

$${}^o C_k \in \mathbf{U} | C^\lambda$$

$$0 < {}^o C_o \in \mathbf{\Psi} | C^\lambda$$

$${}^o C_k {}^o C_o = {}^o C_o {}^o C_k$$

$${}^z C_z = {}^o C_{\neq}^* {}^o C_o {}^o C_{\neq}$$

$$\emptyset = e_G \Rightarrow {}^o C_{\emptyset} = e_C$$

$${}^{zg} C_{wg} = {}^w C_g^* {}^z C_w {}^z C_g \in C^{\mathbb{C}}$$

$$\begin{array}{ccc}
 C^\lambda & \xrightarrow{{}^z C_w^\lambda} & C^\lambda \\
 {}^z C_g^\lambda \uparrow & & \downarrow {}^w C_g^* \\
 C^\lambda & \xrightarrow{{}^{zg} C_{wg}^\lambda} & C^\lambda
 \end{array}$$

$${}^z g = k \neq g$$

$${}^o C_{\neq g} = {}^o C_{k \neq g} = {}^o C_k {}^o C_{\neq} {}^z C_g$$

$$\text{LHS} = {}^o C_{\neq g}^* {}^o C_o {}^o C_{\neq g} = {}^o C_{k \neq g}^* {}^o C_o {}^o C_{k \neq g} = \overbrace{{}^o C_k {}^o C_{\neq} {}^z C_g}^* {}^o C_o {}^o C_k {}^o C_{\neq} {}^z C_g$$

$$= {}^z C_g^* {}^o C_{\neq}^* {}^o C_k {}^o C_o {}^o C_k {}^o C_{\neq} {}^z C_g = {}^z C_g^* {}^o C_{\neq}^* {}^o C_o {}^o C_{\neq} {}^z C_g = \text{RHS}$$

$$C_g^{-\chi} \underbrace{C_w^{-\chi} \mathbf{1}} = C_{wg}^{-\chi} \underbrace{C_g^{*\chi} \mathbf{1}}$$

$$\begin{array}{ccc}
 D \begin{array}{c} \triangle \\ \downarrow \\ w \end{array} C^\chi & \xleftarrow{C_w^{-\chi}} & C^\chi \\
 \uparrow C_g^\chi & & \downarrow C_g^{*\chi} \\
 D \begin{array}{c} \triangle \\ \downarrow \\ w \end{array} C^\chi & \xleftarrow{C_{wg}^{-\chi}} & C^\chi
 \end{array}$$

$${}^{zg}\text{LHS} = {}^{zg}C_g^{-1\chi} \overline{{}^z C_w^{-\chi} \mathbf{1}} = {}^z C_g^{-\chi} {}^z C_w^{-\chi} \mathbf{1} = {}^{zg} C_{wg}^{-\chi} {}^w C_g^{*\chi} \mathbf{1} = {}^{zg}\text{RHS}$$

$${}_C G^{-\chi} = \int_{dx}^D {}^o C G_x^{-\chi} {}^x C G_x {}^x C G_o^{-\chi} = \int_{dx}^D {}^o C G_x^{-\chi} {}^o \mathfrak{g}_z {}^* \mathcal{J} {}^o \mathfrak{g}_z {}^x C G_o^{-\chi}$$

$$\mathcal{J} \xrightarrow[\text{bij}]{} \bar{\mathcal{J}} = \int_{dx}^D {}^o C G_x^{-1} {}^x C G_x {}^x C G_o^{-1}$$

$${}^z C G_w^{-\chi} = \int_{dx}^D {}^z C G_x^{-\chi} {}^x C G_x {}^x C G_w^{-\chi}$$

$$\begin{aligned}
 \int_{dx}^D {}^z C G_x^{-\chi} {}^x C G_x {}^x C G_z^{-\chi} &= \int_{dx}^D {}^{o\mathfrak{g}_z} C G_x^{-\chi} {}^{x\mathfrak{g}_z} C G_x {}^{x\mathfrak{g}_z} C G_o^{-\chi} = \int_{dx}^D \overline{{}^{x\mathfrak{g}_z} C G_x^{-\chi} {}^{o\mathfrak{g}_z} C G_x {}^{o\mathfrak{g}_z} C G_o^{-\chi}}^{-1} \\
 &= {}^{o\mathfrak{g}_z} C G_z^{-1} \int_{dx}^D {}^o C G_x^{-\chi} {}^x C G_x {}^x C G_o^{-\chi} {}^{o\mathfrak{g}_z} C G_z^{-1} = {}^{o\mathfrak{g}_z} C G_z^{-1} {}^o C G^{-\chi} {}^{o\mathfrak{g}_z} C G_z^{-1} = \overline{{}^{o\mathfrak{g}_z} C G_x^{-\chi} {}^{o\mathfrak{g}_z} C G_o^{-\chi}}^{-1} = {}^z C G_z^{-\chi}
 \end{aligned}$$

$${}^w \underset{C}{g}^* \underset{C}{G}_w^\chi \underset{C}{g} = \underset{C}{G}_{wg}^\chi$$

$$\begin{aligned} \int_{dz}^D \underbrace{{}^z g \underset{C}{G}_{wg}^{-\chi} \underset{C}{g}^* \mathbf{1} \bowtie \underset{C}{G}_z^z \overline{g \bowtie \mathbf{1}}}_{\text{}} &= \int_{dz}^D \underbrace{{}^z g \underset{C}{G}_{wg}^{-\chi} \underset{C}{g}^* \mathbf{1} \bowtie \underset{C}{g}^* \underset{C}{G}_z^z \overline{g \bowtie \mathbf{1}}}_{\text{}} = \int_{dz}^D \underbrace{{}^z g \underset{C}{G}_{wg}^{-\chi} \underset{C}{g}^* \mathbf{1} \bowtie \underset{C}{G}_{zg}^z \overline{g^{-1} \overline{g}^z \bowtie \mathbf{1}}}_{\text{}} \\ &= \int_{dz}^D \underbrace{{}^z g \underset{C}{G}_{wg}^{-\chi} \underset{C}{g}^* \mathbf{1} \bowtie \underset{C}{G}_{zg}^z \overline{g \bowtie \mathbf{1}}}_{\text{}} \stackrel{\text{inv}}{=} \int_{dz}^D \underbrace{{}^z G_{wg}^{-\chi} \underset{C}{g}^* \mathbf{1} \bowtie \underset{C}{G}_z^z \overline{g \bowtie \mathbf{1}}}_{\text{}} = \underbrace{{}^z G_{wg}^{-\chi} \underset{C}{g}^* \mathbf{1} \bowtie \mathbf{1}}_{\text{}} \\ &= \underbrace{\overline{{}^w \mathbf{1} \bowtie \mathbf{1}}}_{\text{}} \overline{g \bowtie \mathbf{1}} = \mathbf{1} \bowtie \underbrace{{}^w g \overline{g \bowtie \mathbf{1}}}_{\text{}} = \mathbf{1} \bowtie \overline{g \bowtie \mathbf{1}} = \underbrace{{}^z G_w^{-\chi} \mathbf{1} \bowtie g \overline{g \bowtie \mathbf{1}}}_{\text{}} = \int_{dz}^D \underbrace{{}^z G_w^{-\chi} \mathbf{1} \bowtie \underset{C}{G}_z^z \overline{g \bowtie \mathbf{1}}}_{\text{}} \end{aligned}$$

$$\int_{dx}^D \underset{C}{G}_x^{-\chi} \underset{C}{G}_x^x \underset{C}{G}_z^{-\chi} = \underset{C}{g}^{-1} \left( \int_{dx}^D \underset{C}{G}_x^{-\chi} \underset{C}{G}_x^x \underset{C}{G}_o^{-\chi} \right) \underset{C}{g}^* \underset{z}{\text{}} \underset{C}{g}^*$$

= C

$$\begin{aligned} \int_{dx}^D \underset{C}{G}_x^{-\chi} \underset{C}{G}_x^x \underset{C}{G}_z^{-\chi} &= \int_{dx}^D \underset{C}{G}_x^{-\chi} \underset{C}{G}_x^x \underset{C}{G}_{og}^{-\chi} = \int_{dx}^D \underset{C}{G}_{xg}^{-\chi} \underset{C}{G}_{xg}^x \underset{C}{G}_{og}^{-\chi} = \int_{dx}^D \underset{C}{g}^{-1} \underset{C}{G}_x^{-\chi} \underset{C}{g}^* \overline{\underset{C}{g}^{-1} \underset{C}{G}_x^{-\chi} \underset{C}{g}^*} \underset{C}{g}^{-1} \underset{C}{G}_o^{-\chi} \underset{C}{g}^* \\ &= \int_{dx}^D \underset{C}{g}^{-1} \underset{C}{G}_x^{-\chi} \underset{C}{g}^* \underset{C}{g} \underset{C}{G}_x^x \underset{C}{g}^* \underset{C}{g}^{-1} \underset{C}{G}_o^{-\chi} \underset{C}{g}^* = \int_{dx}^D \underset{C}{g}^{-1} \underset{C}{G}_x^{-\chi} \underset{C}{G}_x^x \underset{C}{G}_o^{-\chi} \underset{C}{g}^* = \underset{C}{g}^{-1} \int_{dx}^D \underbrace{\underset{C}{G}_x^{-\chi} \underset{C}{G}_x^x \underset{C}{G}_o^{-\chi}}_{\text{}} \underset{C}{g}^* \end{aligned}$$