:U) = 2\pi i(aT + bU) + \sum_{k \wedge \ell > 0} \log \left(1 - \mathbf{e}^{2\pi i(kT + \ell U)} \right) \prod_{k\ell}^{\infty i} \eta$$

no Wilson lines=unbroken gauge symm

$$E_8 \times E'_8$$

$$\frac{1}{4} \Delta_{\text{eff}}(T:U) = 24\pi i a T - \sum_{k \wedge \ell > 0} \log \left(1 - \mathbf{e}^{2\pi i(kT + \ell U)} \right) \prod_{k\ell}^{\infty i} \frac{(E_2 E_4 - E_6)^2}{\eta^{24}}$$

$$E_8 \times E_8$$

$$\frac{1}{2} \Delta_{\text{eff}}(T:U) = 12\pi i(8T + 12U) - \sum_{k \wedge \ell > 0} \log \left(1 - \mathbf{e}^{2\pi i(kT + \ell U)} \right) \prod_{k\ell}^{\infty i} \frac{E_4 (E_2^2 E_4 - 2E_2 E_6 + E_4^2)}{\eta^{24}}$$

$$\text{hol prepotential } \mathcal{G}_{T:U} = \sum_{k \wedge \ell > 0} \log_5 \left(\mathbf{e}^{2\pi i(kT + \ell U)} \right) \prod_{k\ell}^{\infty i} \frac{E_4^2}{\eta^{24}}$$

$${}^q\log_p = \sum_{n > 0} \frac{q^n}{n^p}$$

$$\Delta_{\text{eff}}(T:U) = \partial_T^2 \partial_U^2 \mathcal{G}_{T:U}$$

symm enhancement

$$T = U: \quad \text{SU}_2$$

$$T = U = i: \quad \text{SU}_2 \times \text{SU}_2$$

$$T = U = \varrho = \mathbf{e}^{2\pi i/3}: \quad \text{SU}_3$$