

$$\frac{1}{2} z v^u B_u = -z \overset{*}{u} v - z \overset{*}{v} u + u \overset{*}{u} \overset{*}{z} u v + u \overset{*}{v} \overset{*}{z} u u$$

$$S_\ell \xleftarrow{\tilde{g}} S_\ell$$

$$T_{\tilde{g}(u)}(S_\ell) \xleftarrow{T_u(\tilde{g})} T_u(S_\ell)$$

$$T_u(S_\ell) \xleftarrow{h^{-1} T_u(\tilde{g})} T_u(S_\ell)$$

$$T_u(S_\ell) = i X_u \times Z_u^{1/2}$$

$$T_u(\tilde{g}) = \frac{A_u}{0} \Big| \frac{*}{\tilde{g}'(u)}$$

$$\left(\tilde{g}_1 \tilde{g}_2 \right)'(u) = \tilde{g}'_1(\tilde{g}_2(u)) \tilde{g}'_2(u)$$

$$\overline{\det T_u(\tilde{g})} = \det A_u \overline{\det \tilde{g}'(u)}$$

$$\lambda_w - \overset{u}{\tilde{\gamma}}_w = \frac{\overset{*}{u}(w_1 + \overset{*}{w}_1)}{0} \Big| \frac{2 \overset{*}{u} w_{1/2}}{\overset{*}{u}(w_1 + \overset{*}{w}_1) - 2Q(w_0; u)}$$

$$\mathbb{L} \xrightarrow{\text{alin}} \mathbb{L} \Rightarrow \text{tr } \mathbb{L}_{\mathbb{R}} = 0$$

$$Jz = iz \Rightarrow J_{\mathbb{R}}^2 = -1_{\mathbb{R}}$$

$$\mathbb{L}_{\mathbb{R}} J_{\mathbb{R}} = -J_{\mathbb{R}} \mathbb{L}_{\mathbb{R}} \Rightarrow \mathbb{L}_{\mathbb{R}} = J_{\mathbb{R}} \mathbb{L}_{\mathbb{R}} J_{\mathbb{R}}$$

$$\text{tr } \mathbb{L}_{\mathbb{R}} = \text{tr } J_{\mathbb{R}} \mathbb{L}_{\mathbb{R}} J_{\mathbb{R}} = \text{tr } J_{\mathbb{R}}^2 \mathbb{L}_{\mathbb{R}} = \text{tr } (-1_{\mathbb{R}}) \mathbb{L}_{\mathbb{R}} = -\text{tr } \mathbb{L}_{\mathbb{R}}$$

$$x \in X_u$$

$$\text{tr}_{iX_u}^{\mathbb{R}} \underline{\dot{u}} x = \left(1 + \frac{a}{2}(\ell - 1)\right) x|u$$

$$\text{tr}_{Z_u^{1/2}}^{\mathbb{C}} \underline{\dot{u}} x = \frac{b + (r - \ell)a}{2} x|u$$

$$\text{tr}_{iX_u}^{\mathbb{R}} \underline{\dot{u}} x = \sum_i \underline{y_i \dot{u} x} | y_i = c_1 x|u$$

$$c_1 \ell = c_1 u|u = \sum_i \underline{y_i \dot{u} u} | y_i = \sum_i y_i | y_i = \dim iX_u = \ell + \frac{a}{2} \ell(\ell - 1) \Rightarrow c_1 = 1 + \frac{a}{2}(\ell - 1)$$

$$Z_u^{1/2} = \sum_{1 \leq i \leq \ell < j \leq r} Z_{ij} \oplus \sum_{1 \leq i \leq \ell} Z_{i0}$$

$$\text{tr}_{Z_u^{1/2}}^{\mathbb{C}} \underline{\dot{u}} x = \sum_j \underline{v_j \dot{u} x} | v_j = c_2 x|u$$

$$c_2 \ell = c_2 u|u = \sum_j \underline{v_j \dot{u} u} | v_j = \frac{1}{2} \sum_j v_j | v_j = \frac{1}{2} \dim Z_u^{1/2} = \frac{\ell b + \ell(r - \ell)a}{2} \Rightarrow c_2 = \frac{b + (r - \ell)a}{2}$$

$$\text{Re tr}_{iX_u} \left(\lambda_w - u \underline{\tilde{\gamma}}_w \right) = \left(\frac{d}{r} + \frac{a}{2}(r - \ell) \right) (w|u + u|w)$$

$$\text{Re tr} \frac{\underline{\dot{u}} w_1 + \dot{w}_1}{0} \Big| \frac{2 \underline{\dot{u}} w_{1/2}}{\underline{\dot{u}} w_1 + \dot{w}_1 - 2Q(w_0; u)} = \text{tr}_{iX_u} \underline{\dot{u}} w_1 + \dot{w}_1 + \text{Re tr}_{Z_u^{1/2}} \underline{\dot{u}} w_1 + \dot{w}_1$$

$$u \underline{\tilde{\delta}}_w = \frac{1}{2} \text{tr}_{iX_u}^{\mathbb{R}} \underline{\dot{u}} w_1 + \dot{w}_1 + \text{tr}_{Z_u^{1/2}}^{\mathbb{C}} \underline{\dot{u}} w_1 + \dot{w}_1 = \left(\frac{d}{r} + \frac{a}{2}(r - \ell) \right) \frac{w|u + u|w}{2}$$

$$\frac{1}{2} \left(1 + \frac{a}{2}(\ell - 1) + b + (r - \ell)a \right) \underline{w_1 + \dot{w}_1} | u = \left(1 + \frac{a}{2}(\ell - 1) + b + (r - \ell)a \right) \frac{w|u + u|w}{2}$$

$$= \left(1 + a \left(r - \frac{\ell + 1}{2} \right) + b \right) \frac{w|u + u|w}{2} = \left(\frac{d}{r} + \frac{a}{2}(r - \ell) \right) \frac{w|u + u|w}{2}$$