

unit ball

$$\lambda = 1 - \ell$$

$$D_{\frac{2}{w}}^{d+\ell} \mathbb{C} = \sum_{\mu_r \geq \ell} Z_{\bullet}^{\mu} \mathbb{C}$$

$$\gamma_{d+\ell} \times \gamma = \sum_{\mu \geq \ell} \frac{\gamma^{\mu} \times \gamma^{\mu}}{(\ell-1)! (\mu-\ell)!}$$

$$\lambda = 0$$

$$D_{\frac{2}{w}}^{d+1} \mathbb{C} = \sum_{\mu_r > 0} Z_{\bullet}^{\mu} \mathbb{C}$$

$$\gamma_{d+2} \times \gamma = \sum_{\mu > 0} \frac{\gamma^{\mu} \times \gamma^{\mu}}{(\mu-1)!}$$

$$\alpha > (r-1) a/2$$

$$\ell \in \mathbb{N}$$

$$z \overbrace{\mathfrak{S}_e^{\ell} \gamma}^{\Delta_z^{-\alpha-\ell}} = \frac{\Gamma_{\alpha+\ell}}{\Gamma_{\alpha}} \underbrace{\mathfrak{S}_e^{\ell} \Delta_z^{-\alpha-\ell}}_{\times \gamma}$$

$$z \mathfrak{S}_e^{\ell} z \mathfrak{S}_w^{\mu} w \mathfrak{S}_e^{-\ell} = \frac{(d/r)_{\mu+\ell}}{(d/r)_{\mu}} z \mathfrak{S}_w^{\mu+\ell}$$

$$z \mathfrak{S}_e^{\ell} z \Delta_w^{-\alpha-\ell} = \sum_{\mu \geq 0} \frac{(\alpha+\ell)_{\mu}}{(d/r)_{\mu}} \frac{(d/r)_{\mu+\ell}}{(d/r)_{\mu}} z \mathfrak{S}_w^{\mu+\ell} w \mathfrak{S}_e^{-\ell}$$

$$\Rightarrow \underbrace{\mathfrak{S}_e^{\ell} \Delta_z^{-\alpha-\ell}}_{\times \gamma} = \sum_{\mu \geq 0} \frac{(\alpha+\ell)_{\mu}}{(d/r)_{\mu}} \frac{(d/r)_{\mu+\ell}}{(d/r)_{\mu+\ell}} z \gamma_{\mu+\ell} z \mathfrak{S}_e^{-\ell} = \frac{\Gamma_{\alpha}}{\Gamma_{\alpha+\ell}} \sum_{\nu_r \geq \ell} \frac{(d/r)_{\nu}}{(d/r)_{\nu-\ell}} z \gamma_{\nu} z \mathfrak{S}_e^{-\ell} = \frac{\Gamma_{\alpha}}{\Gamma_{\alpha+\ell}} z \overbrace{\mathfrak{S}_e^{\ell} \gamma}$$

$\lambda \in$ pole set

$$\ell = d/r - \lambda$$

$$\nu = \ell + d/r = p - \lambda$$

$$\partial \mathfrak{s}_e^\ell \underbrace{g \mathfrak{K}_\lambda \eta}_{\lambda} = g \mathfrak{K}_{p-\lambda} \underbrace{\partial \mathfrak{s}_e^\ell \eta}_{\lambda}$$

$$v = u \cdot \varphi_a \Rightarrow \begin{cases} u = v \cdot \varphi_a \\ du = \overline{v \varphi_a} dv \end{cases}$$

$$v \varphi_a \mathfrak{s}_e = \frac{a-v}{v} \mathfrak{s}_e = \frac{-v \mathfrak{s}_e^a \Delta_v}{v \Delta_a}$$

$$\begin{aligned} \frac{\Gamma_\alpha}{\Gamma_{\alpha+\ell}} z \overbrace{\partial \mathfrak{s}_e^\ell \varphi_a \mathfrak{K}_\lambda \eta}^{\alpha = d/r} &\stackrel{\text{Lem}}{=} \underbrace{\mathfrak{s}_e^\ell \Delta_z^{\lambda-p}}_{d/r} \mathfrak{K}_{d/r} \underbrace{\varphi_a \mathfrak{K}_\lambda \eta}_{\lambda} = \int_S u \varphi_a \eta u \varphi_a^{\lambda/p} u \overline{\mathfrak{s}_e}^\ell z \Delta_u^{\lambda-p} = \int_S \overline{v \varphi_a}^v \eta v \varphi_a^{-\lambda/p} v \varphi_a \overline{\mathfrak{s}_e}^\ell z \Delta_{v \varphi_a}^{\lambda-p} \\ &= \int_S v \eta v \overline{\mathfrak{s}_e}^\ell z \varphi_a \Delta_v^{\lambda-p} \frac{v \Delta_a^\ell}{a \Delta_v^\ell} z \varphi_a^{1-\lambda/p} \overline{v \varphi_a}^v v \varphi_a^{-\lambda/p} v \overline{\varphi_a}^{1-\lambda/p} \\ &= z \varphi_a^{1-\lambda/p} \int_S v \eta v \overline{\mathfrak{s}_e}^\ell z \varphi_a \Delta_v^{\lambda-p} v \Delta_a^{(\ell + \overline{\lambda} - p/2)} a \Delta_v^{(-\ell + p - \overline{\lambda} - p/2)} a \Delta_a^{\overline{p \lambda/p - 1 - \lambda/p + 1/2}} \\ &= z \varphi_a^{\nu/p} \int_S v \eta v \overline{\mathfrak{s}_e}^\ell v \overline{\Delta}_{z \varphi_a}^{\lambda-p} = z \varphi_a^{1-\lambda/p} \overbrace{\partial \mathfrak{s}_e^\ell \eta}^{z \varphi_a} = z \overbrace{\varphi_a \mathfrak{K}_{p-\lambda} \eta} \end{aligned}$$

$$z \mathfrak{s}_e^\ell w \overline{\mathfrak{s}_e}^\ell z \Delta_w^{-\alpha+\ell} = {}_2F_1(d/r; \alpha | \lambda)$$